

# RADAR SOUNDING OF THE AURORAL PLASMA

by

CESAR LA HOZ

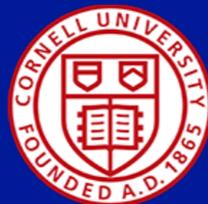
[cesar.la.hoz@uit.no](mailto:cesar.la.hoz@uit.no)

with contributions by my friends

Brett Isham, Mike Kosch and Mike Rietveld



THE ARCTIC UNIVERSITY OF NORWAY



CORNELL UNIVERSITY

# OUTLINE

1. Background on Radar Incoherent Scattering theory
2. Natural Enhanced Ion Acoustic Lines, NEIAL
3. Polar Mesospheric Summer Echoes, PMSE
4. Langmuir turbulence: decay and cavitating instability

disclaimer: time constraint and personal participation have defined this work



EISCAT

near Tromsø

Northern Norway

VHF radar

UHF radar

HF Heater

# EISCAT

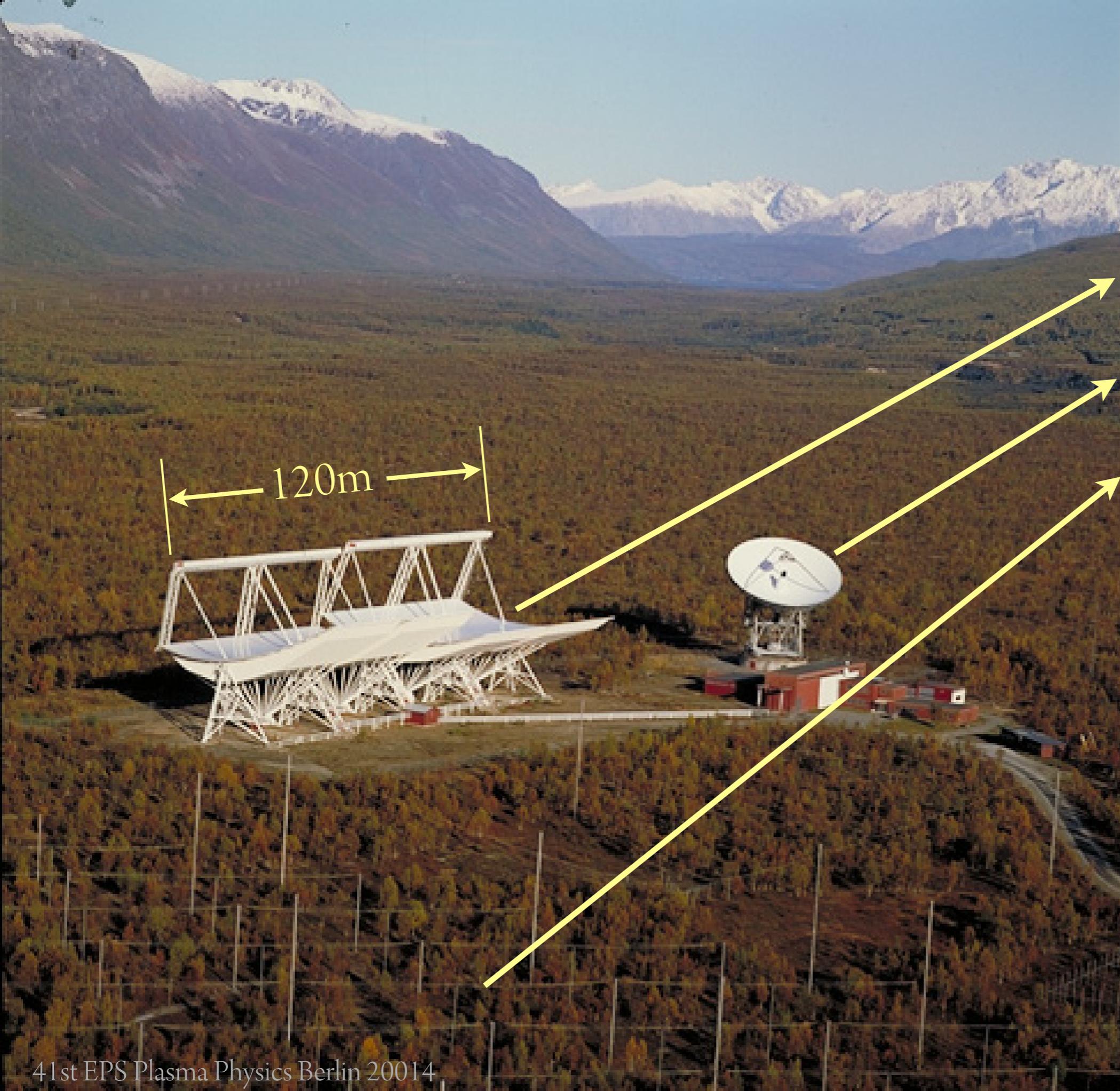
near Tromsø  
Northern Norway

VHF radar

UHF radar

HF Heater

120m

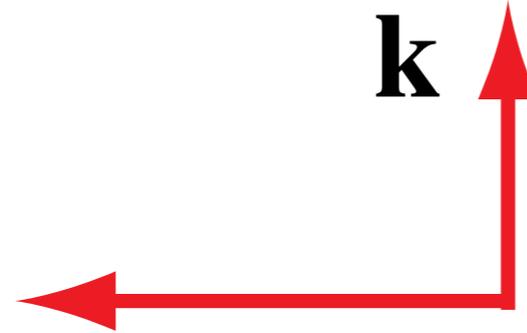
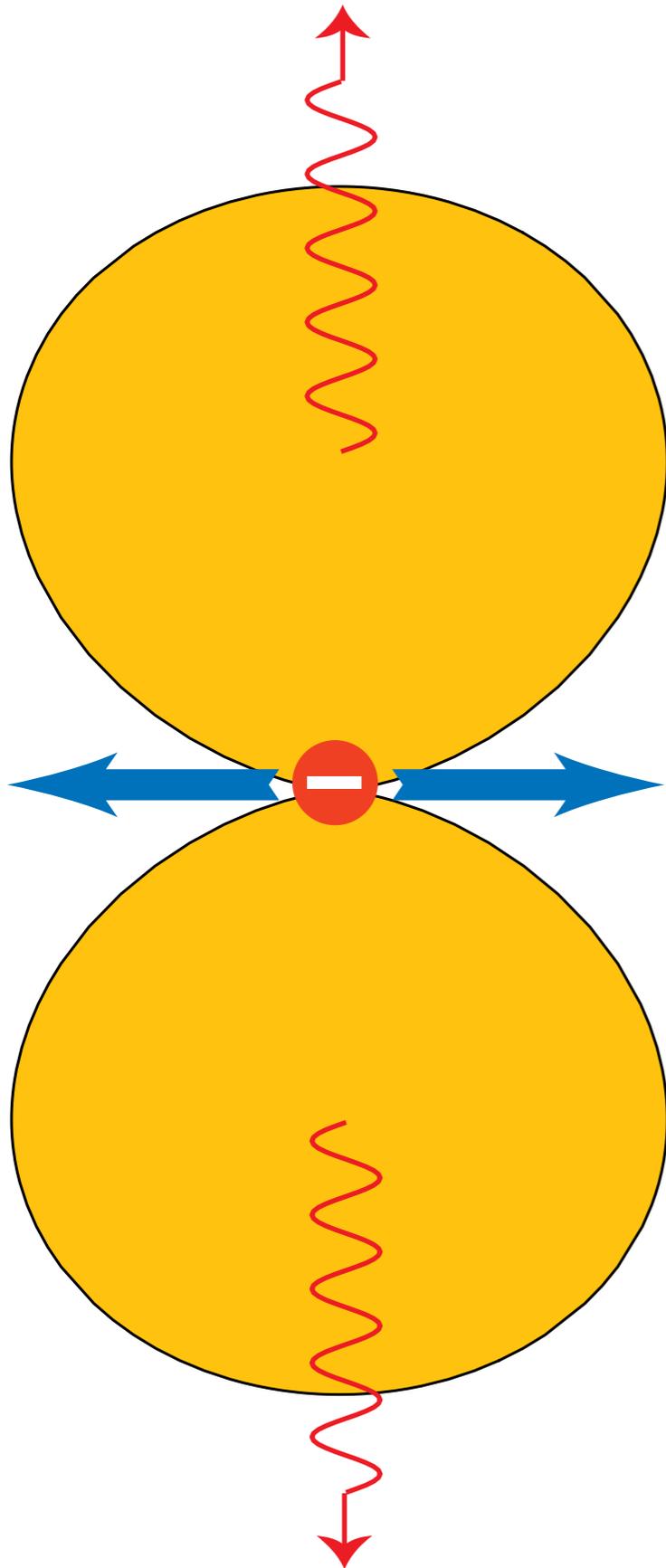


# Thomson Scattering

**electron**

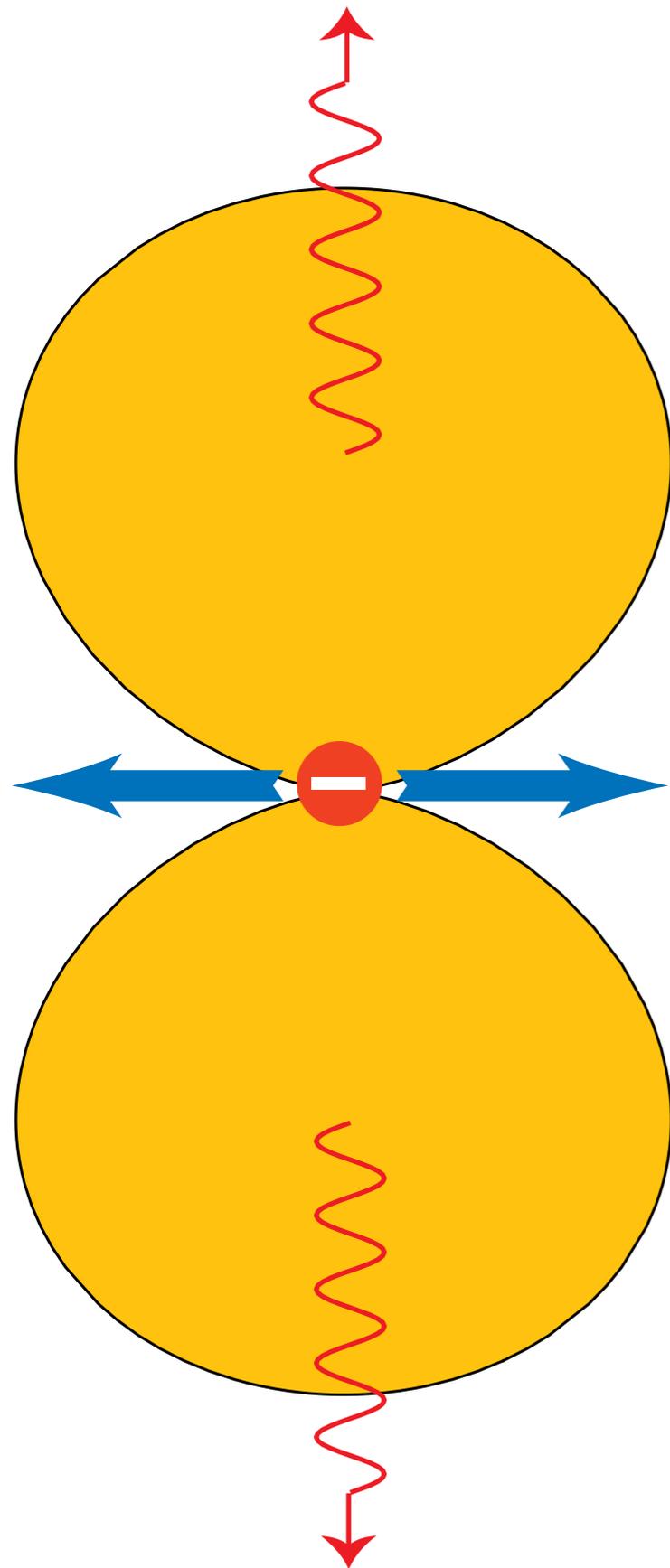
$$\sigma_{ele} = 10^{-28} \text{ m}^2$$

scattering x-section



$$\mathbf{E} \sin(\omega t - \mathbf{k} \cdot \mathbf{x})$$

# Thomson Scattering



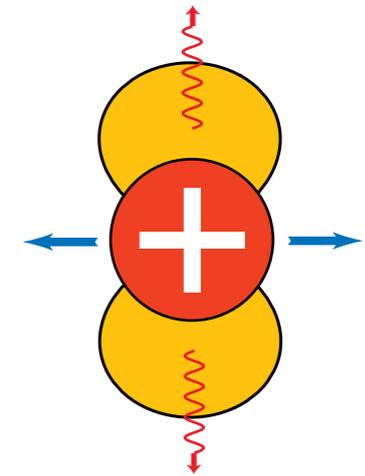
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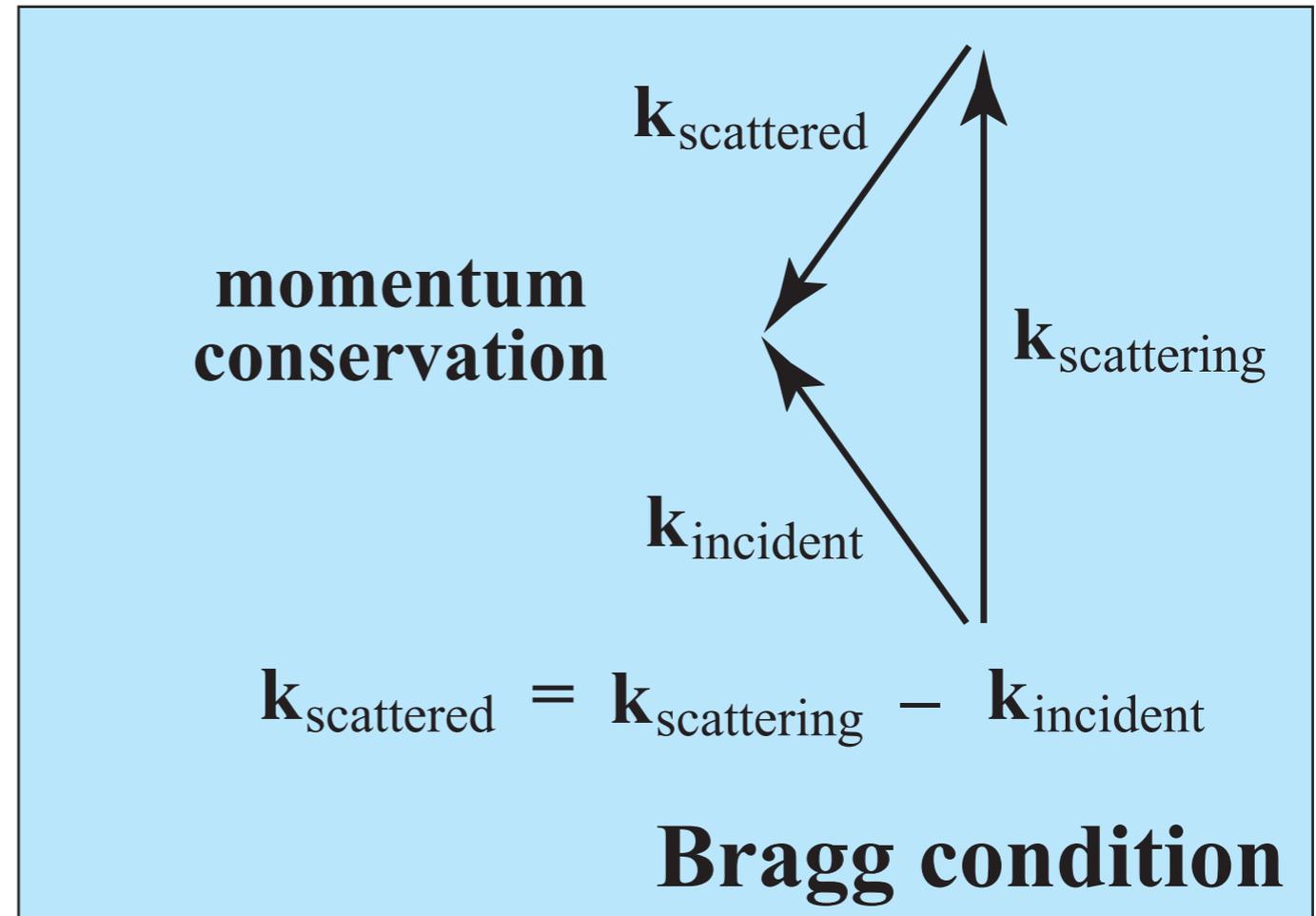
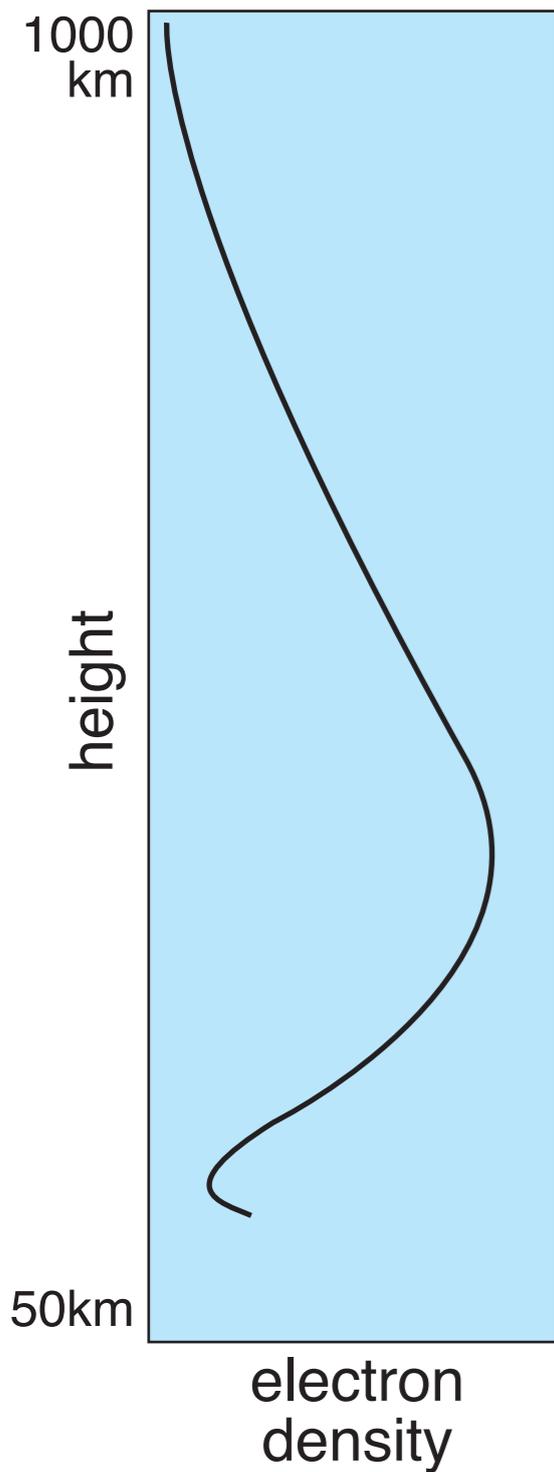
**ion**



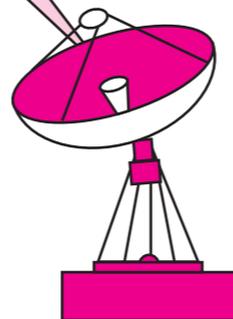
$$\frac{\sigma_{ion}}{\sigma_{ele}} = \left( \frac{m_{ele}}{m_{ion}} \right)^2 \approx 10^{-6} - 10^{-8}$$

# Incoherent Scattering from ionised media

arises from fluctuations of electron density

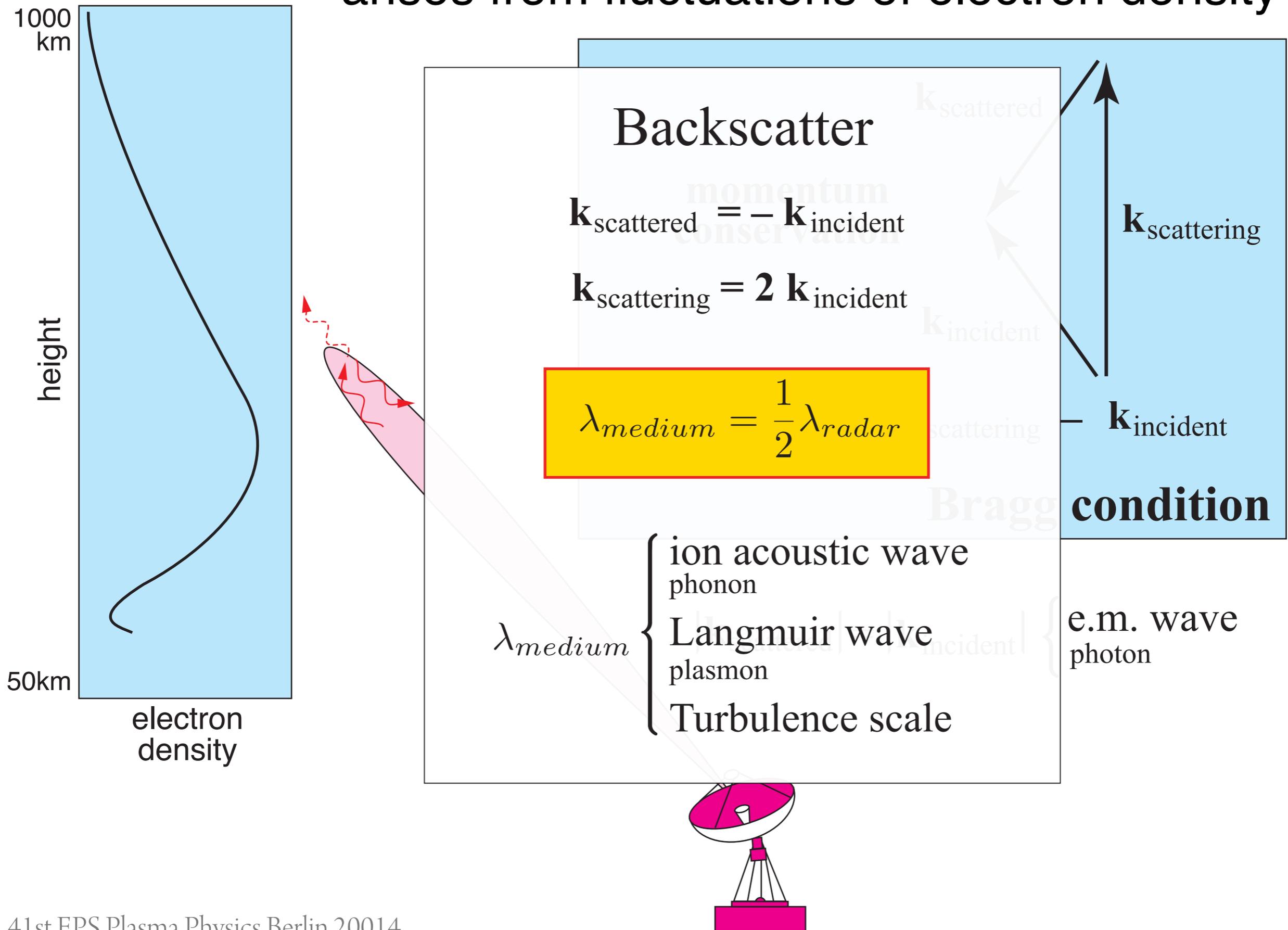


$$|\mathbf{k}_{\text{scattered}}| = |\mathbf{k}_{\text{incident}}| \begin{cases} \text{e.m. wave} \\ \text{photon} \end{cases}$$

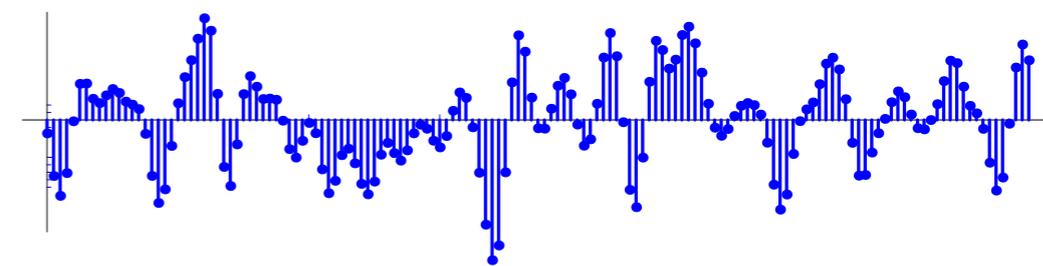
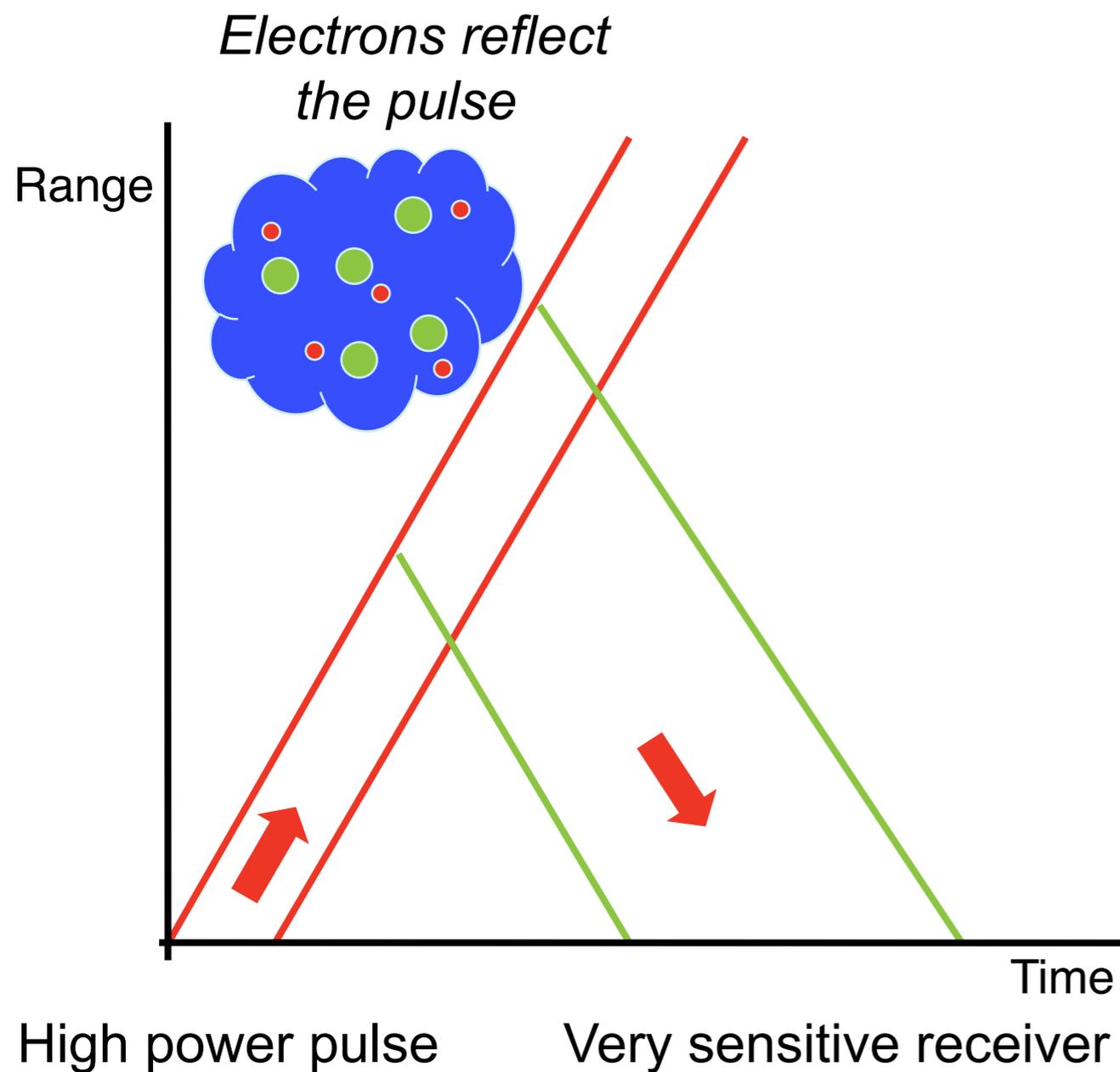


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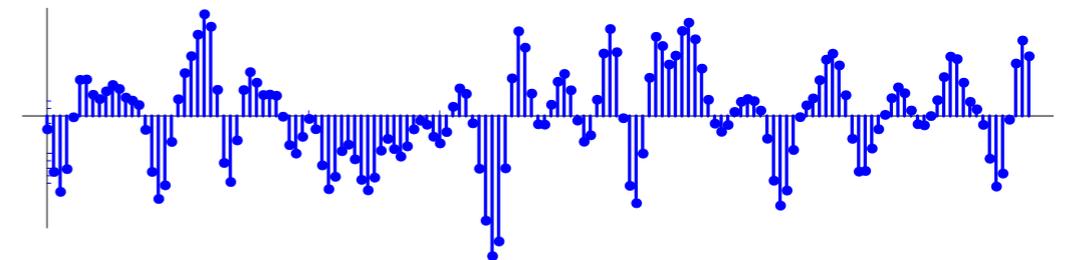
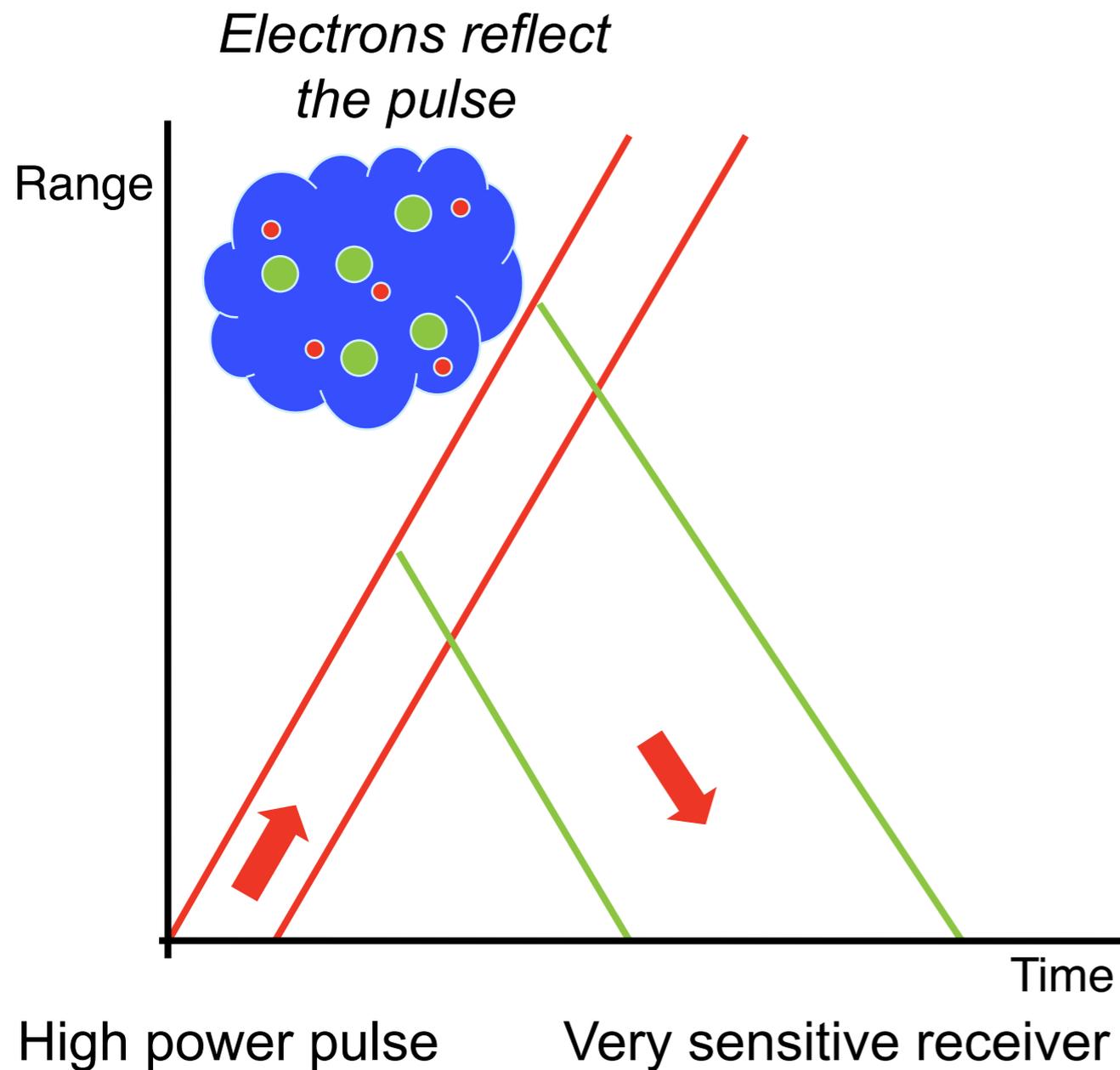
# How does it work?



produces a **stochastic** signal much smaller than the noise

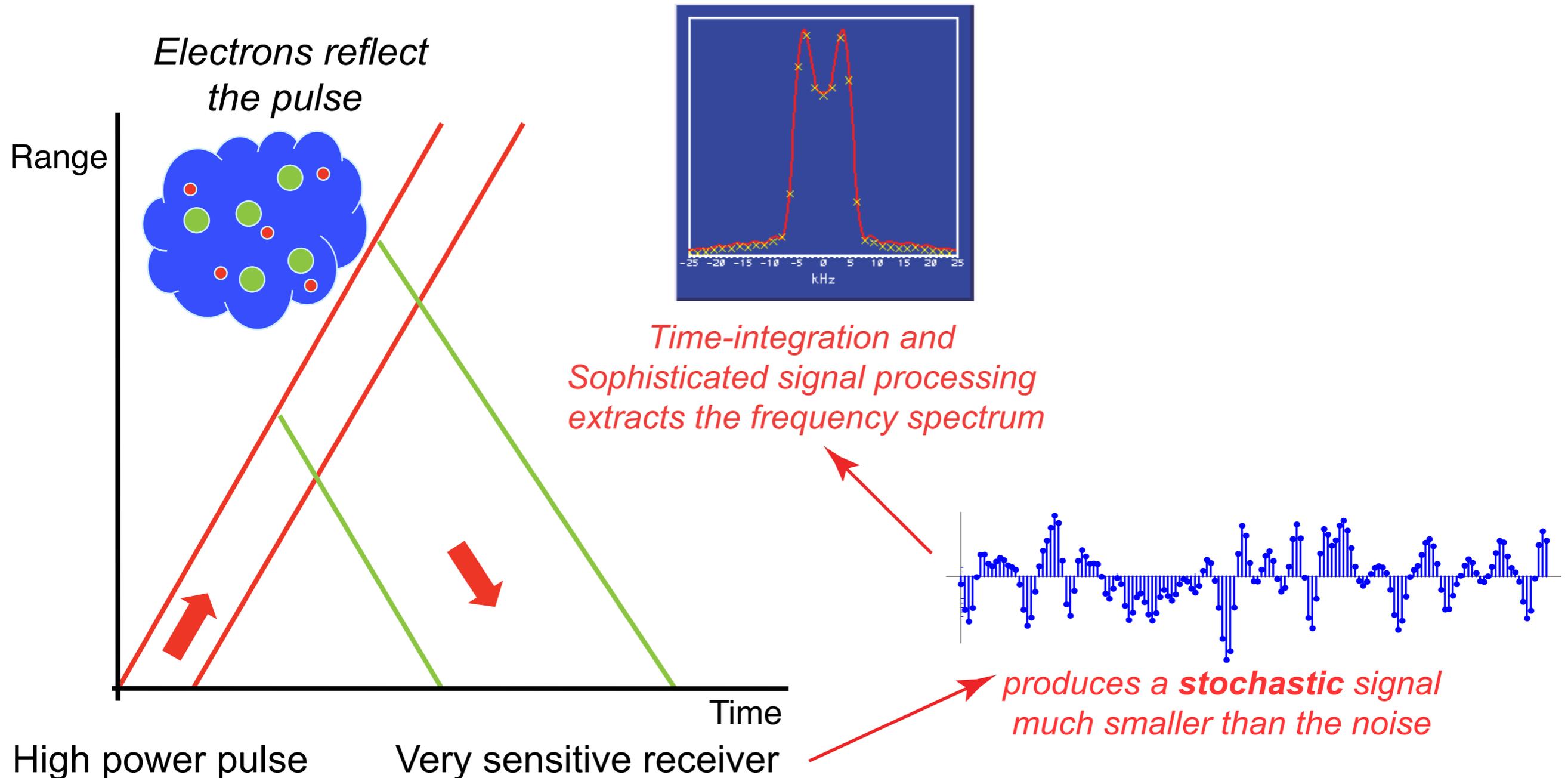
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Typical: 1 Mega Watt transmitted ( $10^6$  W)  
1 femto Watt received ( $10^{-15}$  W)



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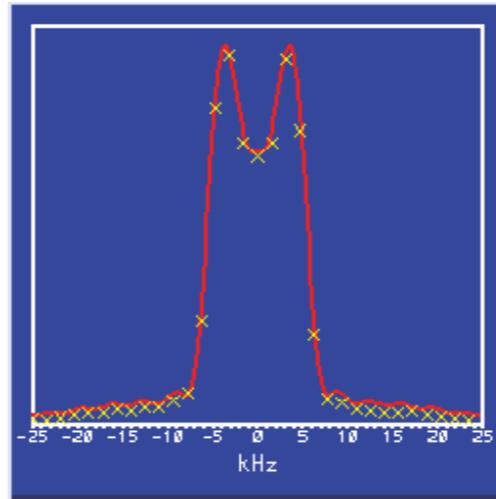
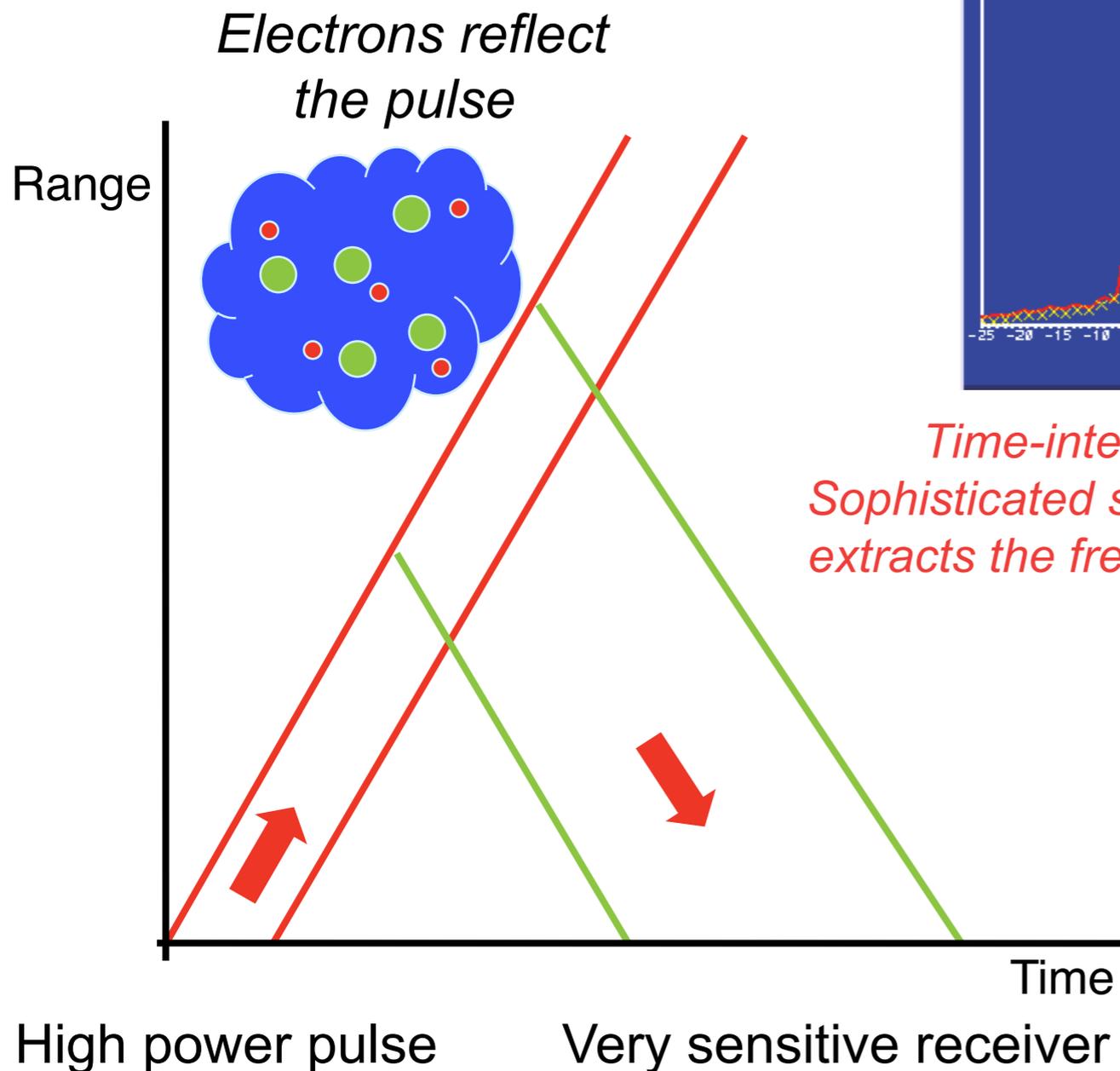
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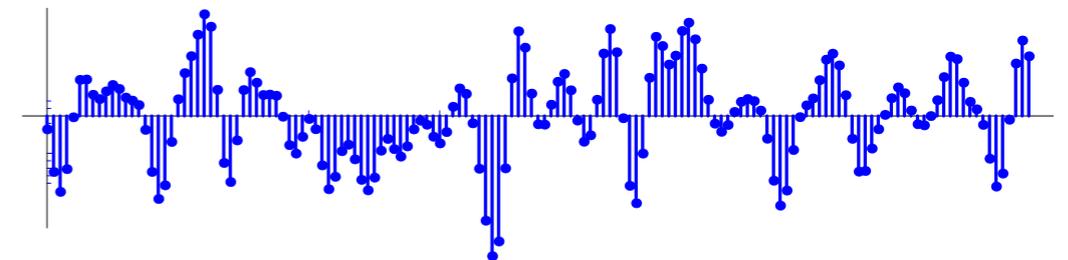
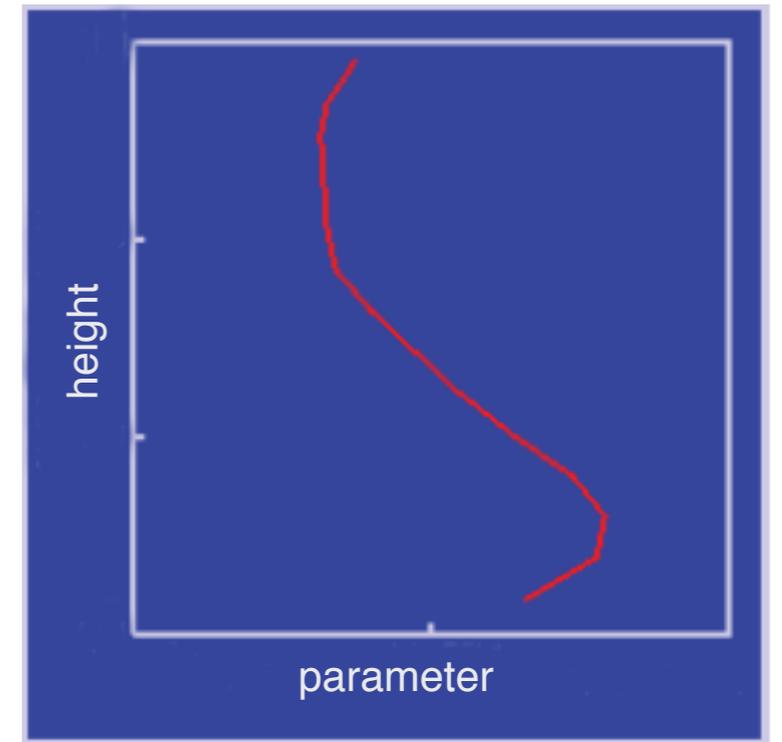
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*Least squares fitting produces ionospheric plasma parameters*

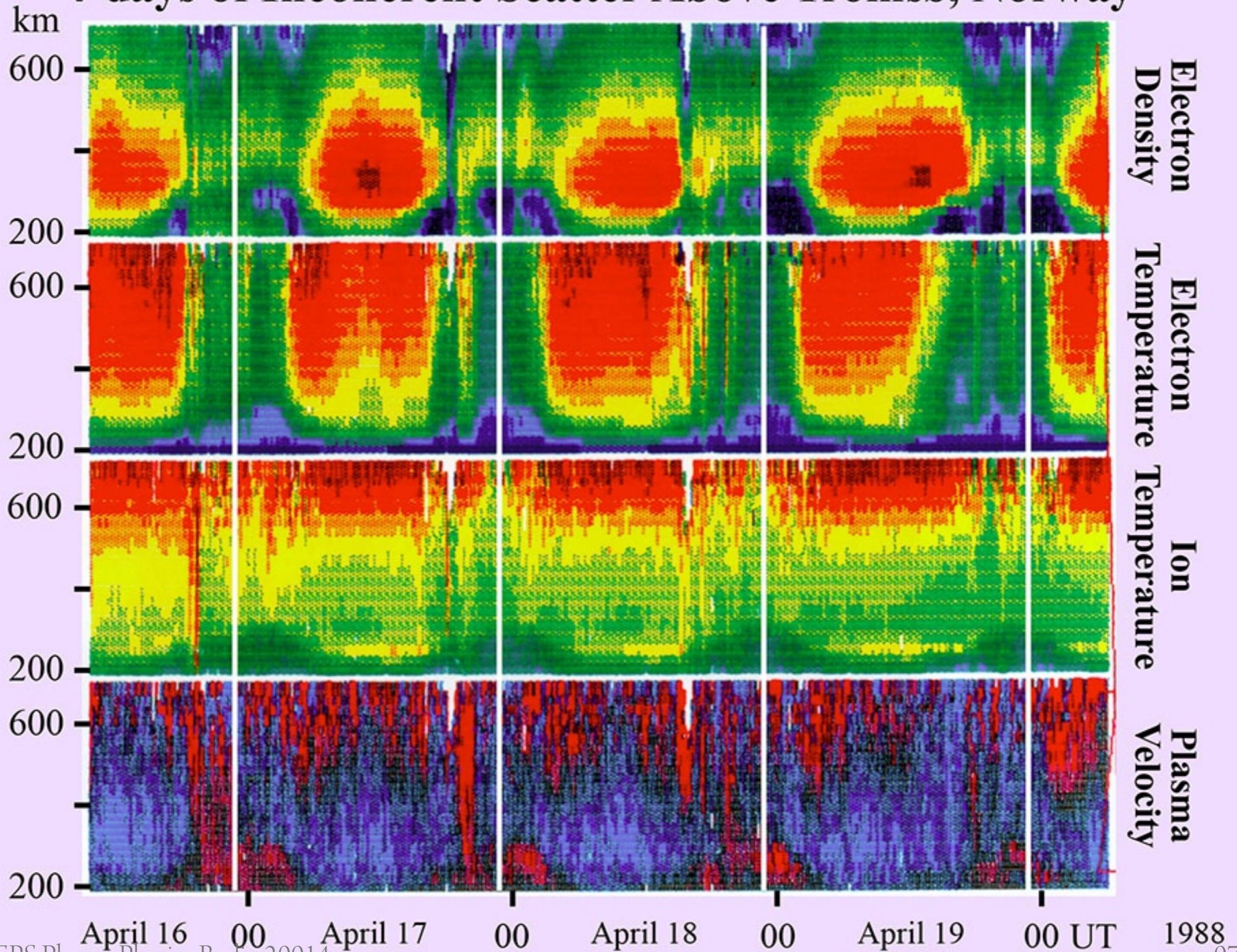


*Time-integration and Sophisticated signal processing extracts the frequency spectrum*

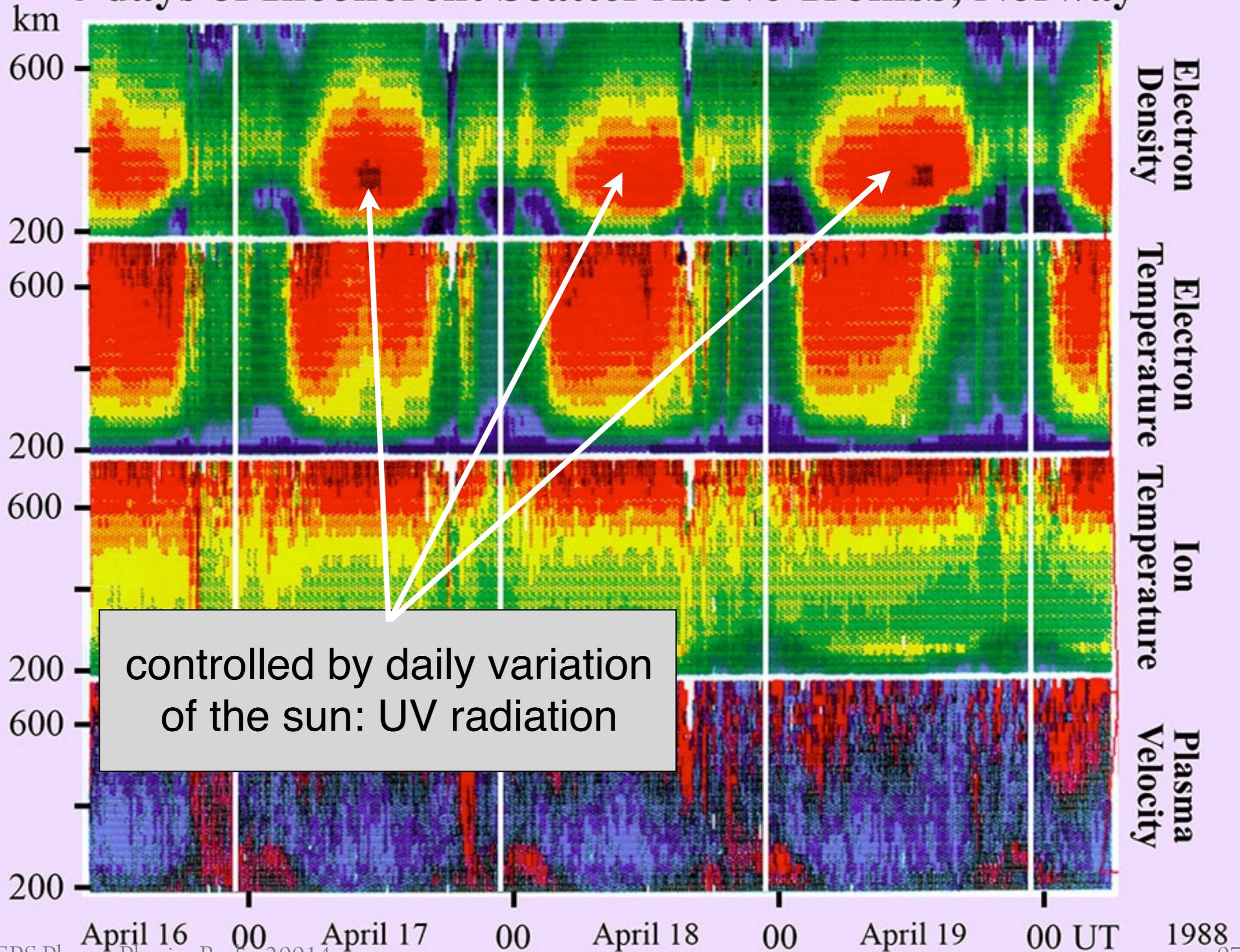


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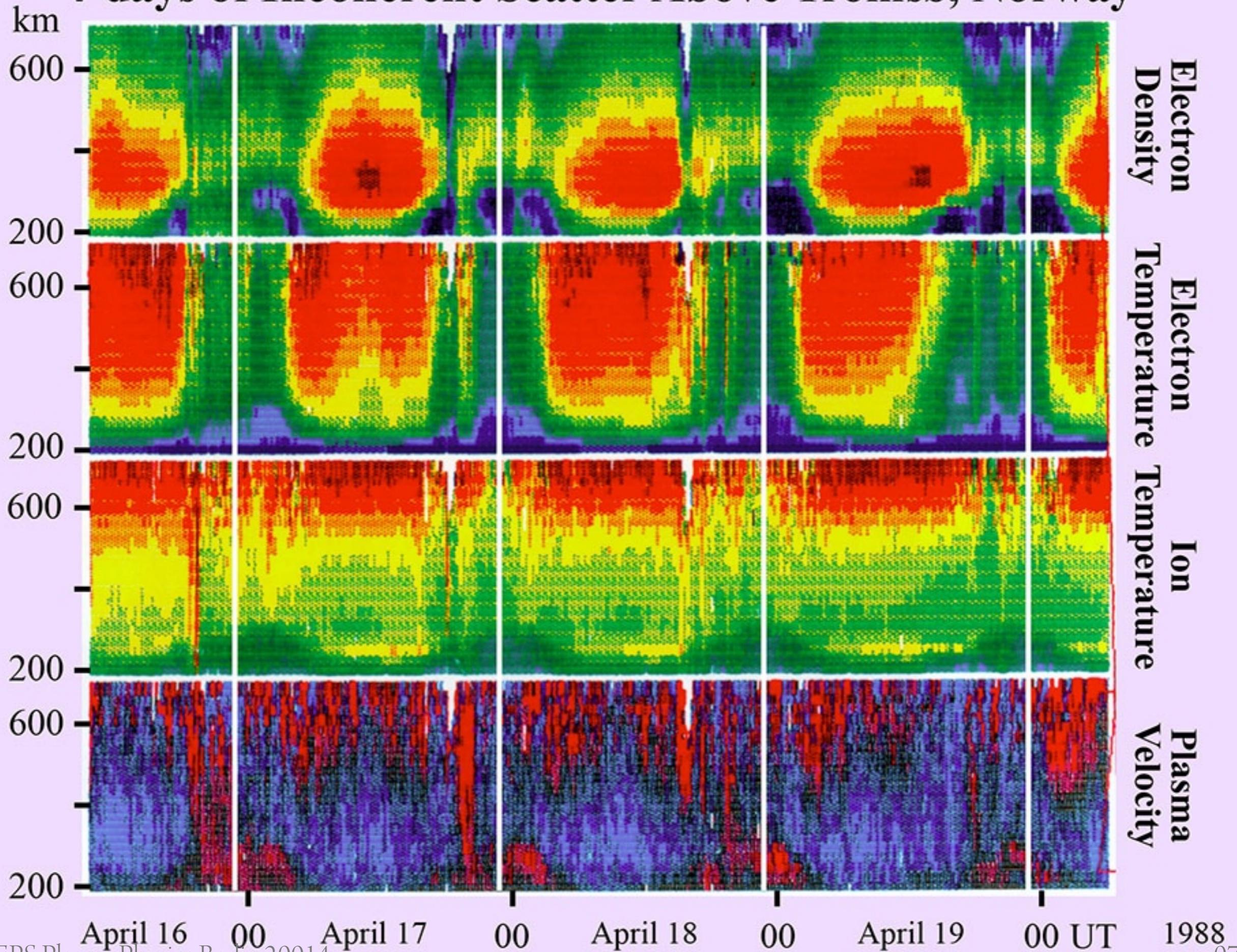
# 4-days of Incoherent Scatter Above Tromsø, Norway



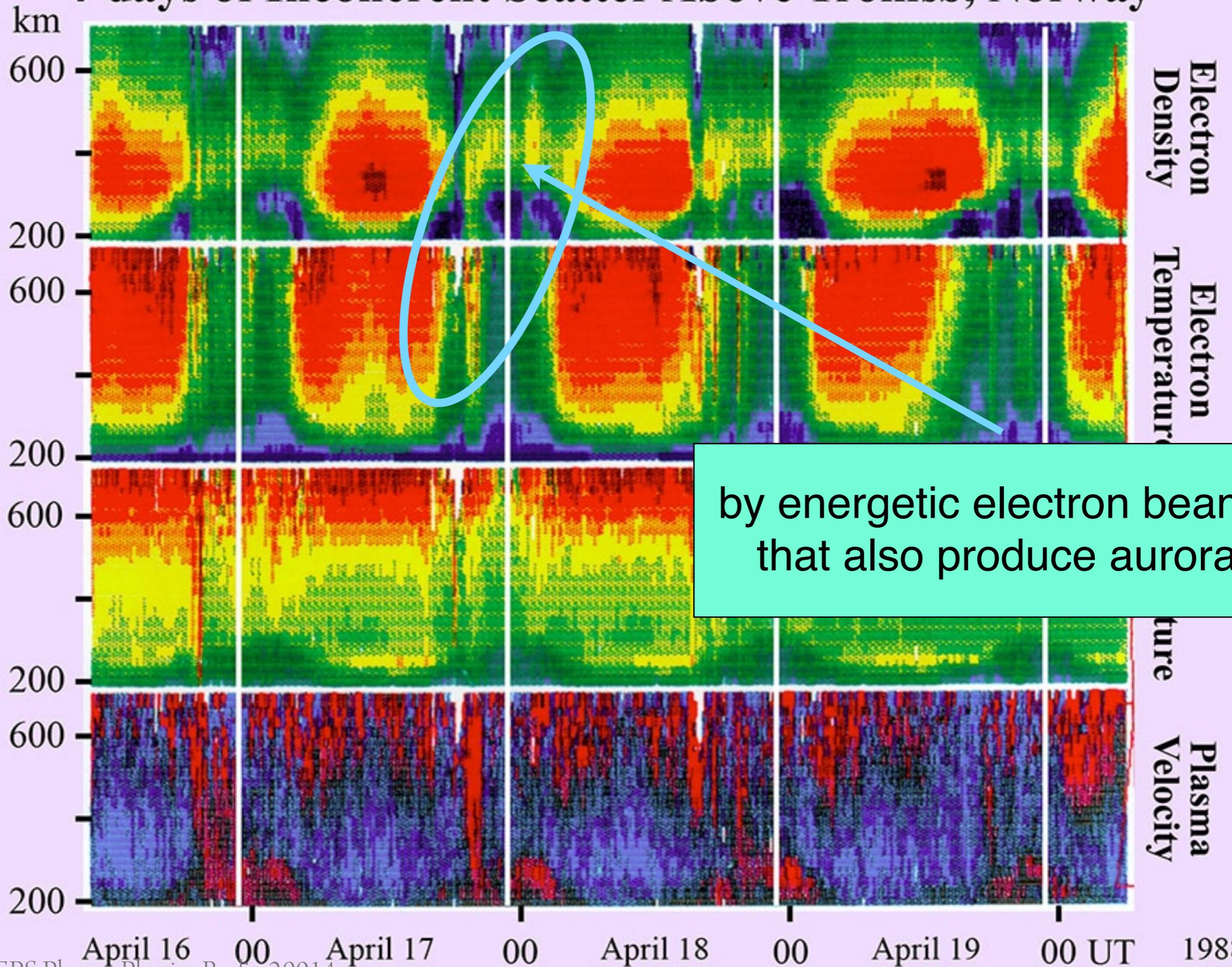
# 4-days of Incoherent Scatter Above Tromsø, Norway



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# The Incoherent Scattering Spectrum

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

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## dielectric function

$$\epsilon(\mathbf{k}, \omega) = 1 + \sum_{\alpha} \chi_{\alpha}(\mathbf{k}, \omega)$$

## electric susceptibility

$$\chi_{\alpha}(\mathbf{k}, \omega) = \frac{\omega_{pe}^2}{k^2} \int_{\mathcal{L}} \frac{\mathbf{k} \cdot \partial_{\mathbf{v}} f_{\alpha}(\mathbf{v})}{\omega - \mathbf{k} \cdot \mathbf{v}} d\mathbf{v}$$

## velocity distribution function

$$f_{e,i}(\mathbf{v}; T_e, T_i, m_i, \nu_{in})$$

## Charge densities

$$N_e = \sum_i N_i$$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

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Each charge in the plasma behaves as in vacuum but it polarises the rest of the plasma resulting in neutralising clouds around each charge:

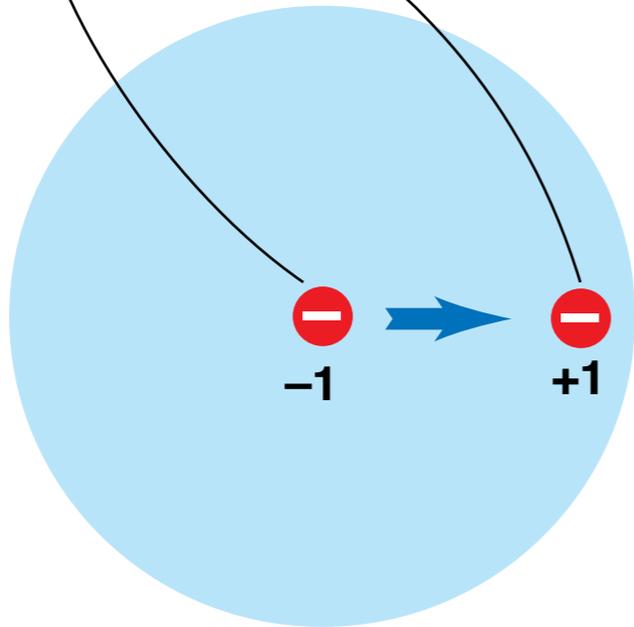
the charge and its cloud is a **dressed (quasi) particle**

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

# Plasma Line $S_{PL}(\mathbf{k}, \omega)$

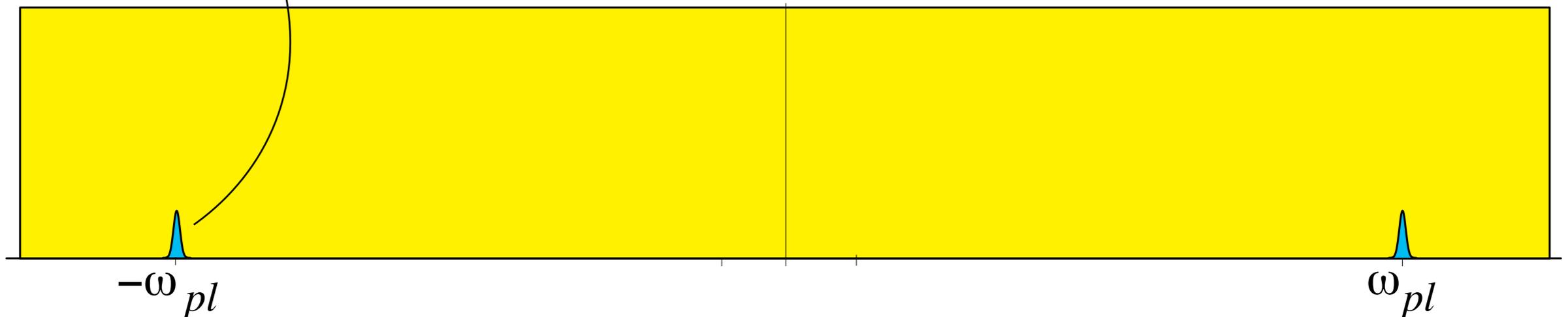
$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

test  
electron  
with cloud



$$\omega_{pl}(k) \approx \omega_{pe} (1 + 3 \lambda_D^2 k^2)$$

$$\epsilon(\mathbf{k}, \omega) = 0$$

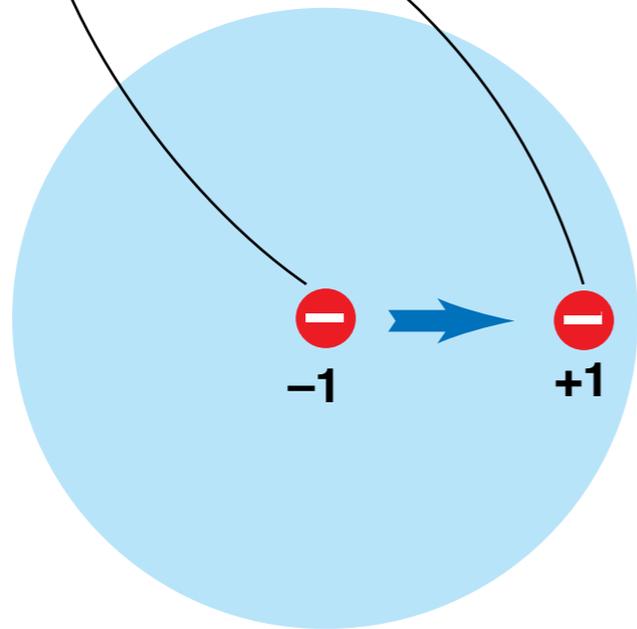


# Plasma Line $S_{PL}(\mathbf{k}, \omega)$

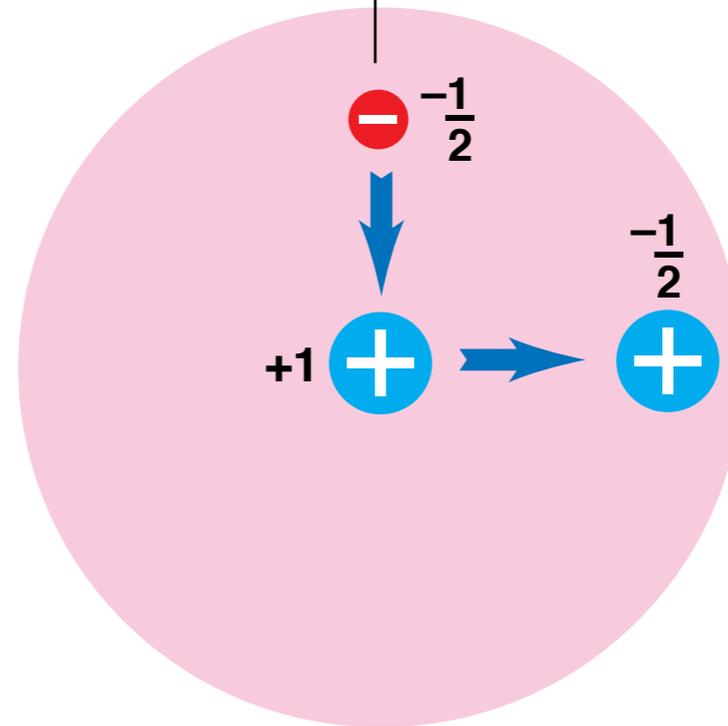
# Ion Line $S_{IL}(\mathbf{k}, \omega)$

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test electron with cloud



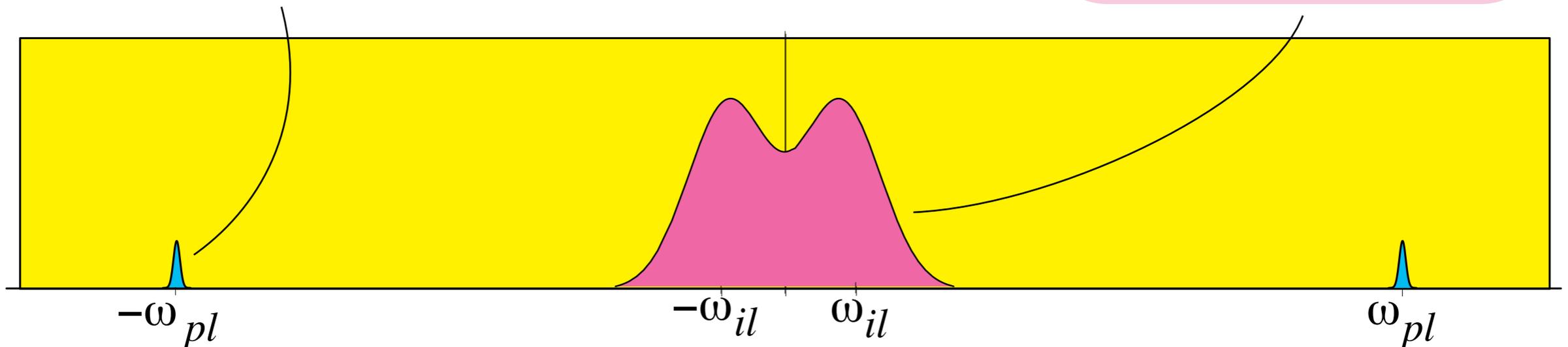
test ion with cloud



$$\omega_{pl}(k) \approx \omega_{pe} (1 + 3 \lambda_D^2 k^2)$$

$$\epsilon(\mathbf{k}, \omega) = 0$$

$$\omega_{ia}(k) \approx k \sqrt{\frac{T_e + 3 T_i}{m_i}}$$



**no collective interactions: no clouds:  $\chi_e(\mathbf{k}, \omega) = 0$**

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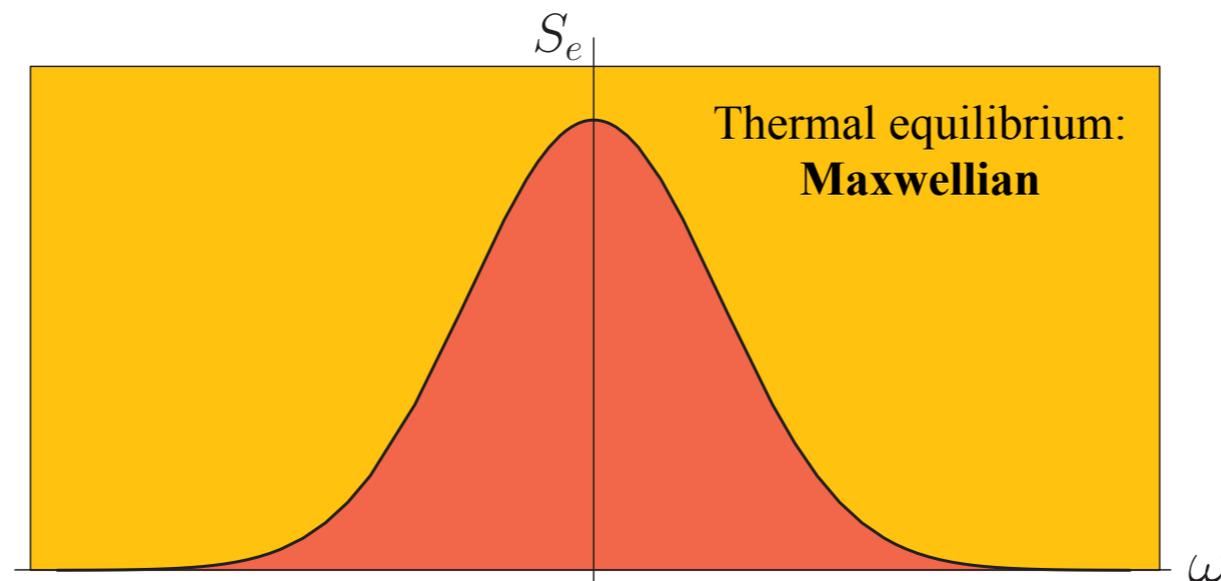
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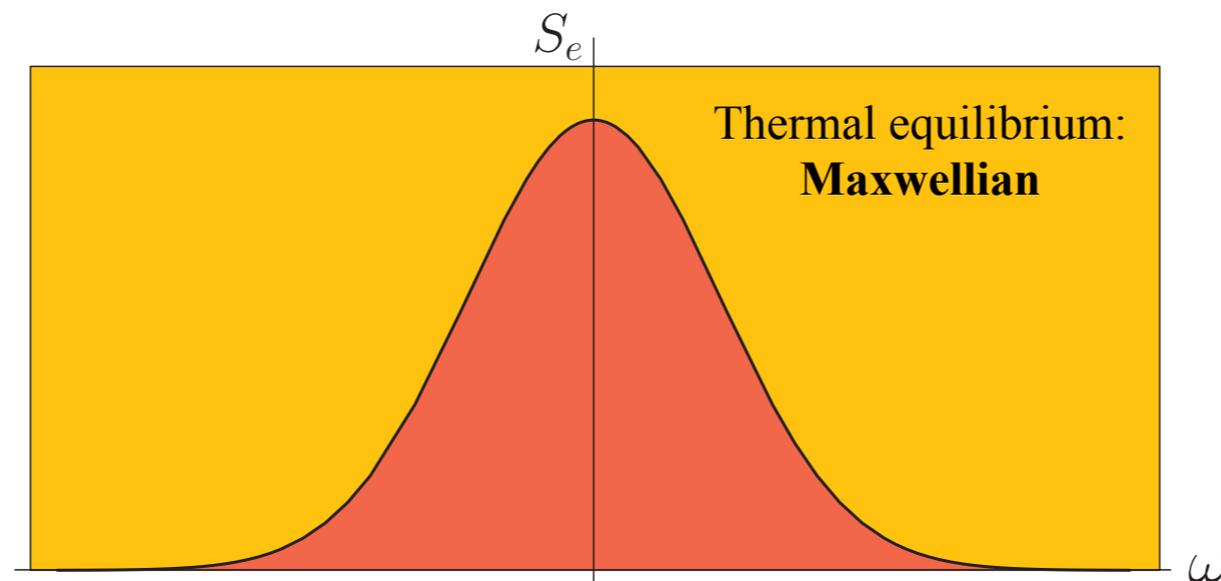
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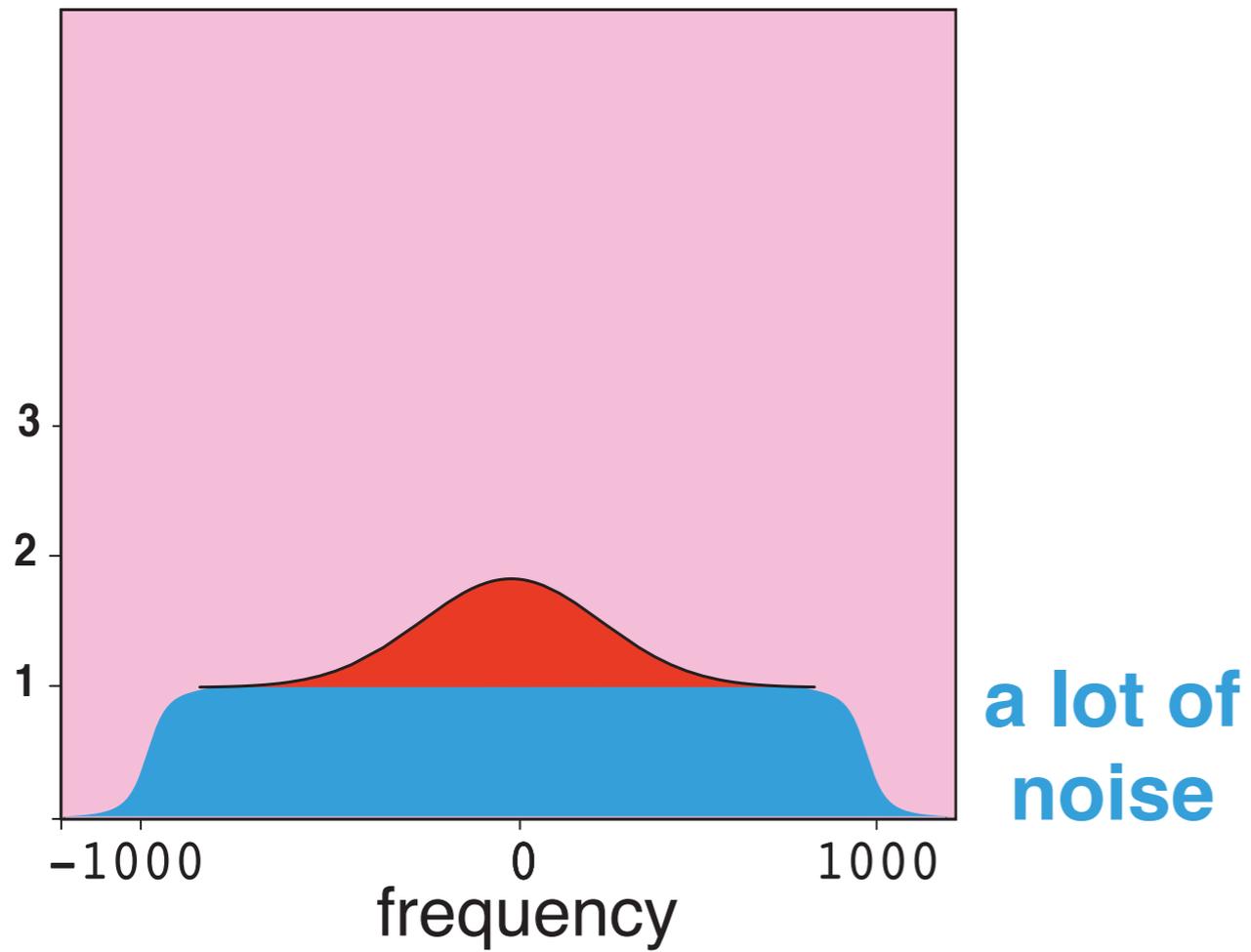


The Arecibo Observatory was designed and built under this premise.

**SNR = 0.005**

**■ signal**

**■ noise**



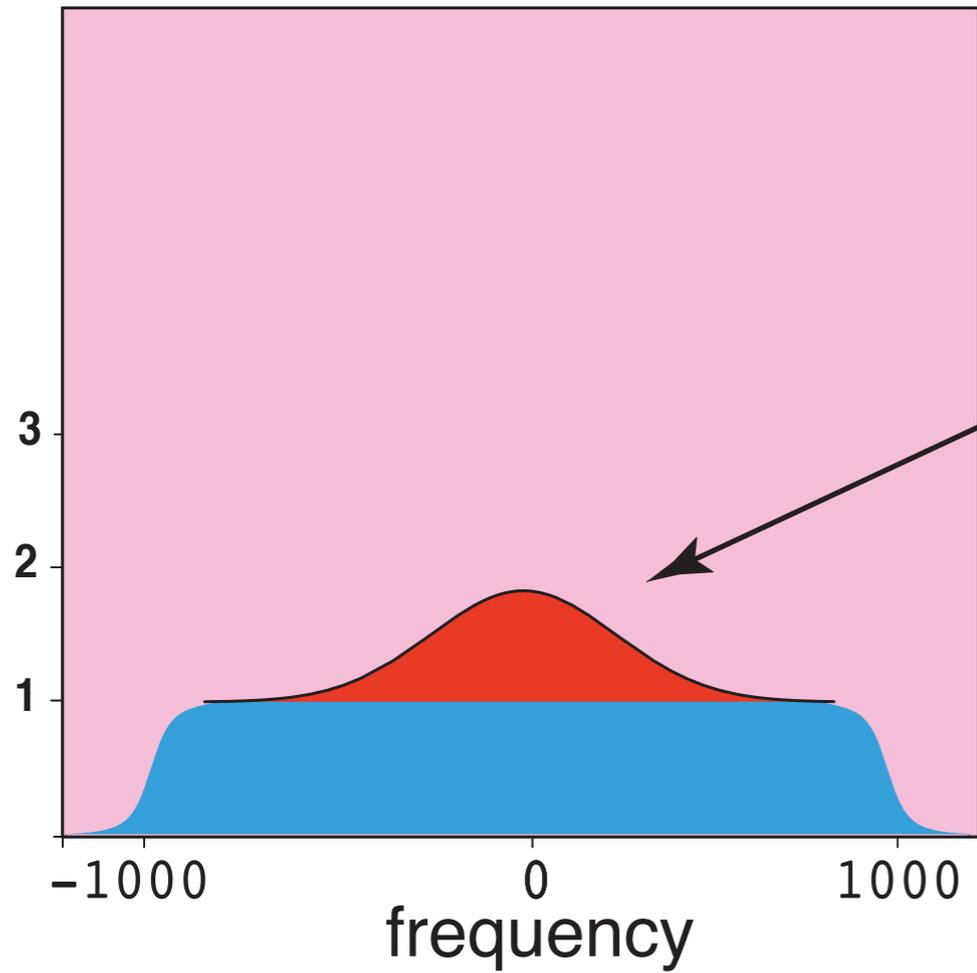
**300 metre dish  
Arecibo**

**SNR = 0.005**

**■ signal**

**■ noise**

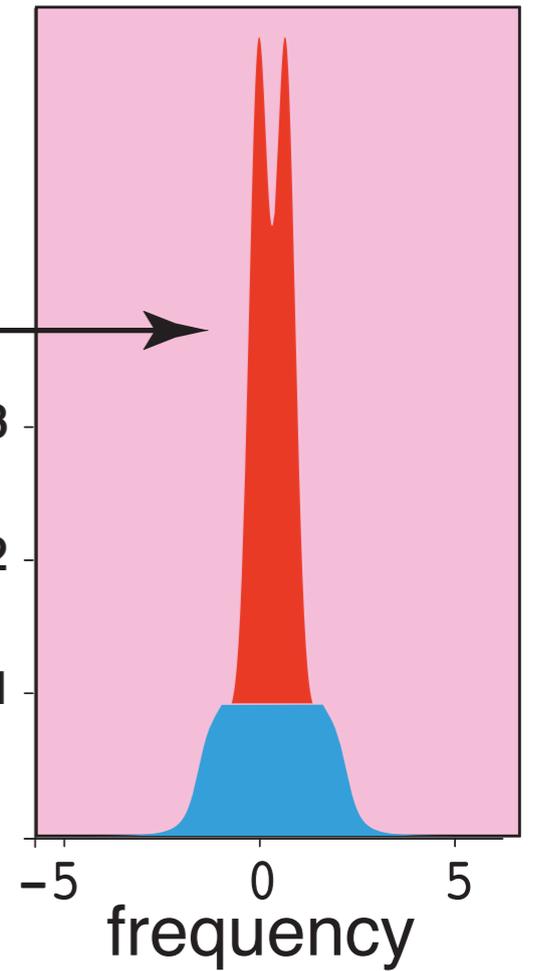
**SNR = 1**



**the same  
signal power**

**a lot of  
noise**

**little  
noise**



**300 metre dish  
Arecibo**

**antenna area ratio: 100**

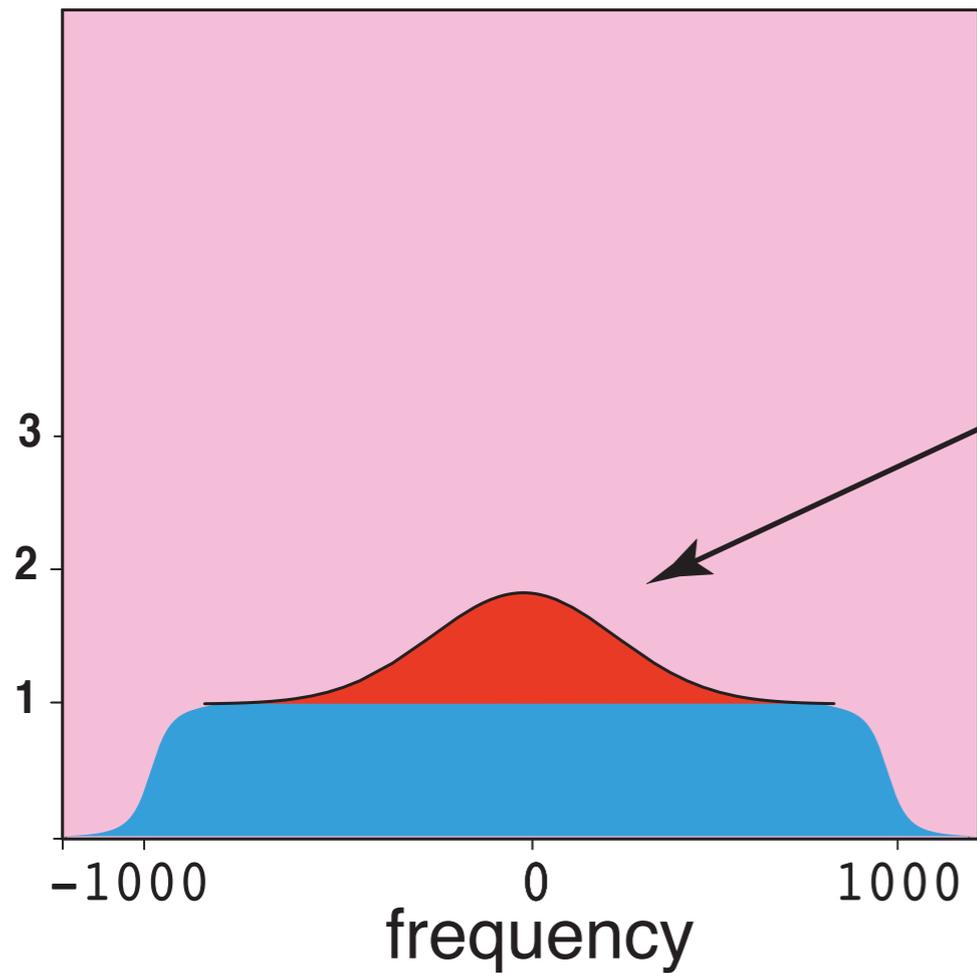
**30 metre dish  
EISCAT**

**SNR = 0.005**

**■ signal**

**■ noise**

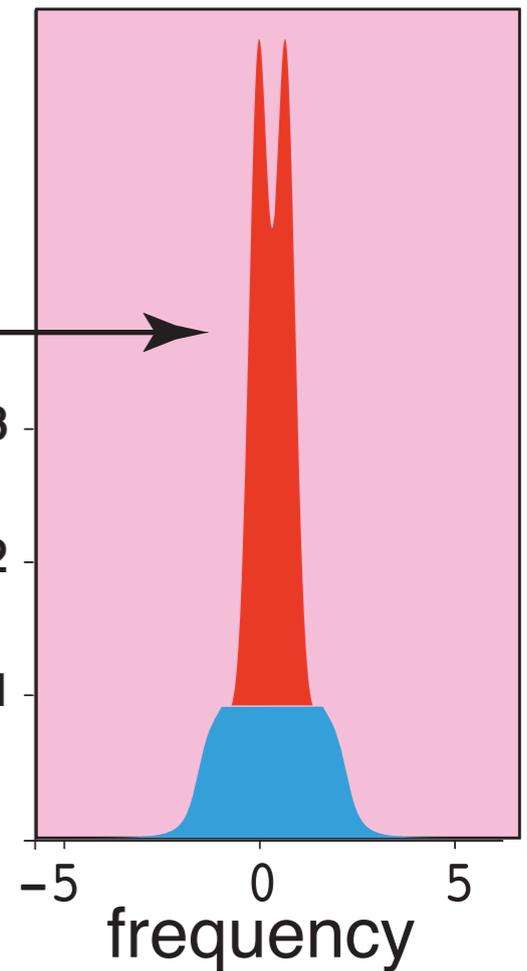
**SNR = 1**



**the same  
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**a lot of  
noise**

**little  
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**300 metre dish  
Arecibo**

**antenna area ratio: 100**

**30 metre dish  
EISCAT**

**extraordinary  
radio telescope**



**Arecibo Observatory  
Puerto Rico**

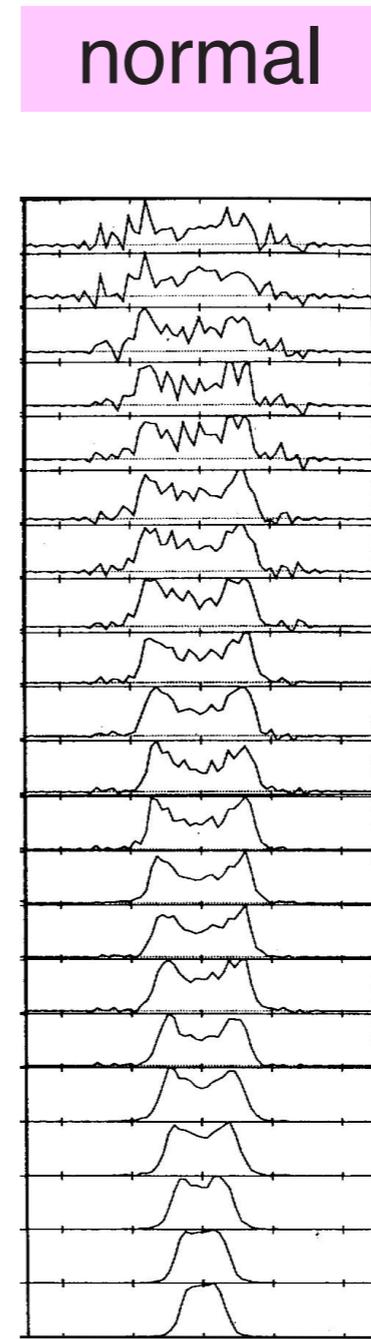
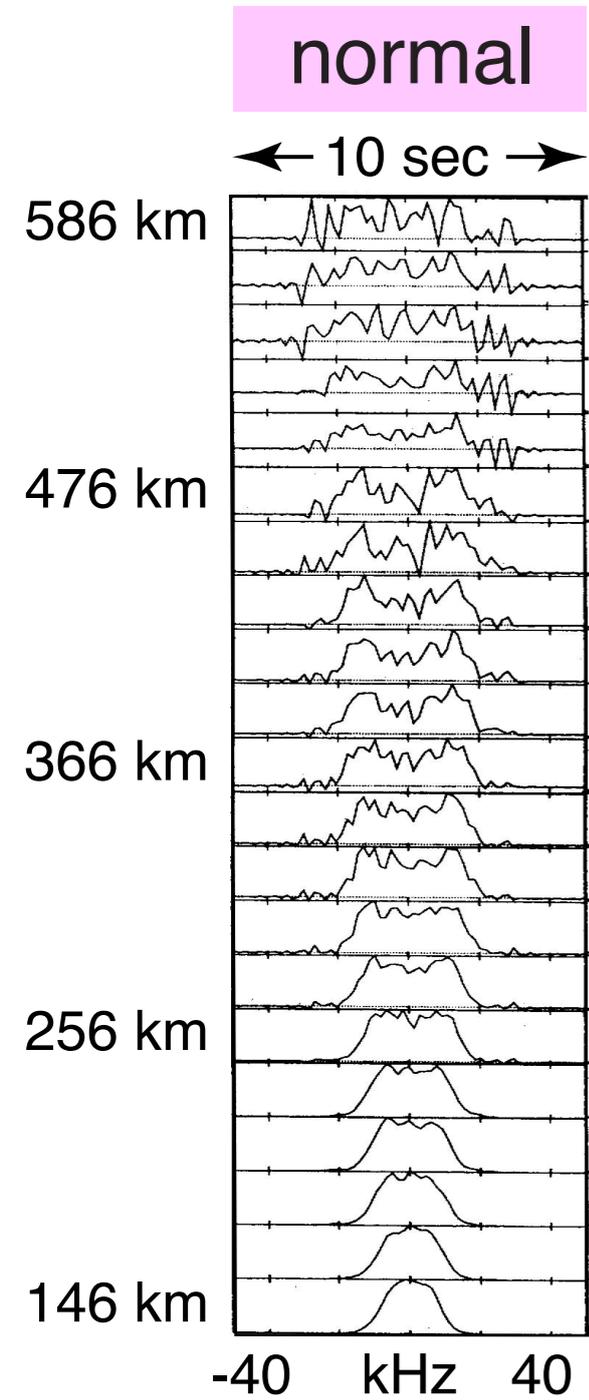
**cost ~150 M USD  
in today's \$**

**300m**

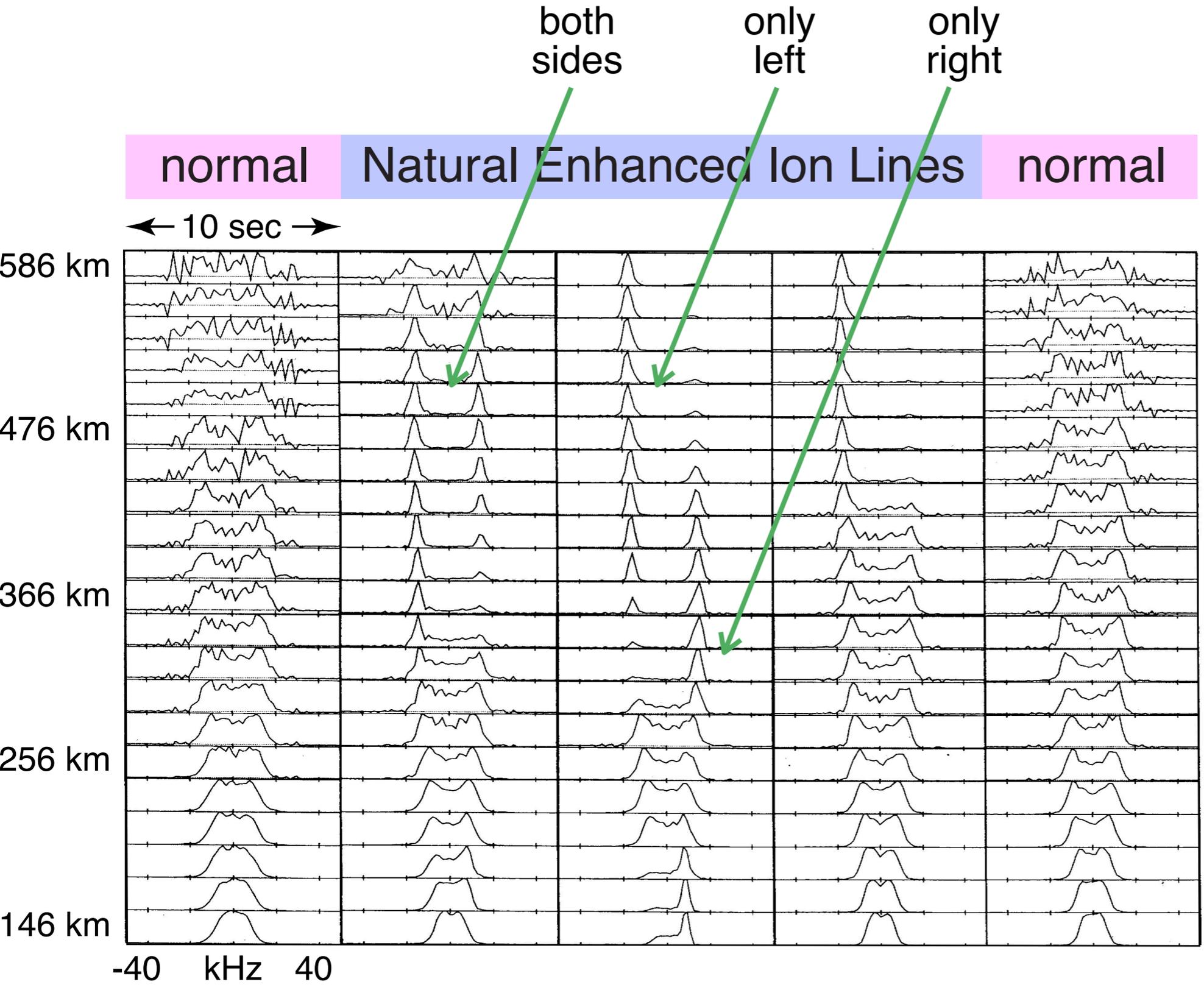
An aerial photograph of the Arecibo Observatory in Puerto Rico. The central feature is a massive, circular radio telescope dish, which is a paraboloid of revolution. The dish is supported by a central tower and a complex network of cables. A pink double-headed arrow spans the diameter of the dish, with the text "300m" written in pink above it. The surrounding landscape is lush and green, with a road and some buildings visible at the base of the dish.

## 2. Natural Enhanced Ion Acoustic Lines, NEIAL

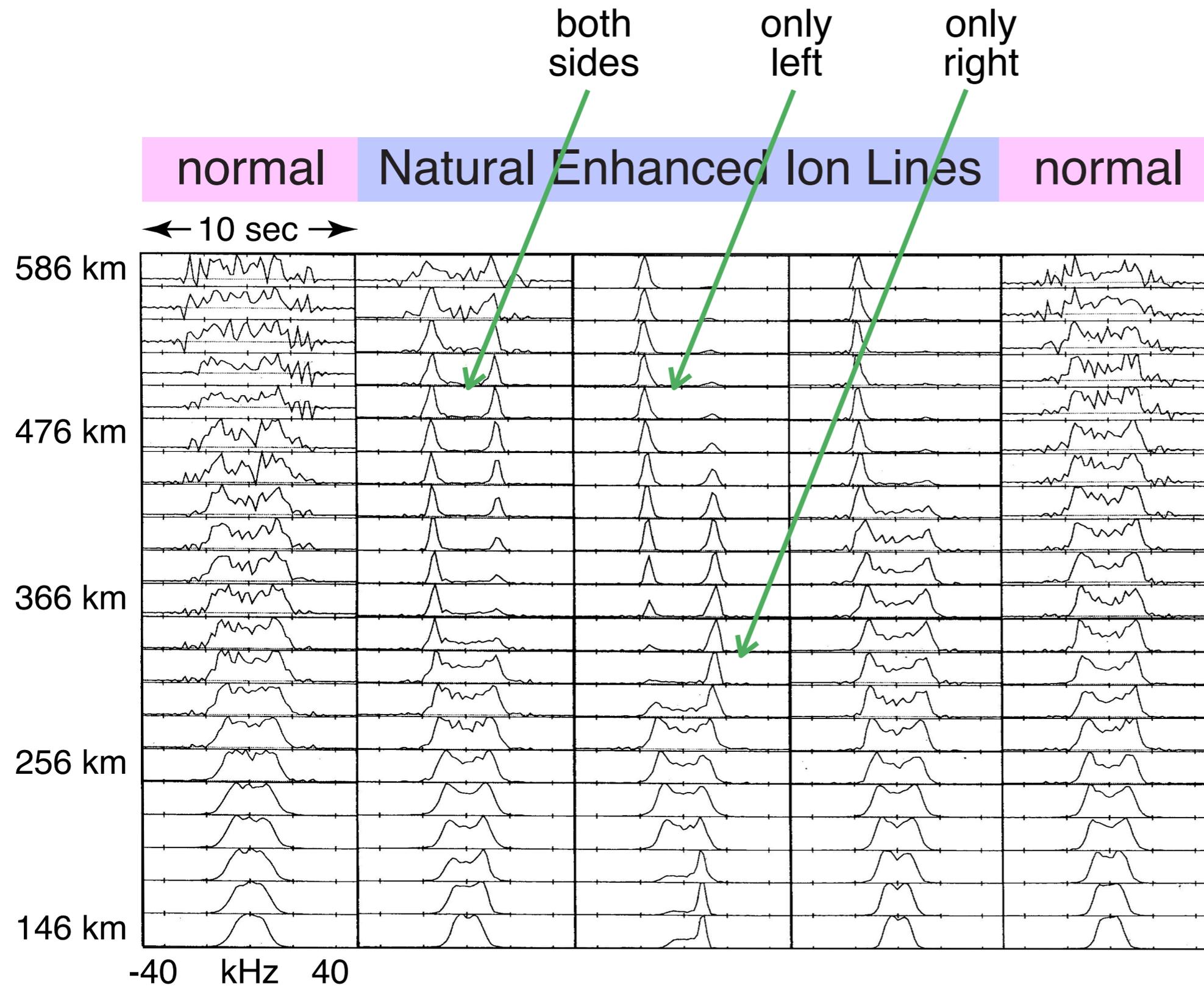
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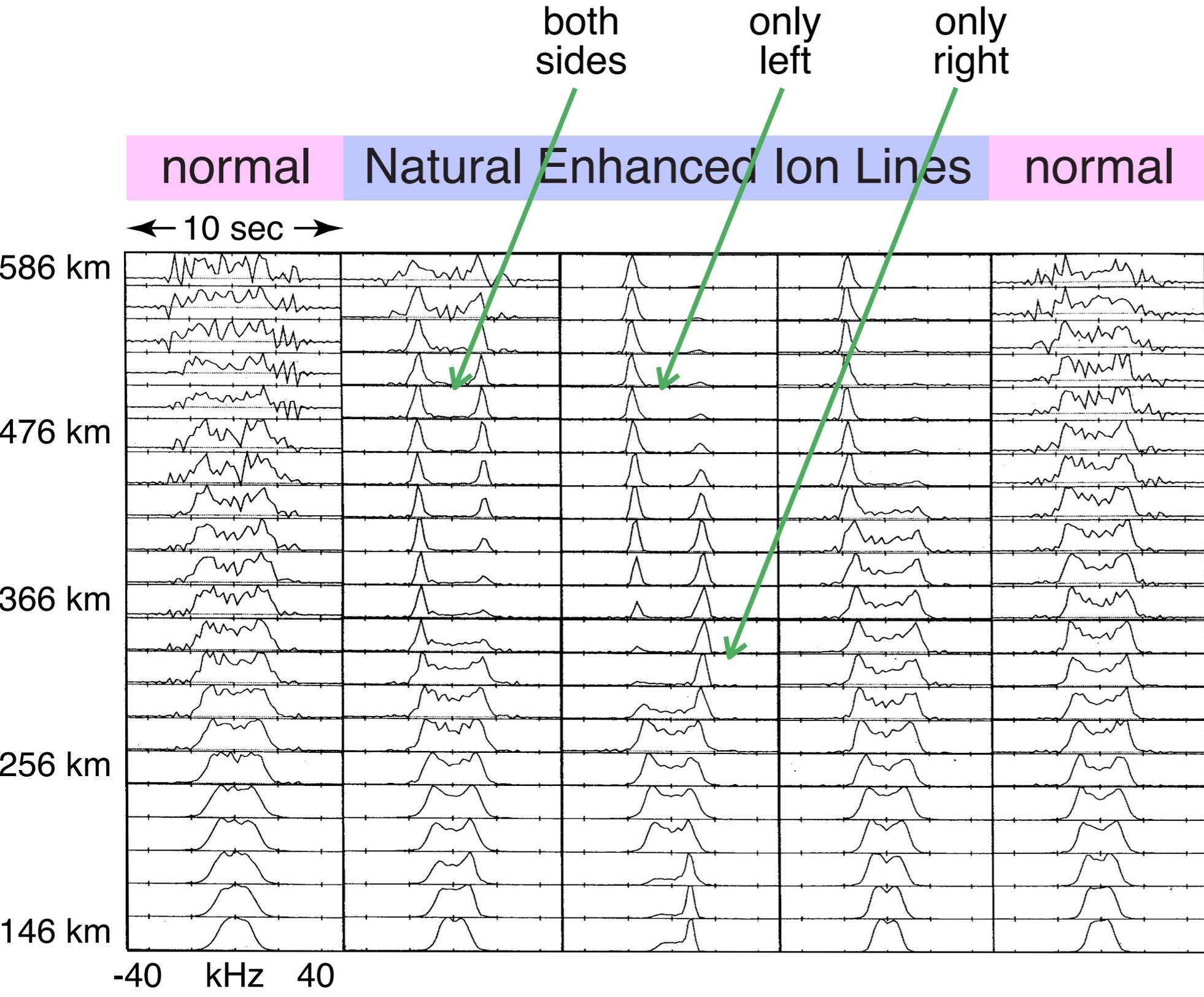


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- Infrequent, short lifetime  
100ms to  $\geq 1$  min

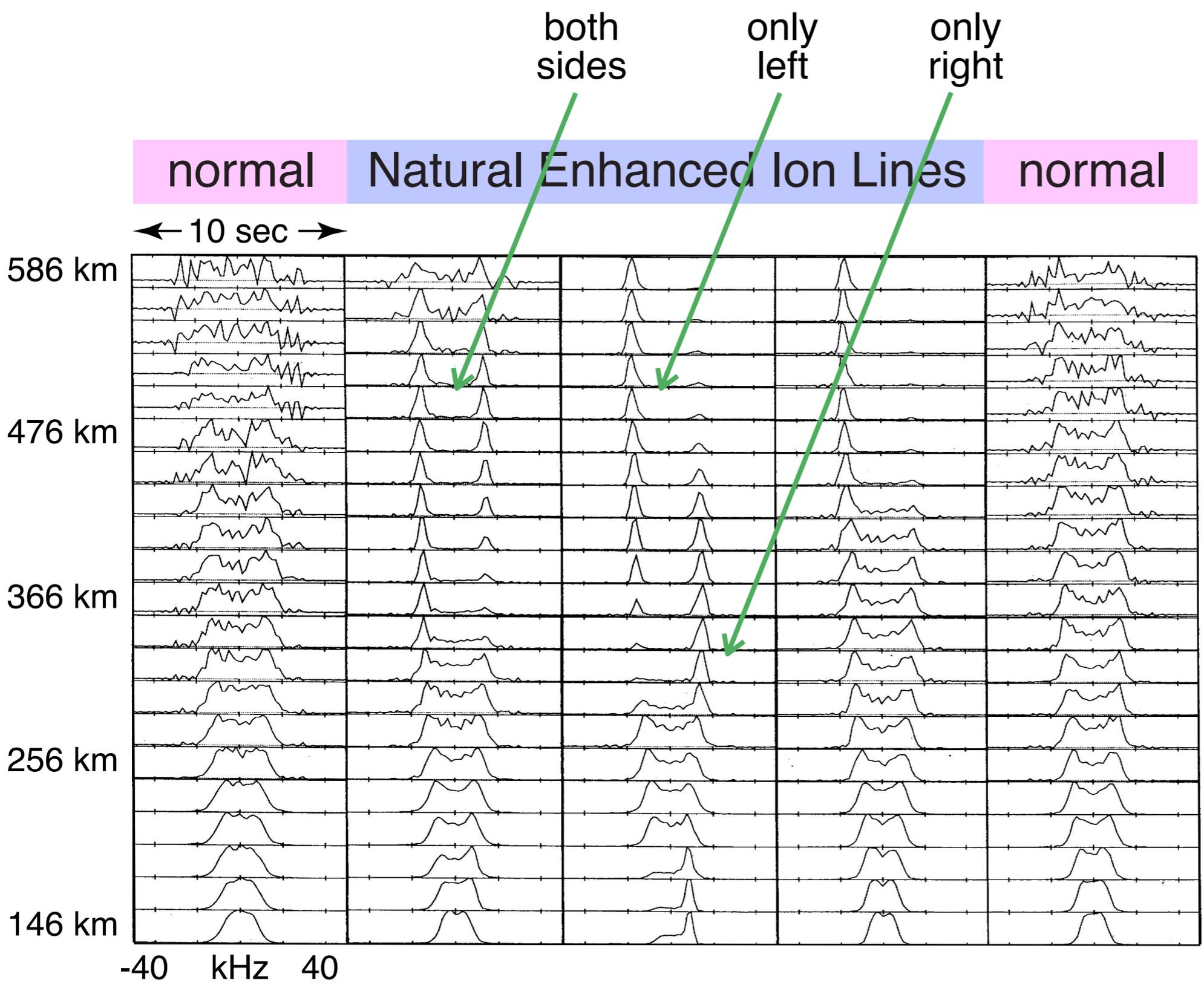
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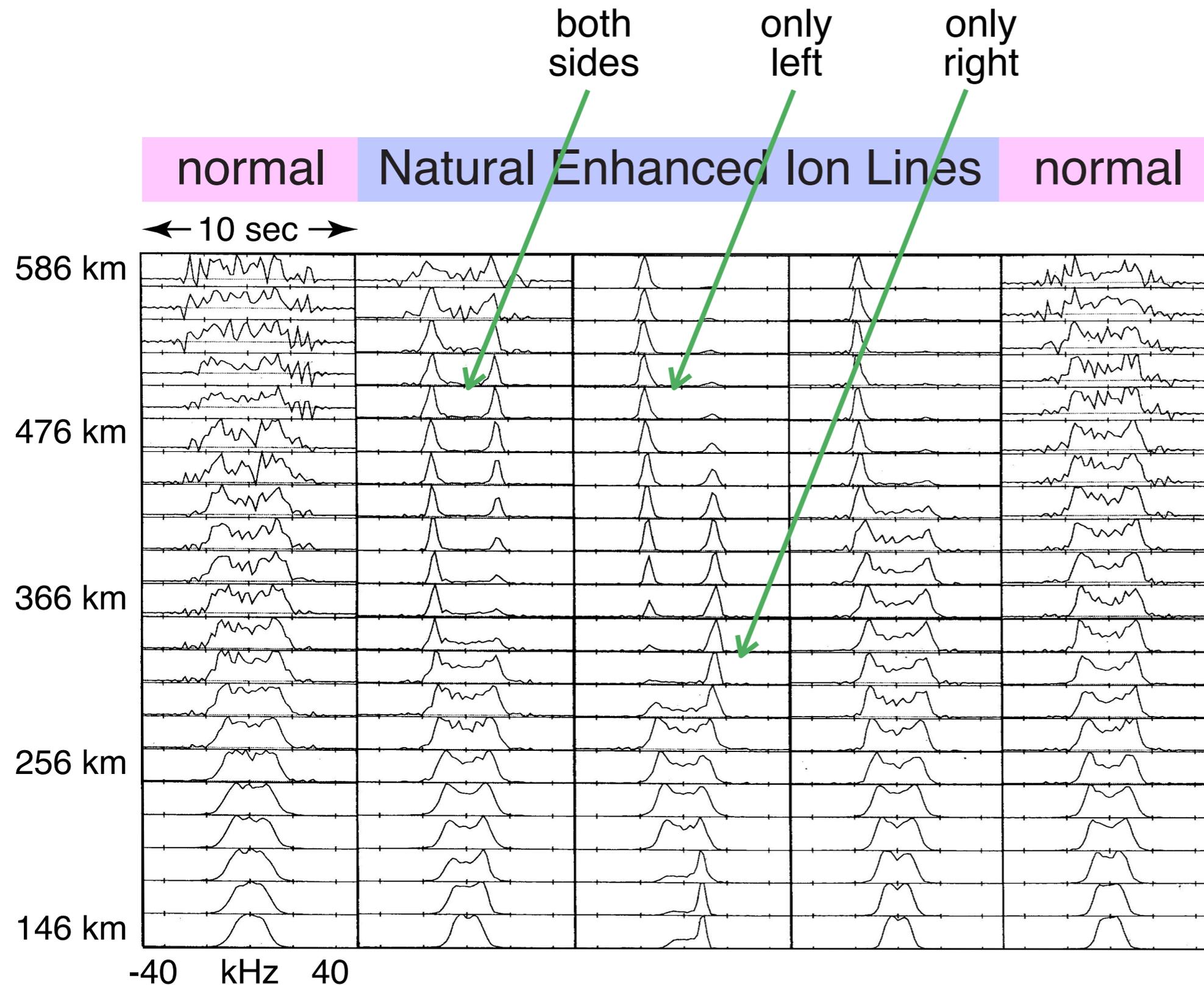
- Enhanced up to 50 dB

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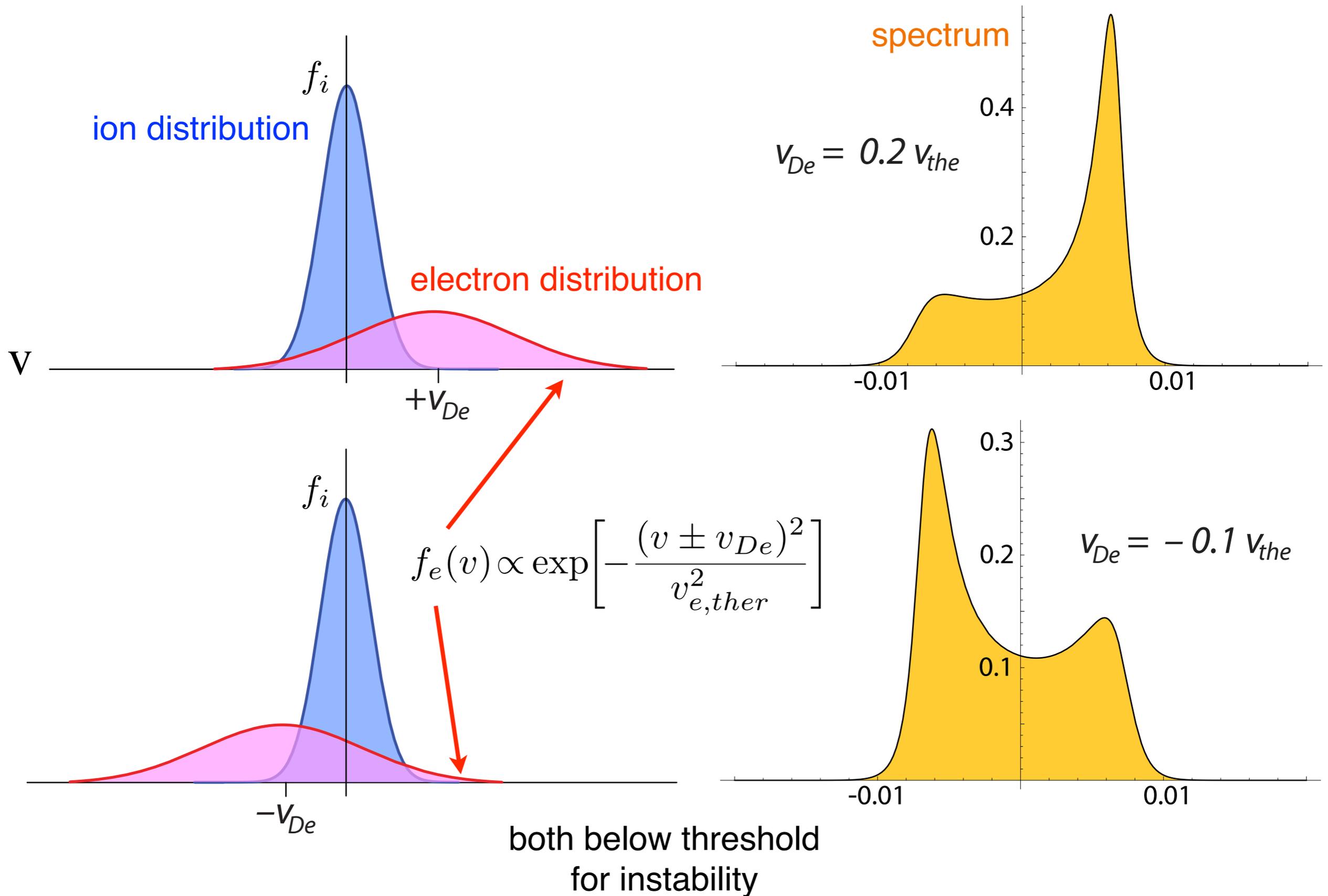
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- Long filaments aligned with geomagnetic field -  
from 150 to  $\geq 1500$  km long and 300 m thick

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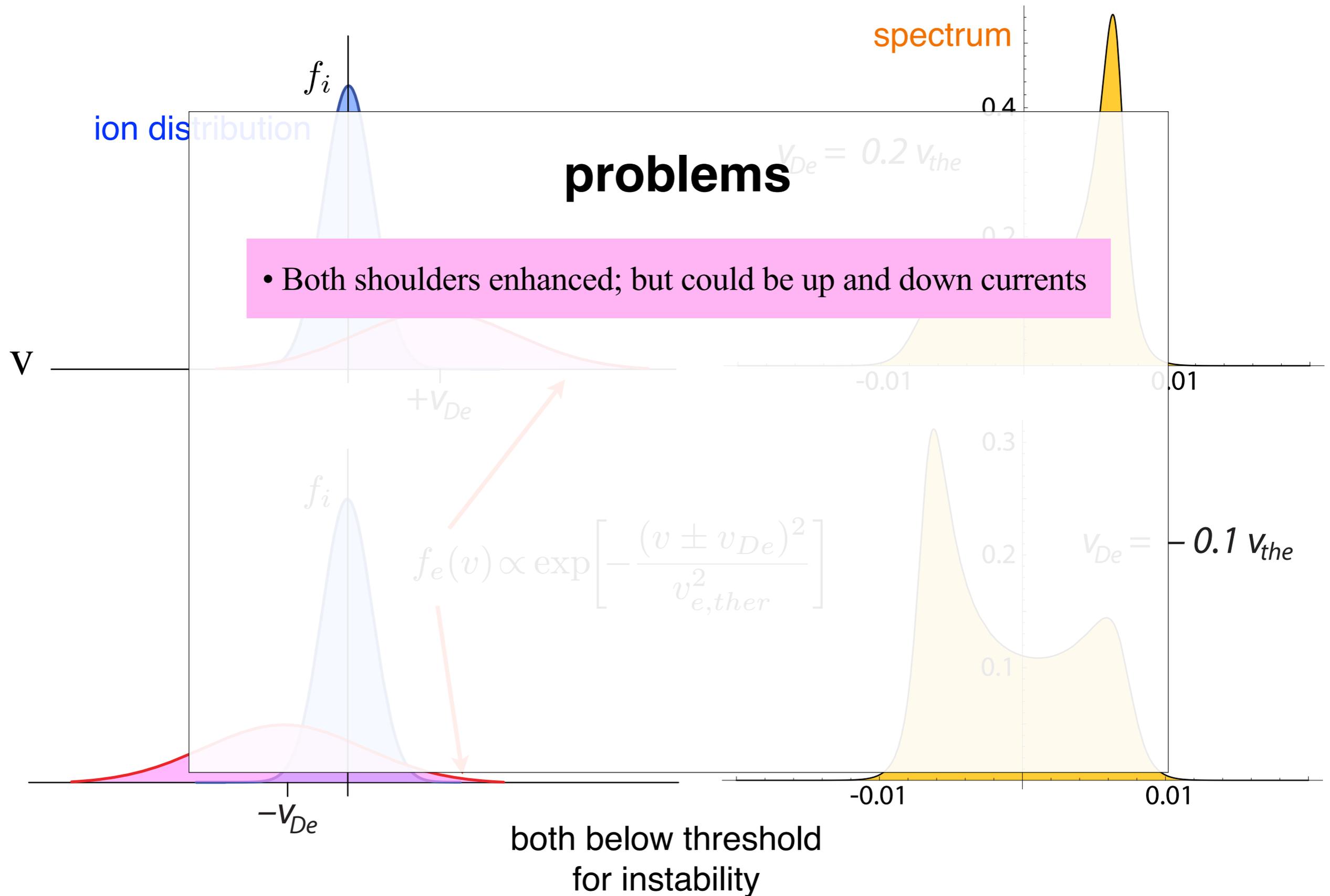


- Infrequent, short lifetime  
100ms to  $\geq 1$  min
- Enhanced up to 50 dB
- Long filaments aligned with geomagnetic field -  
from 150 to  $\geq 1500$  km long and 300 m thick
- Correlation with soft electron aurora  $\leq 500$  eV

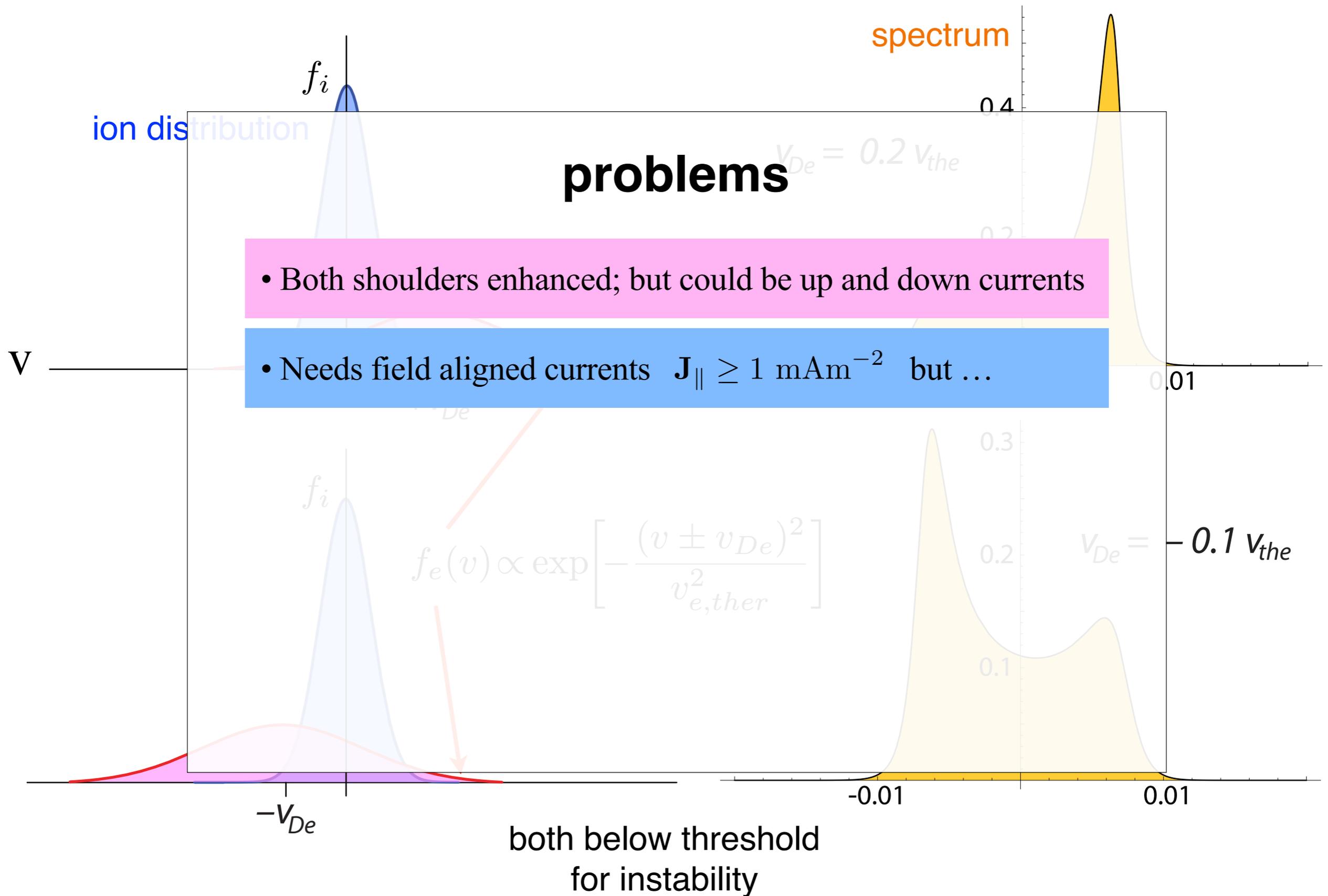
# thermal electron current



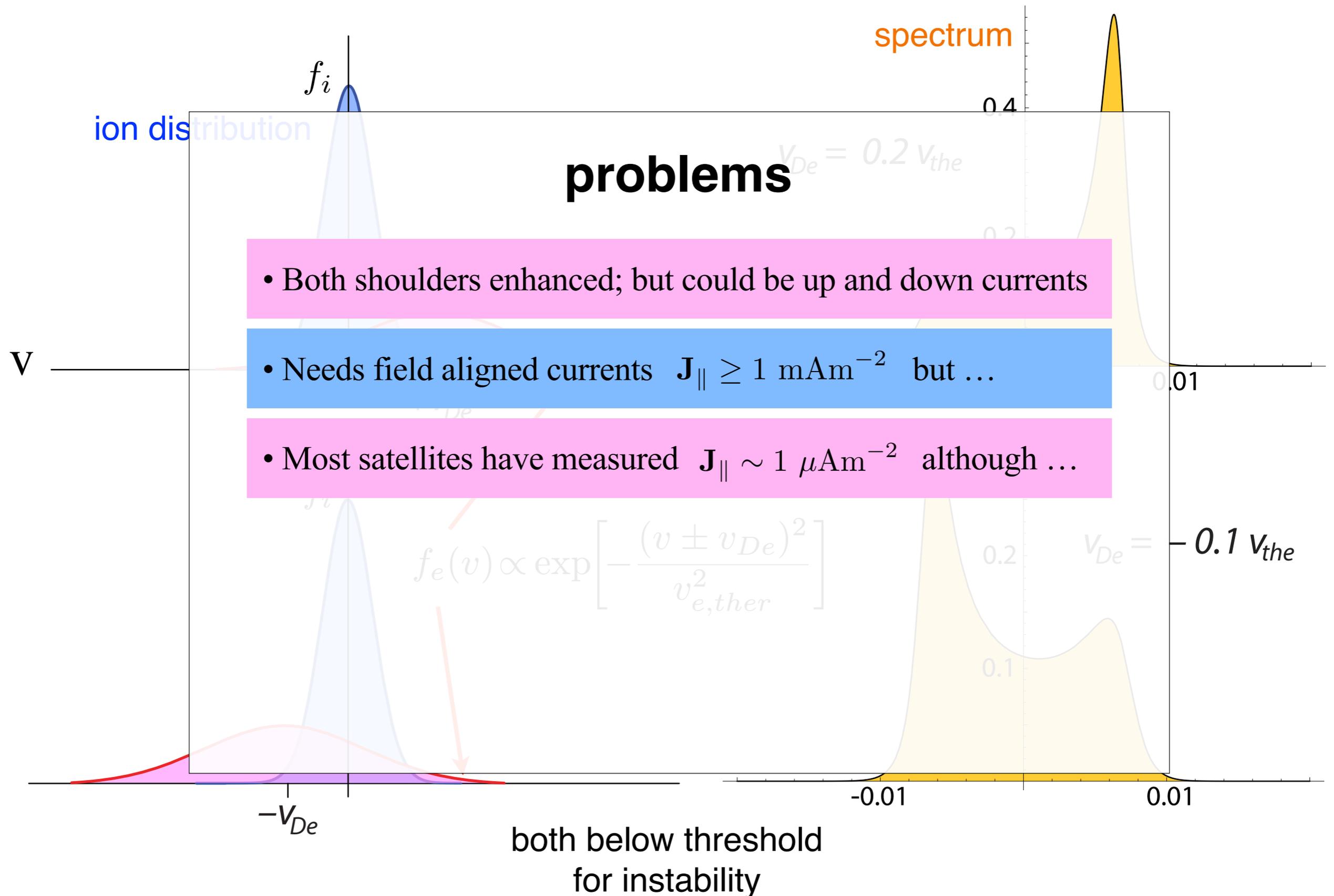
# thermal electron current



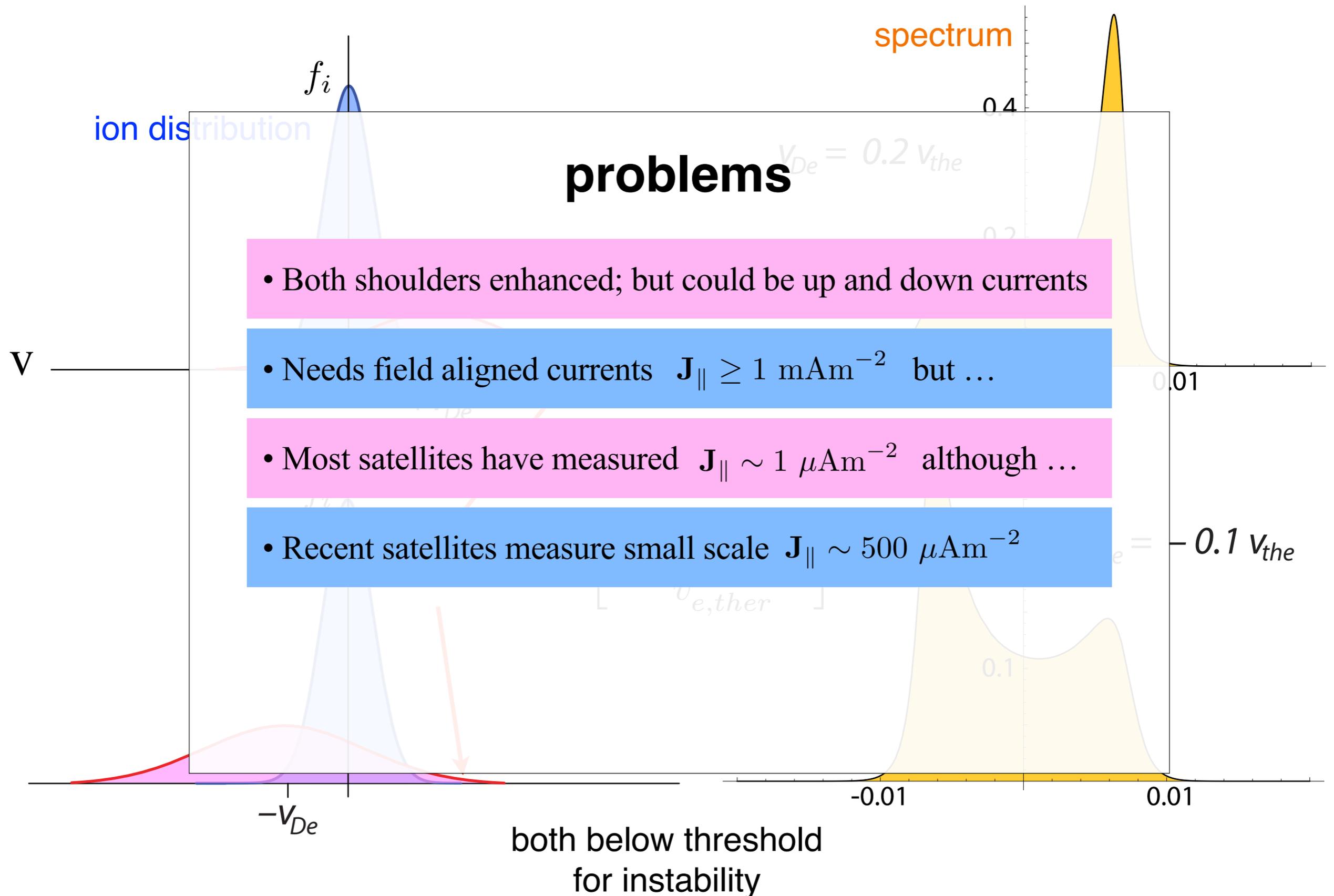
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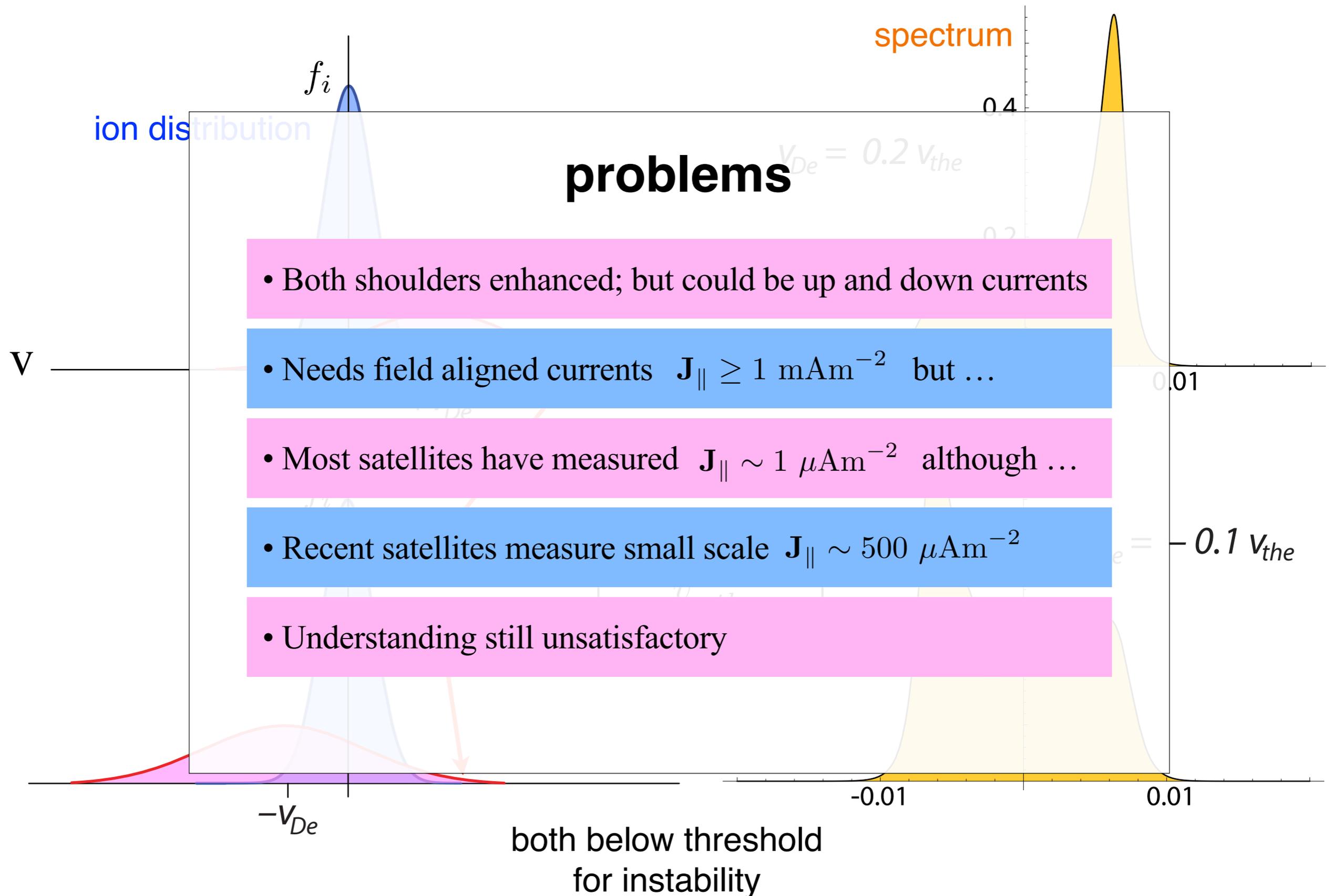
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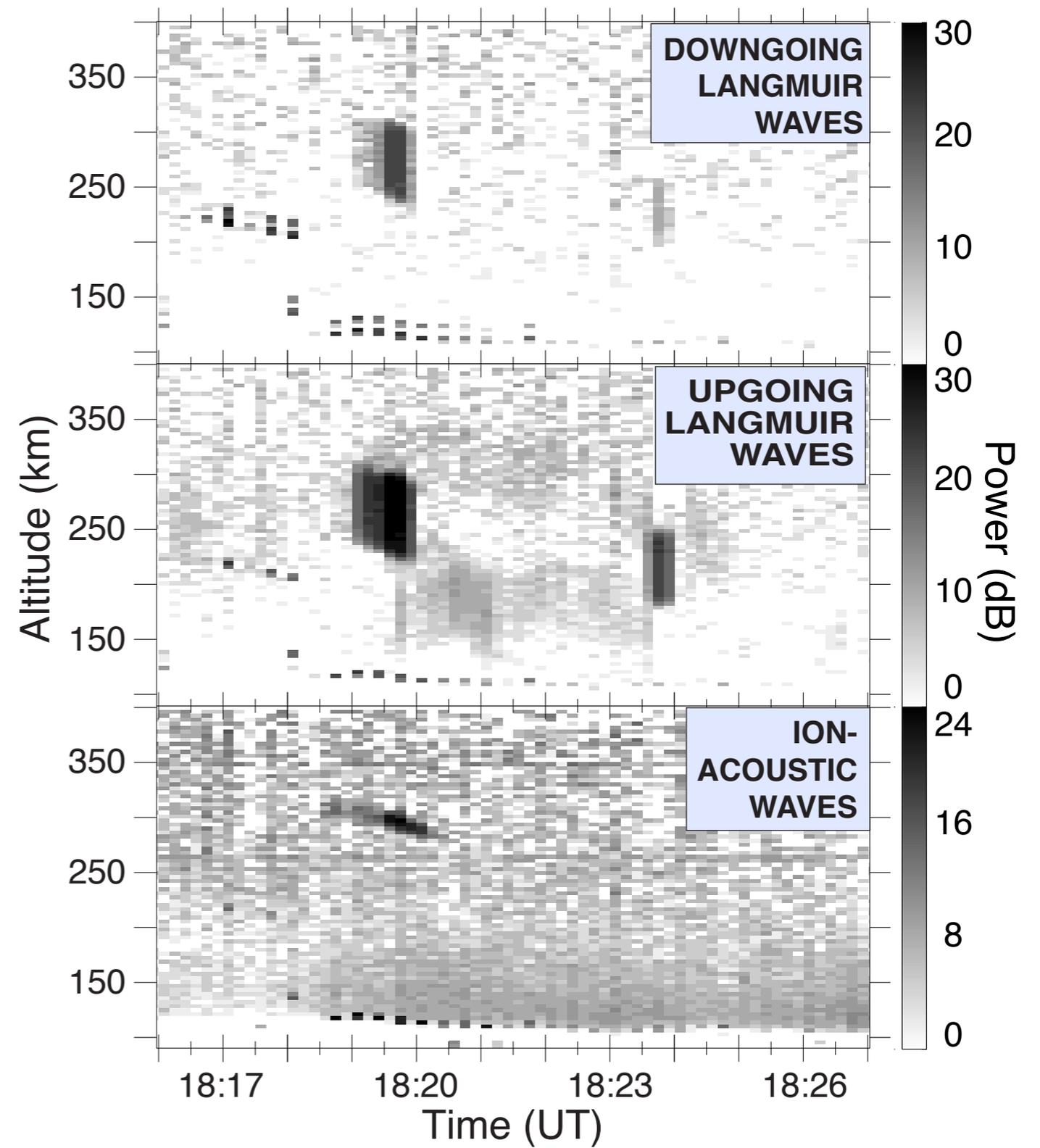
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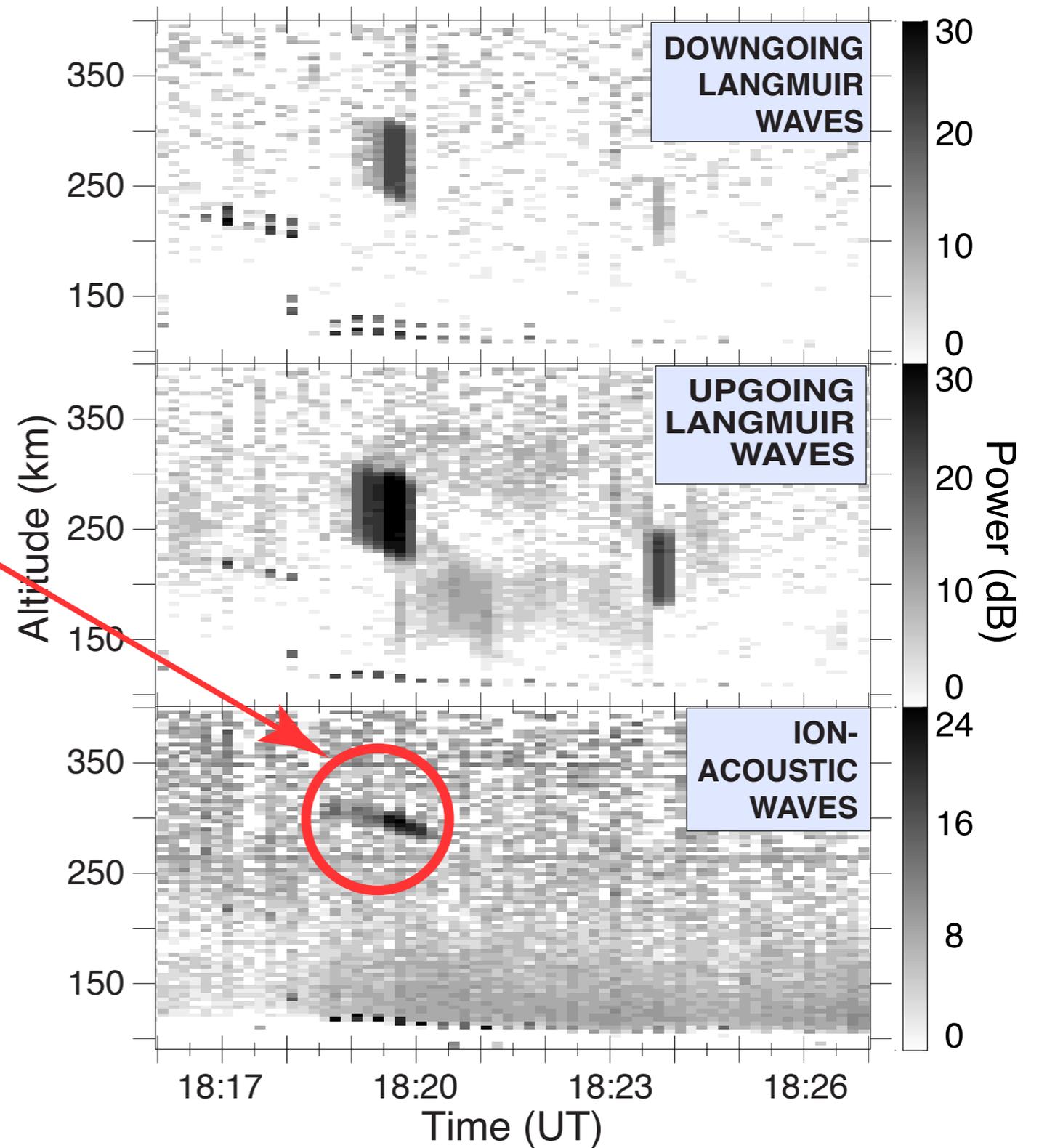


# total power measurements



# total power measurements

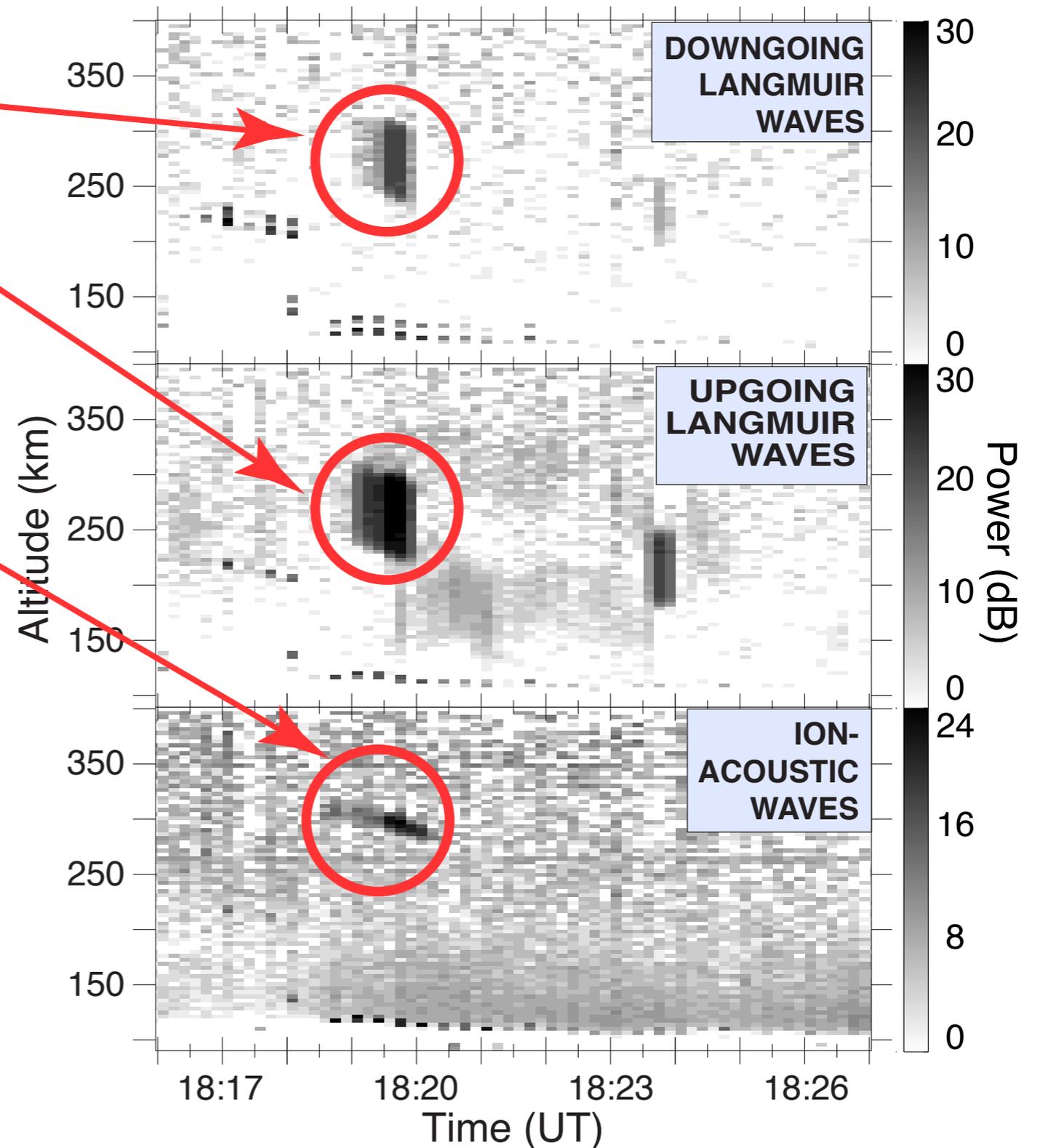
ion acoustic waves  
enhanced  $\times 10^2$   
above thermal level



# total power measurements

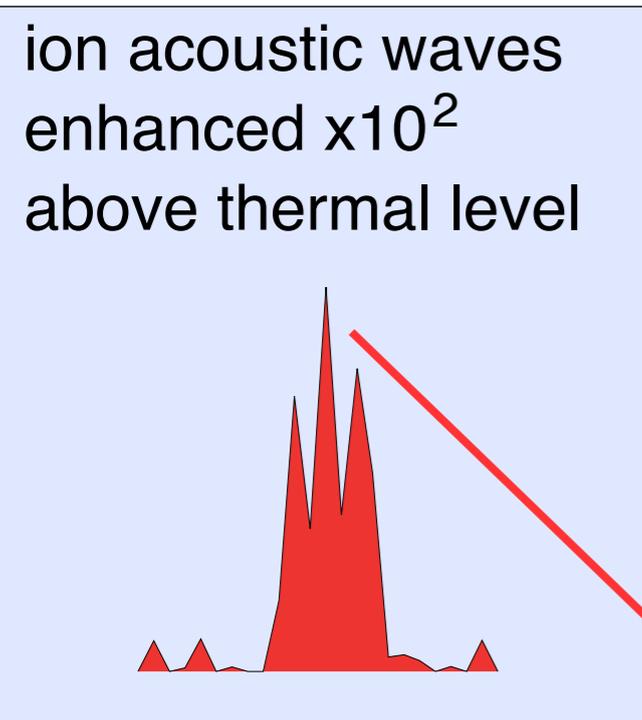
Langmuir waves  
down- and upgoing  
enhanced  $\times 10^2$  and  $\times 10^3$   
above thermal level

ion acoustic waves  
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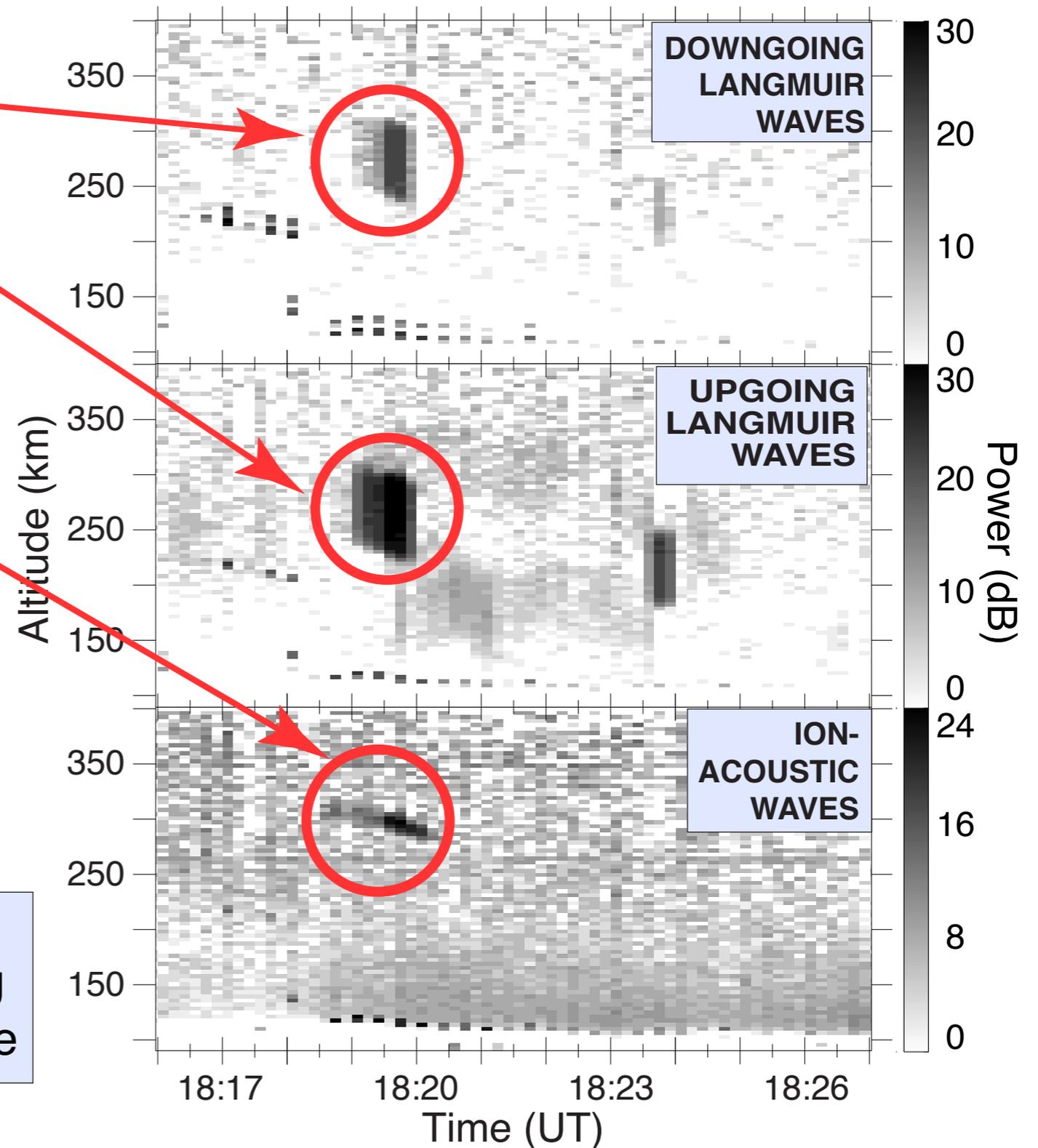


# total power measurements

Langmuir waves  
down- and upgoing  
enhanced  $\times 10^2$  and  $\times 10^3$   
above thermal level



central peak:  
signature of strong  
Langmuir turbulence



# Zakharov equations 1-D

Langmuir  
waves

$$i(\partial_t + \gamma^\ell)E + \partial_{xx}^2 E = nE$$

Ion sound  
waves

$$(\partial_{tt}^2 + \gamma^s \partial_t)n - \partial_{xx}^2 n = \partial_{xx}^2 |E|^2$$

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Damping and  
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Bump-in-tail  
growth

$$\gamma_b(k) = \frac{\chi}{\tau} \frac{\pi}{2n} \frac{\omega_{pe}^3}{k^2} \partial_v F_b(v) \Big|_{v=\omega_{pe}/k}$$

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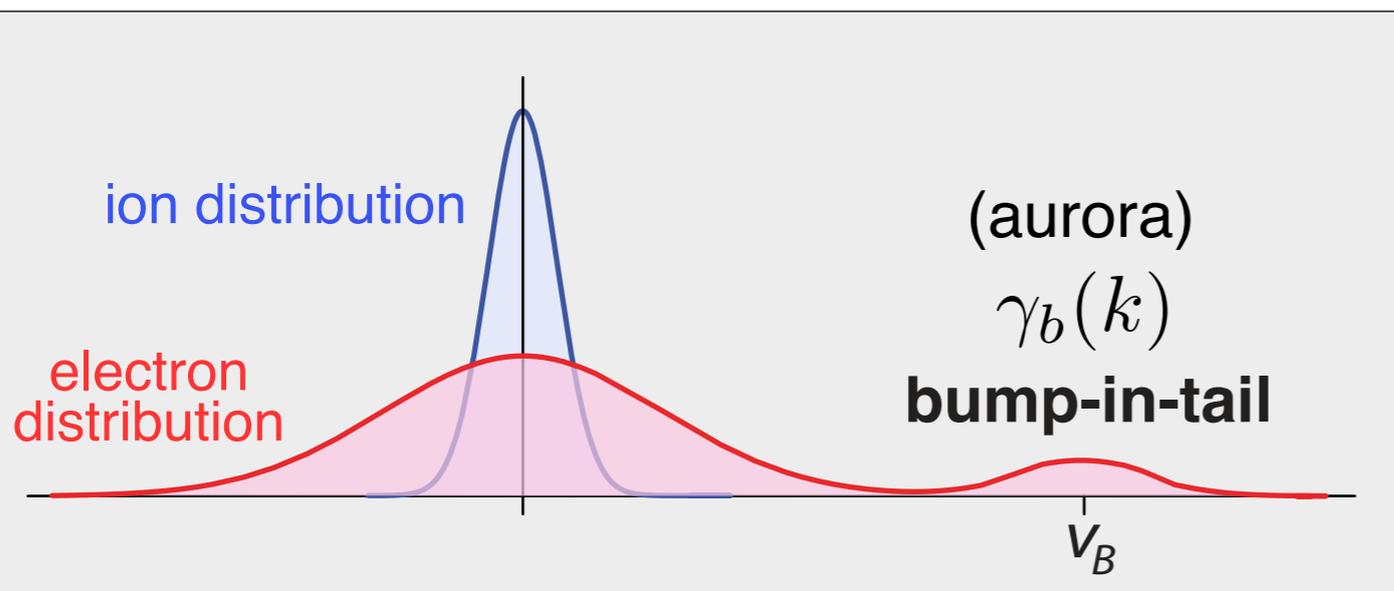
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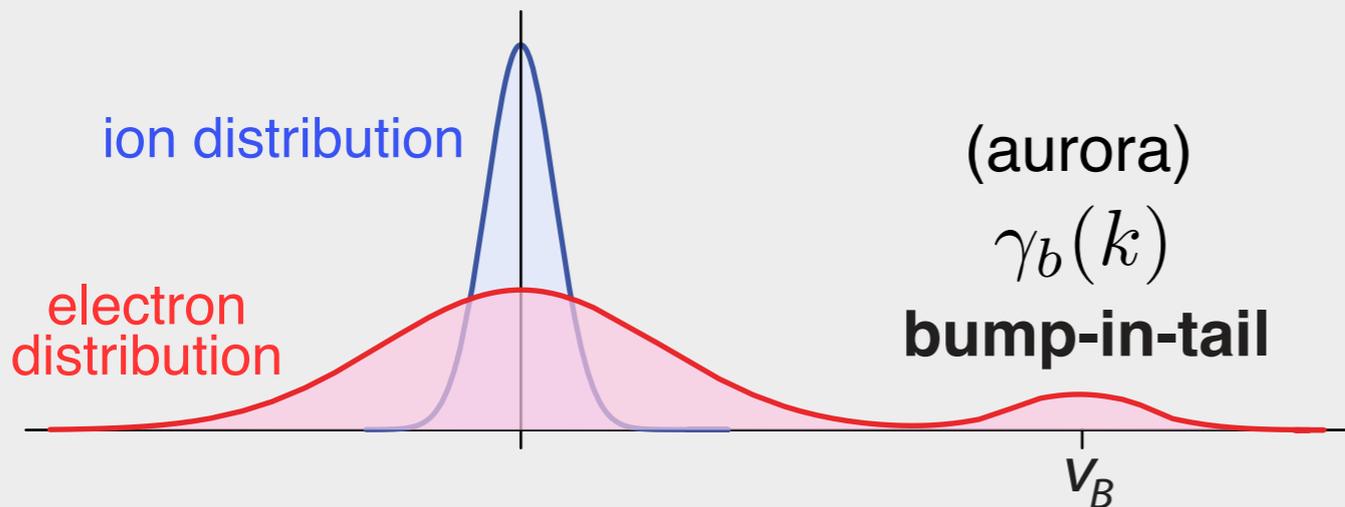
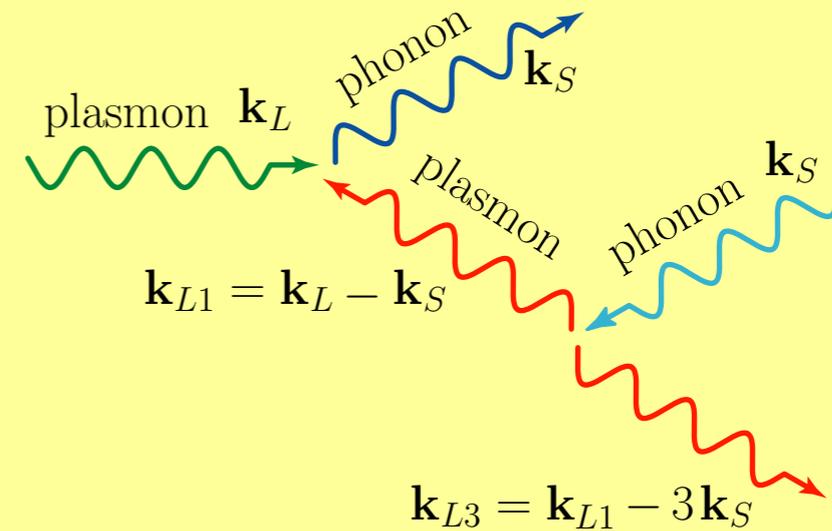
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wave-wave interactions



# Zakharov equations 1-D

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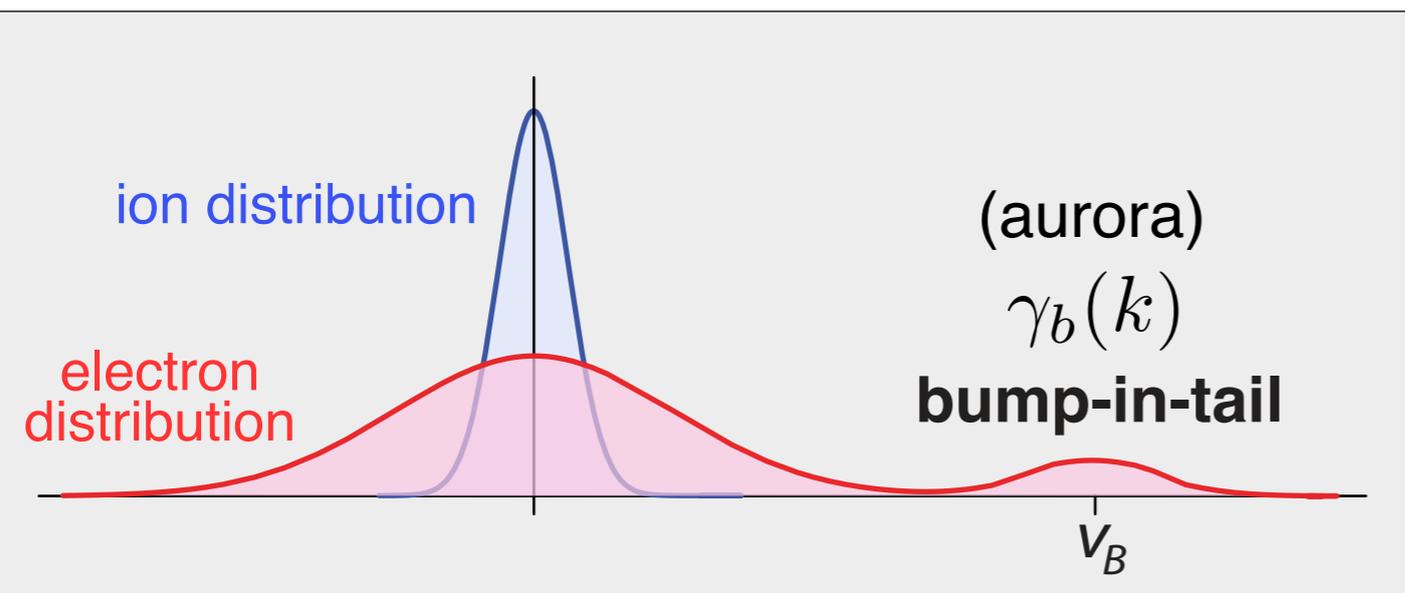
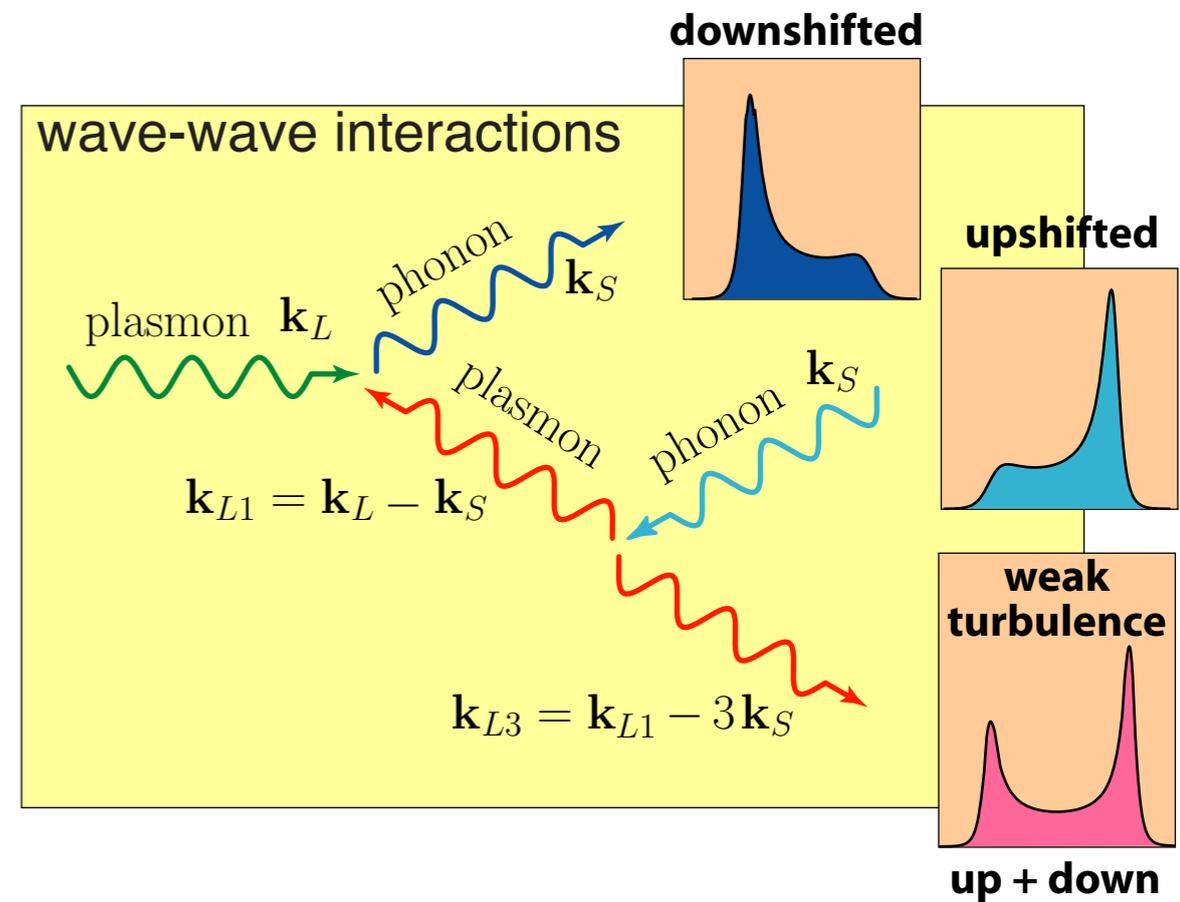
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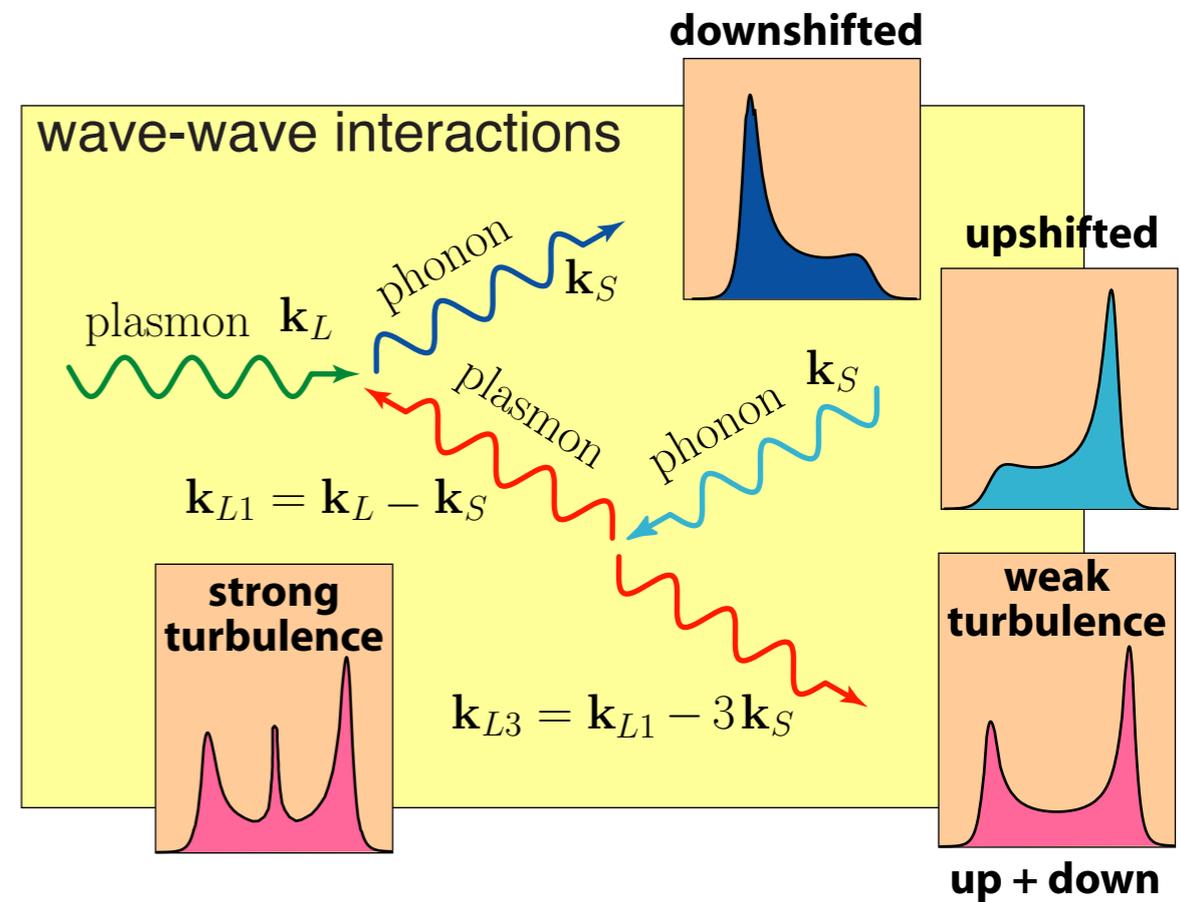
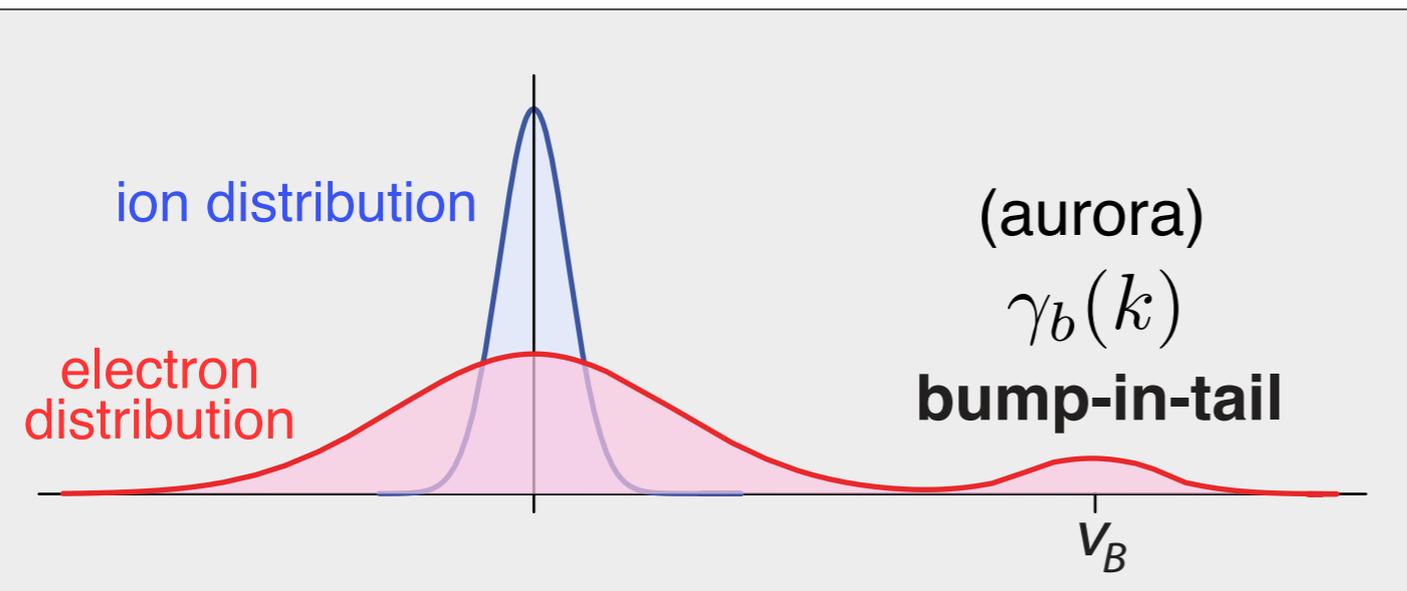
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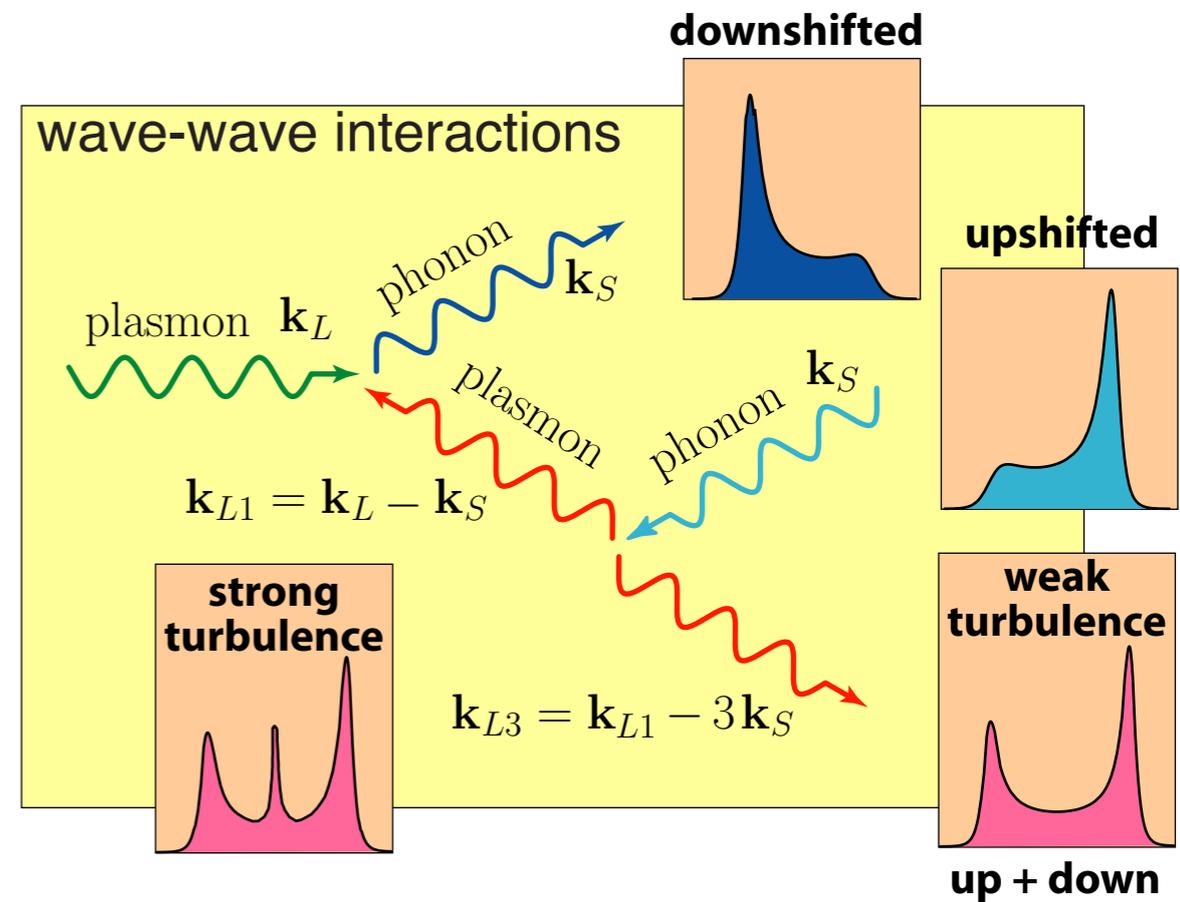
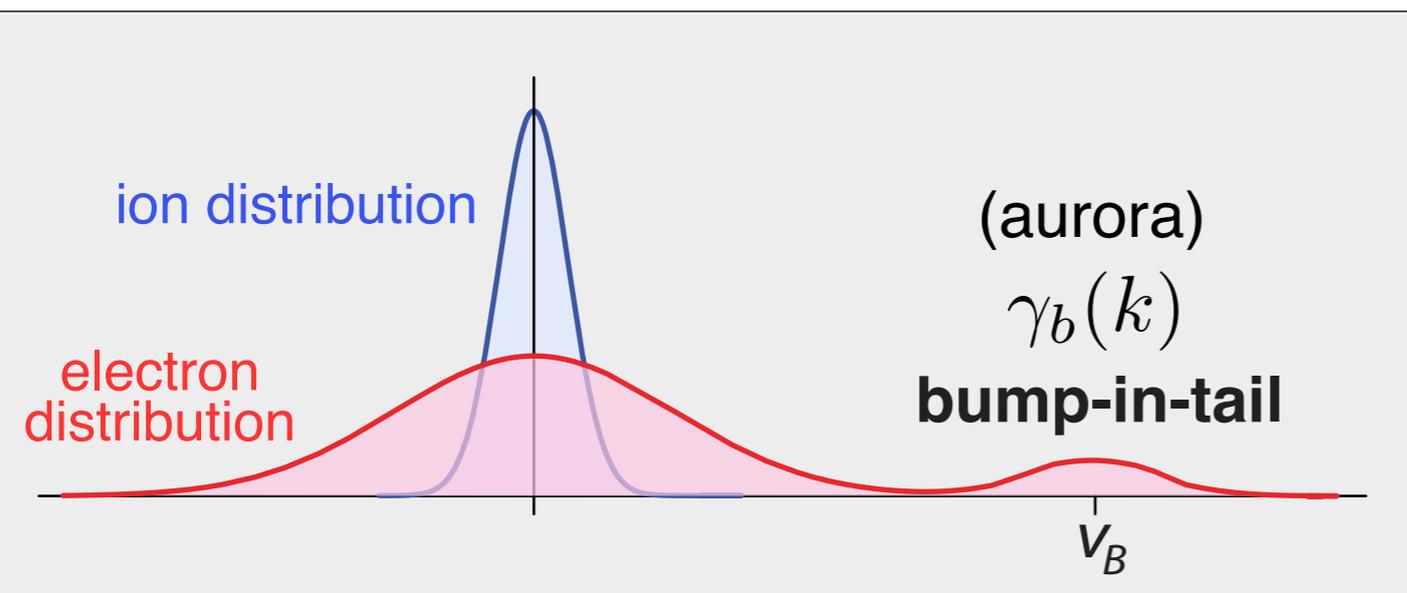
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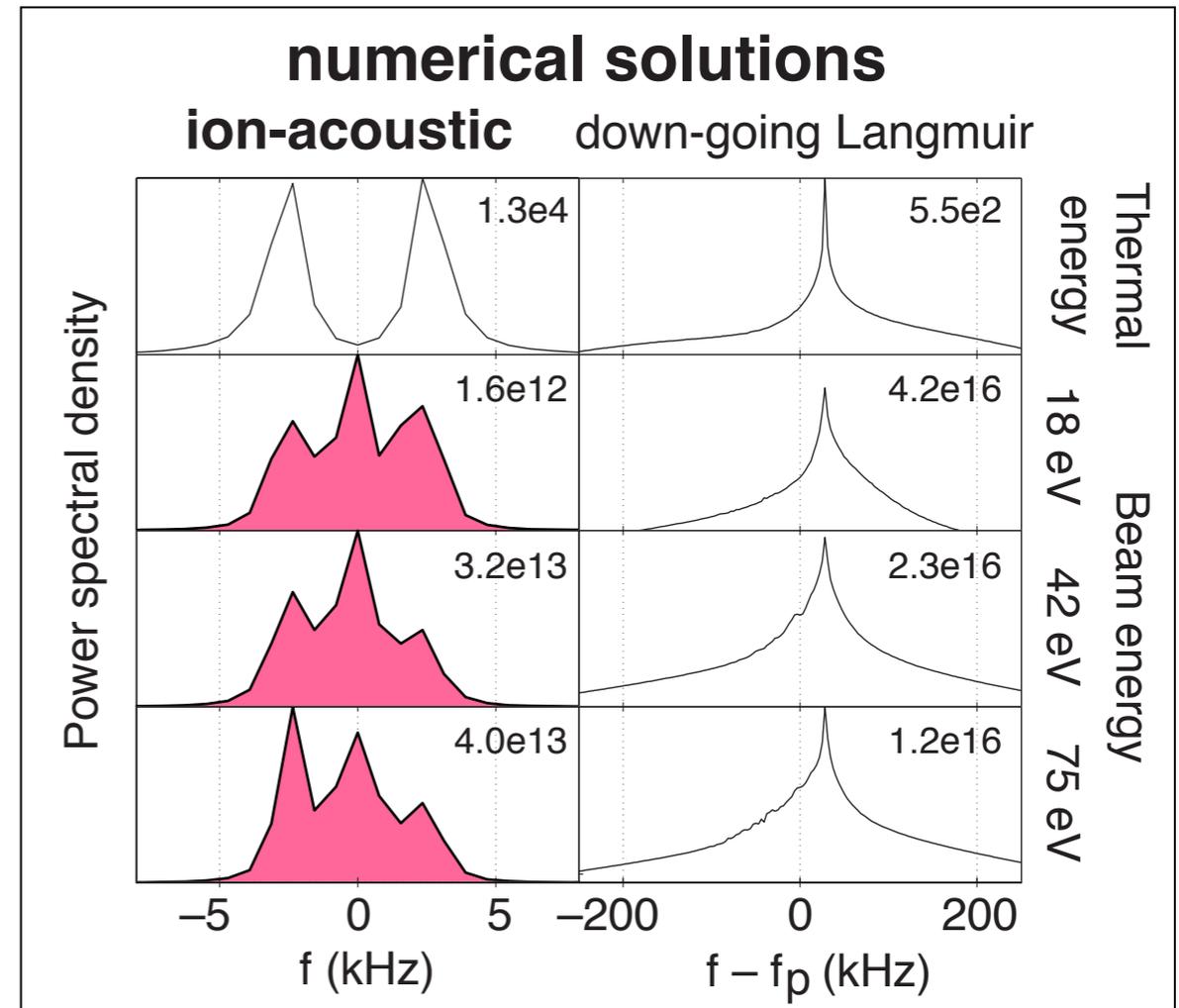
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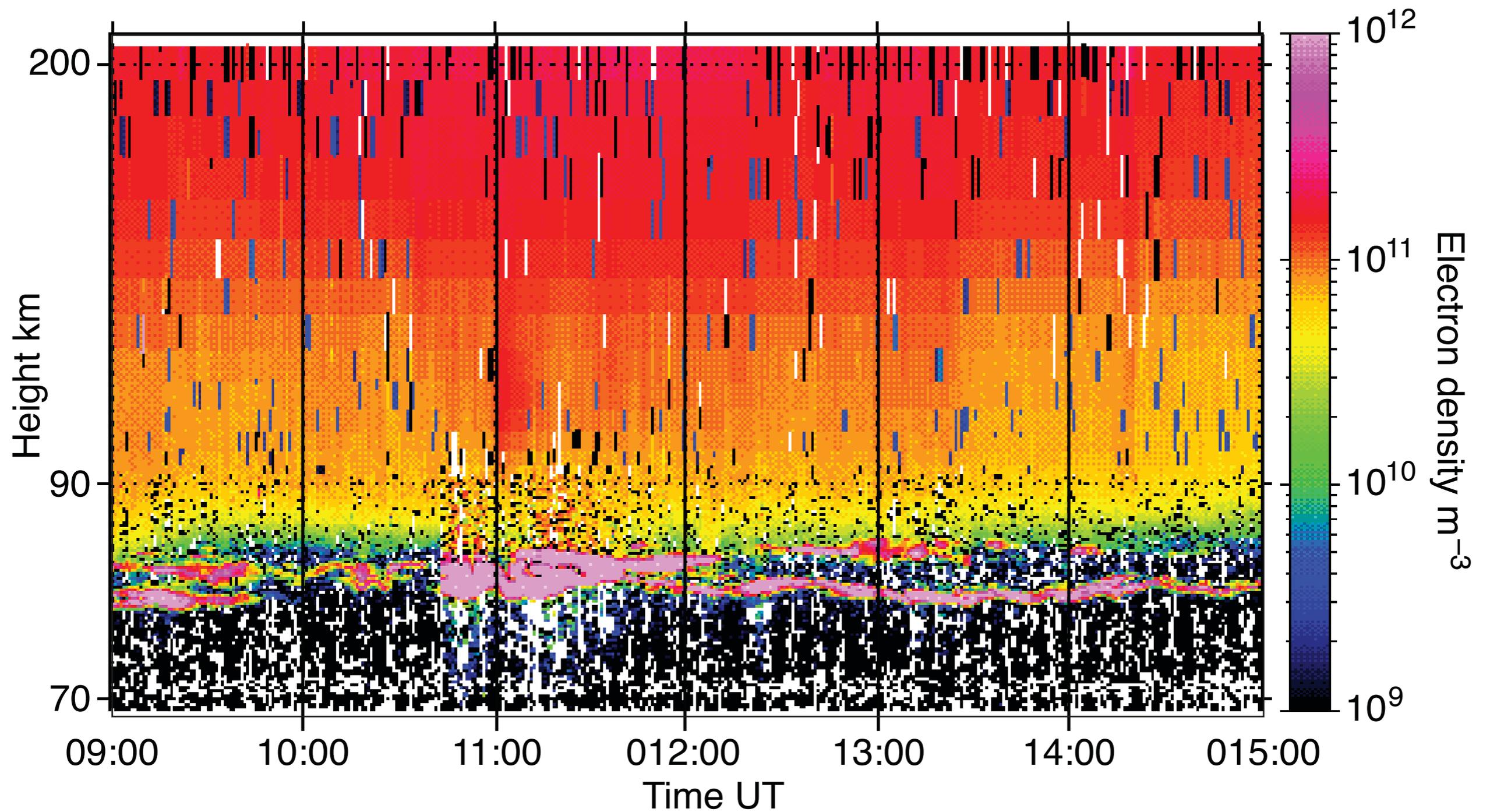
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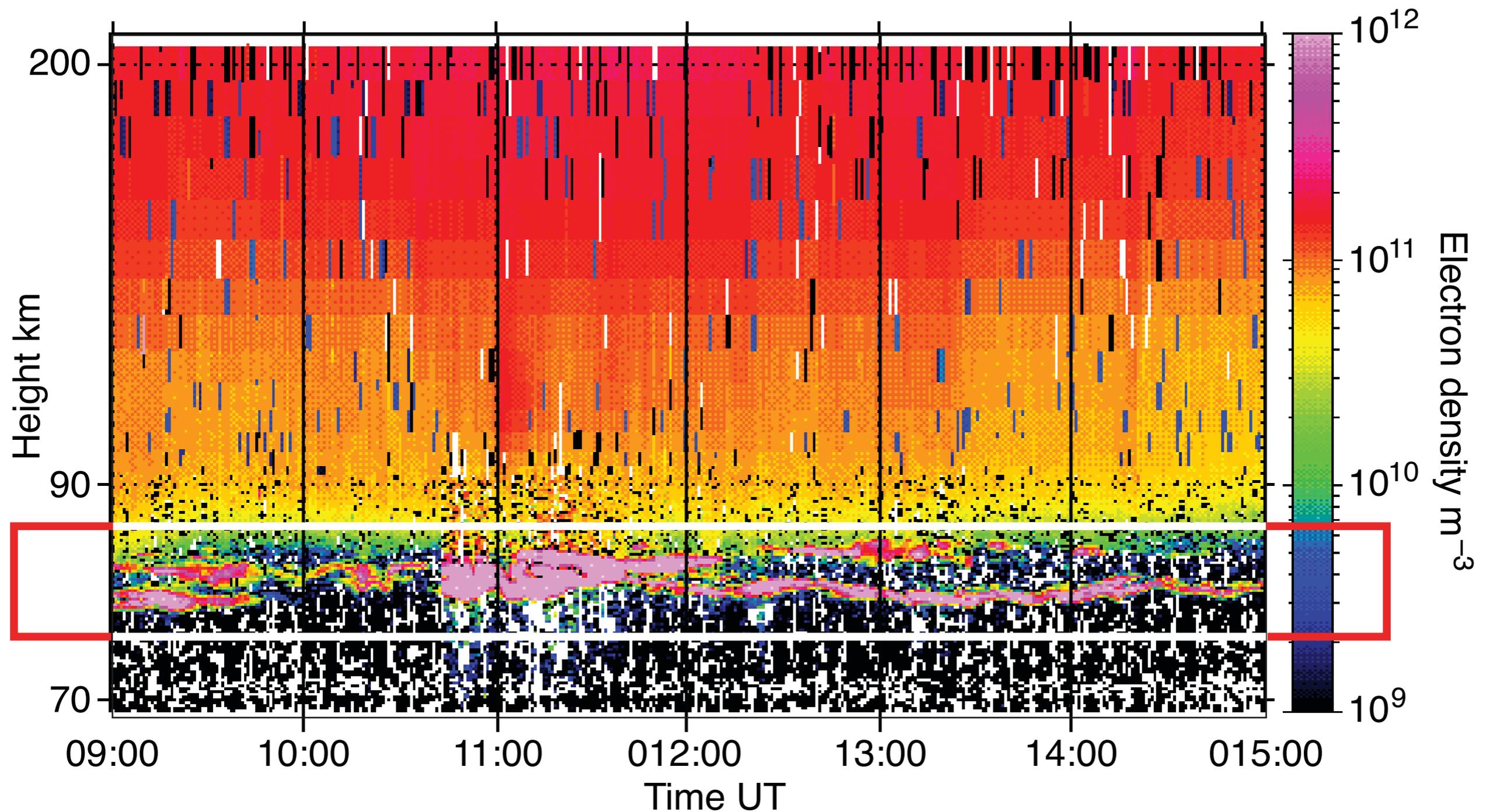
Guio & Forme 2006



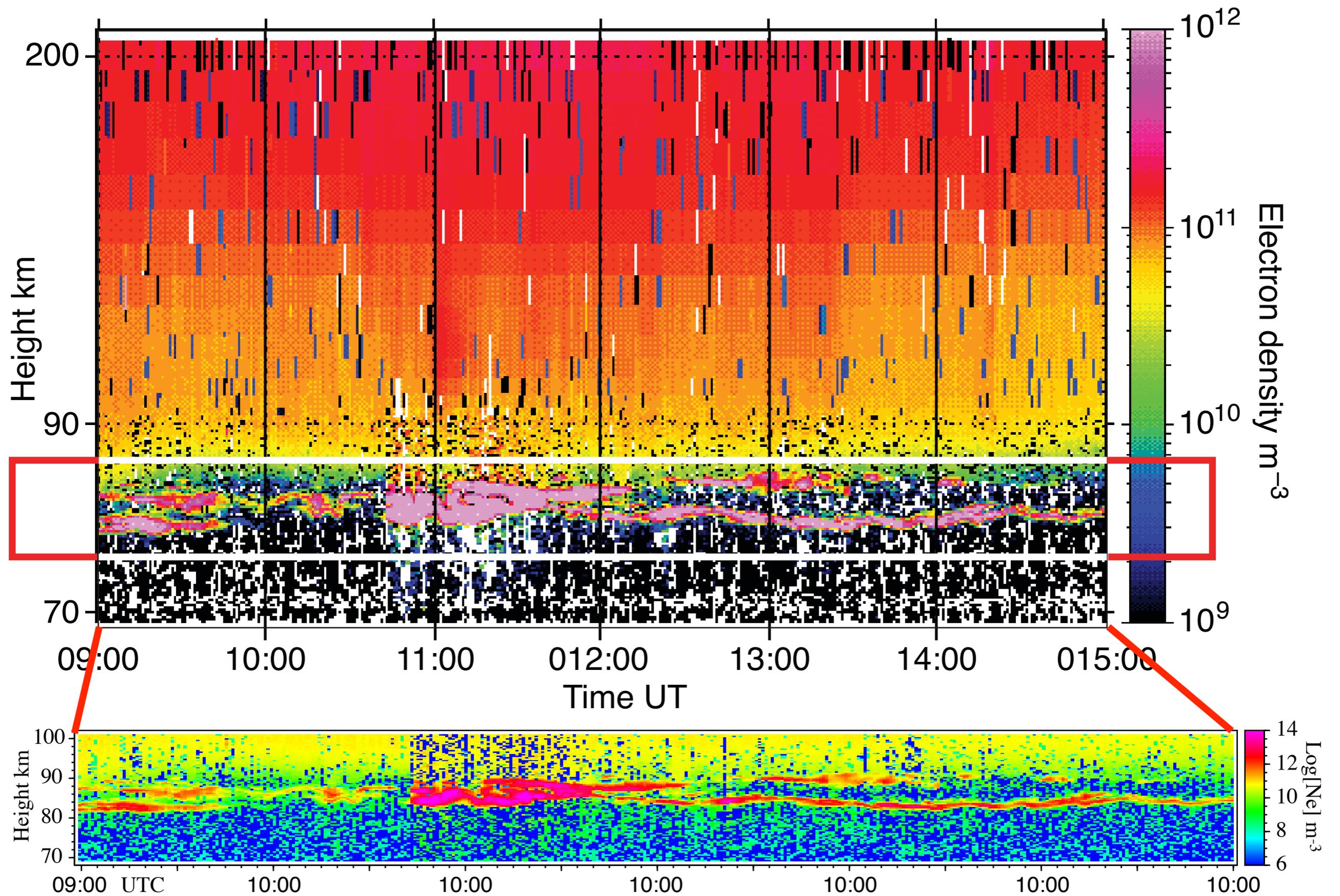
# 3. Polar Mesospheric Summer Echoes PMSE



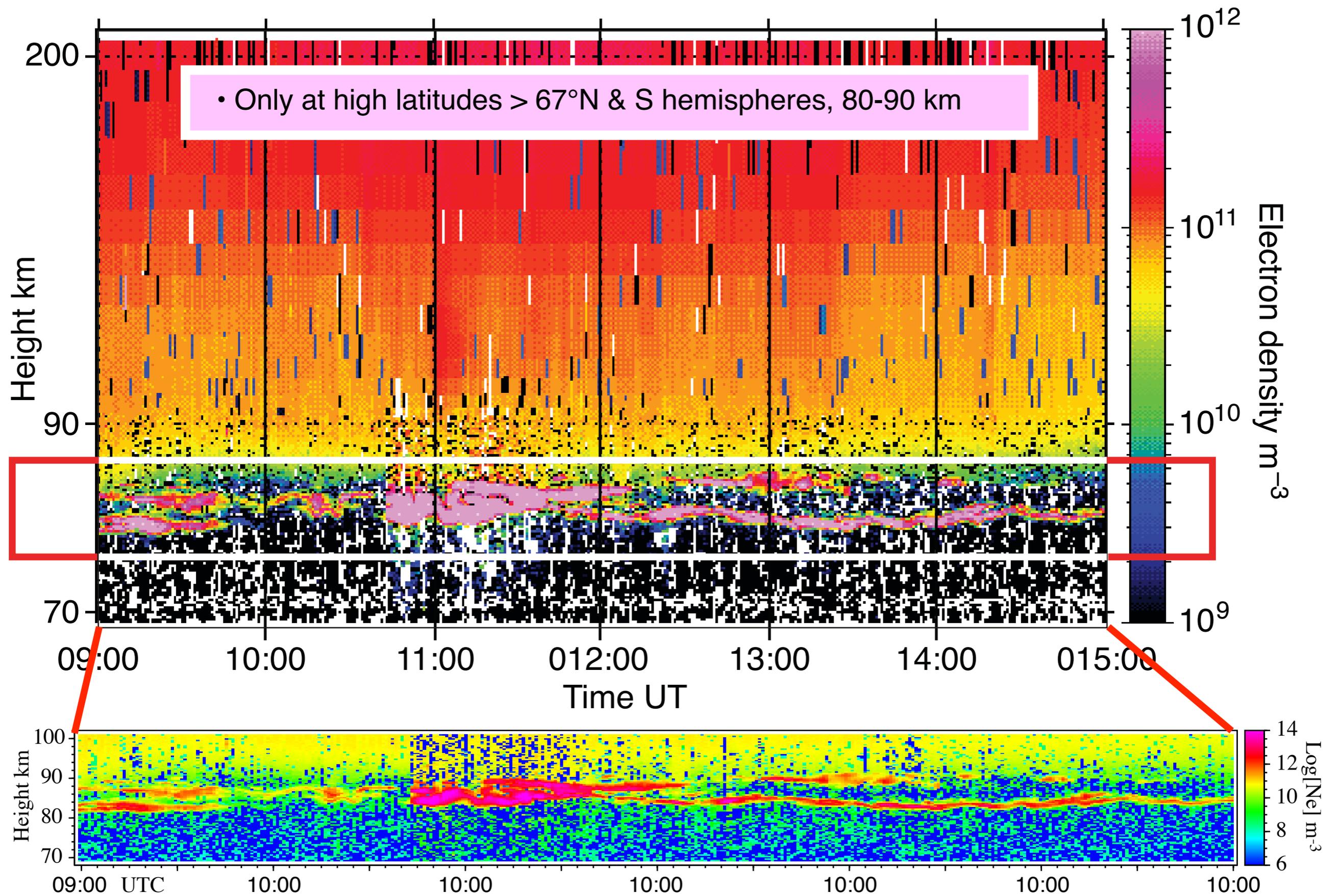
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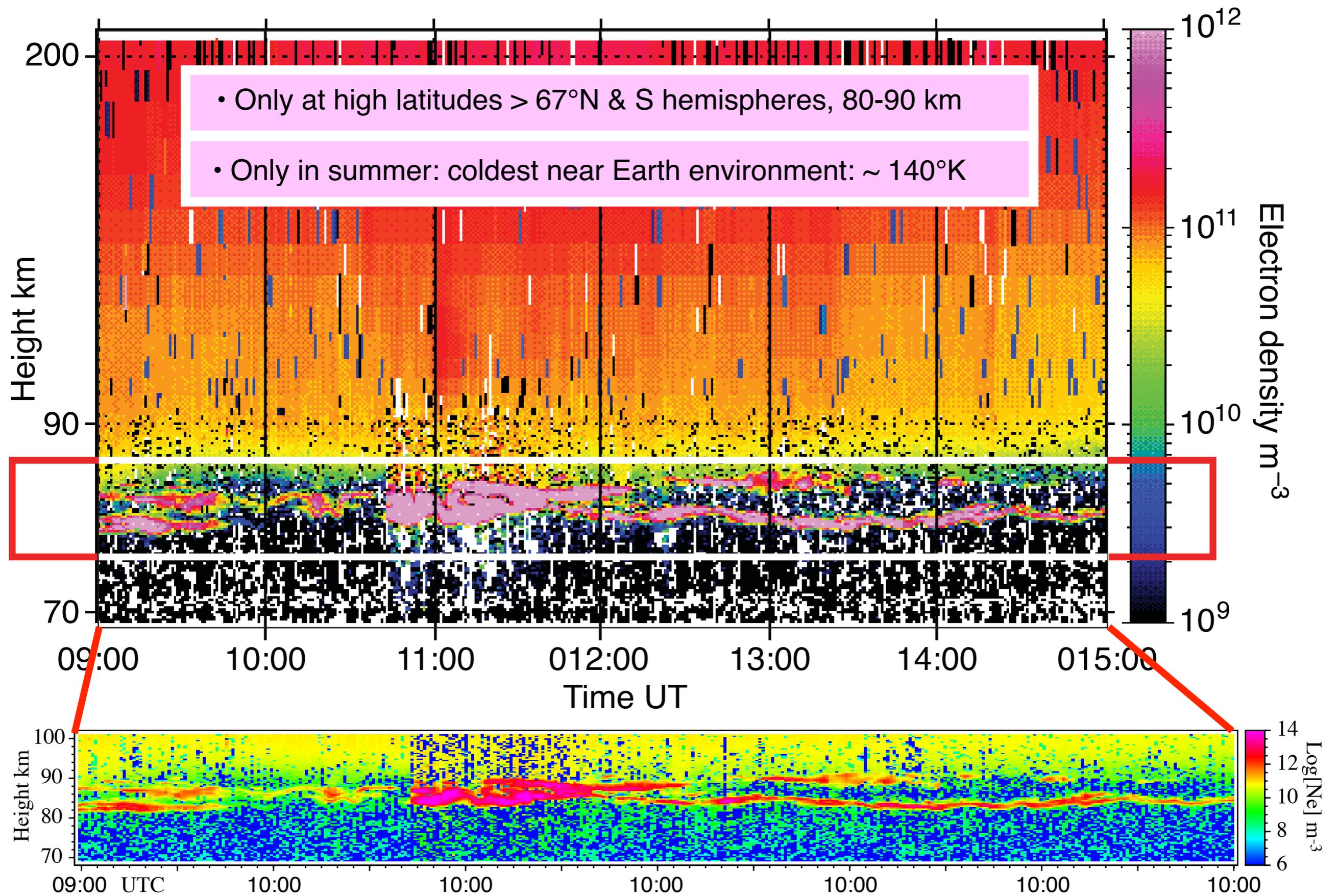
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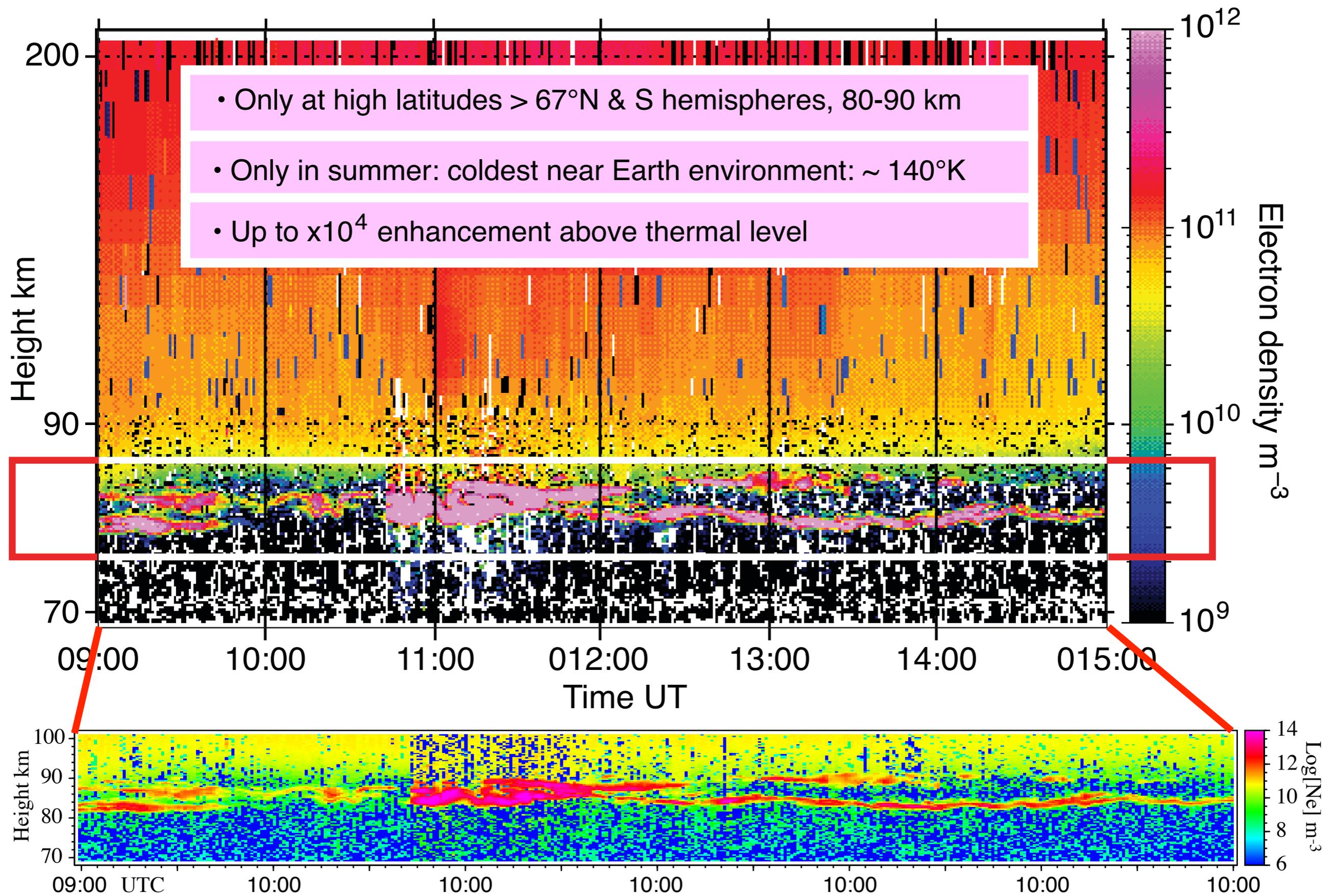
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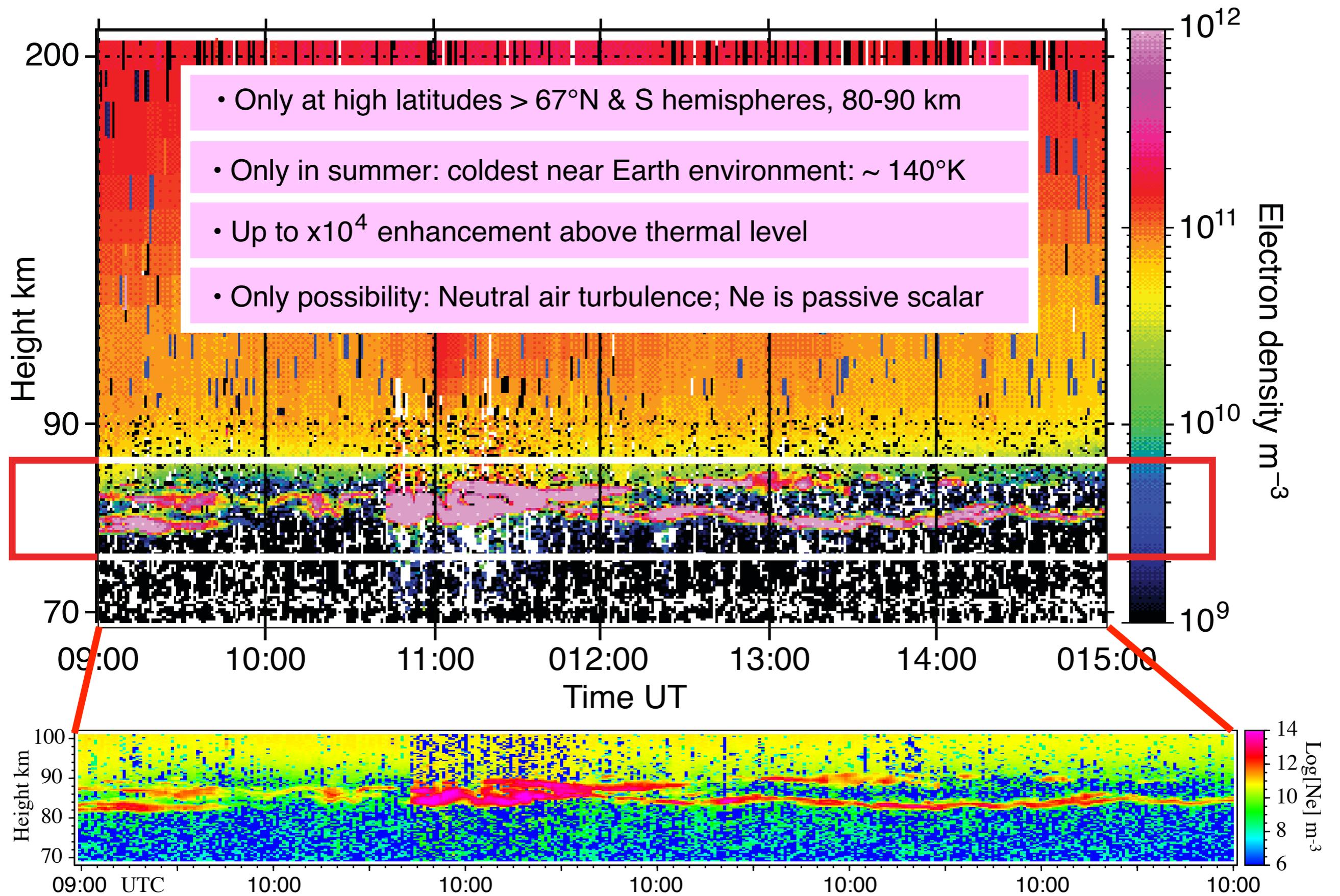
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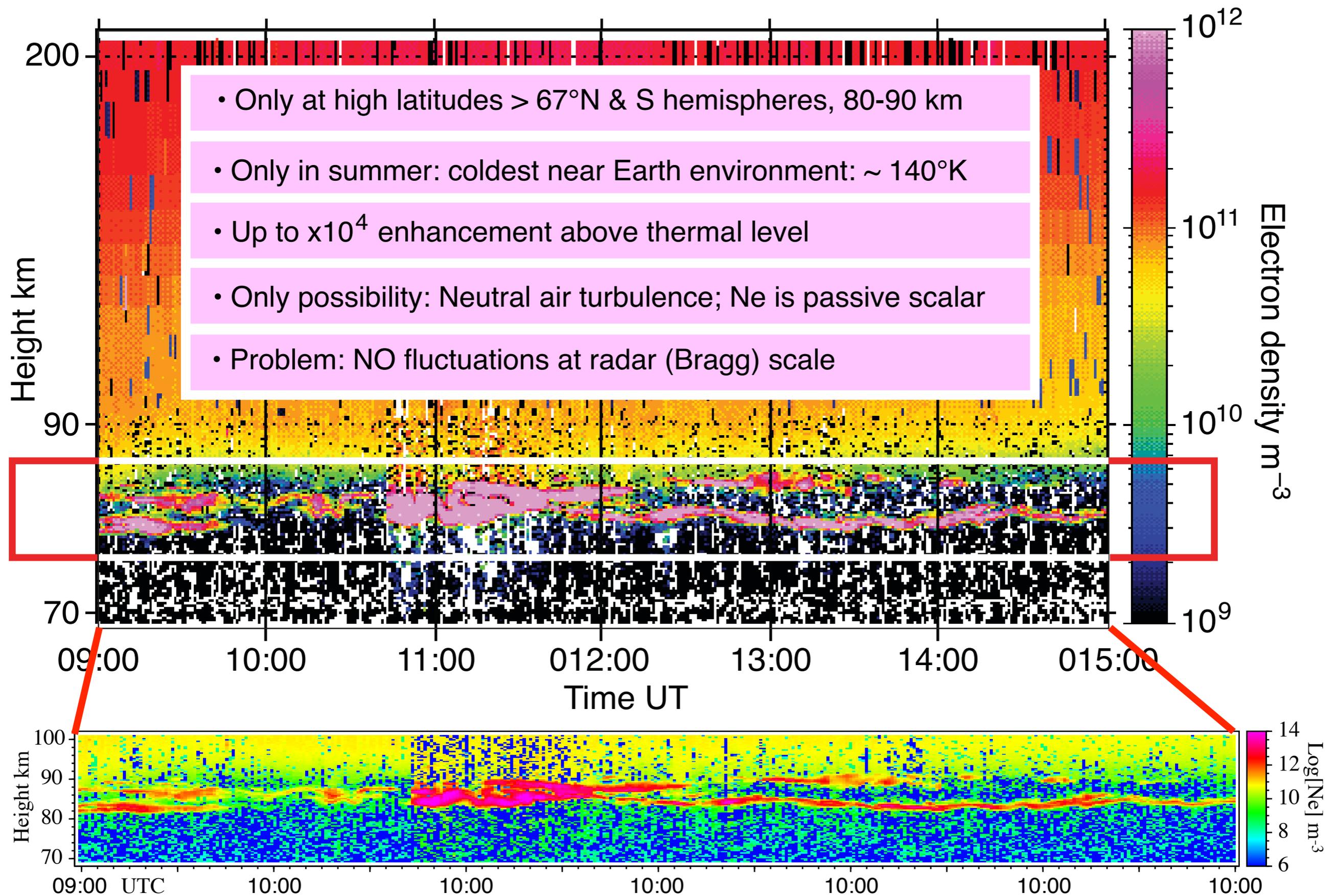
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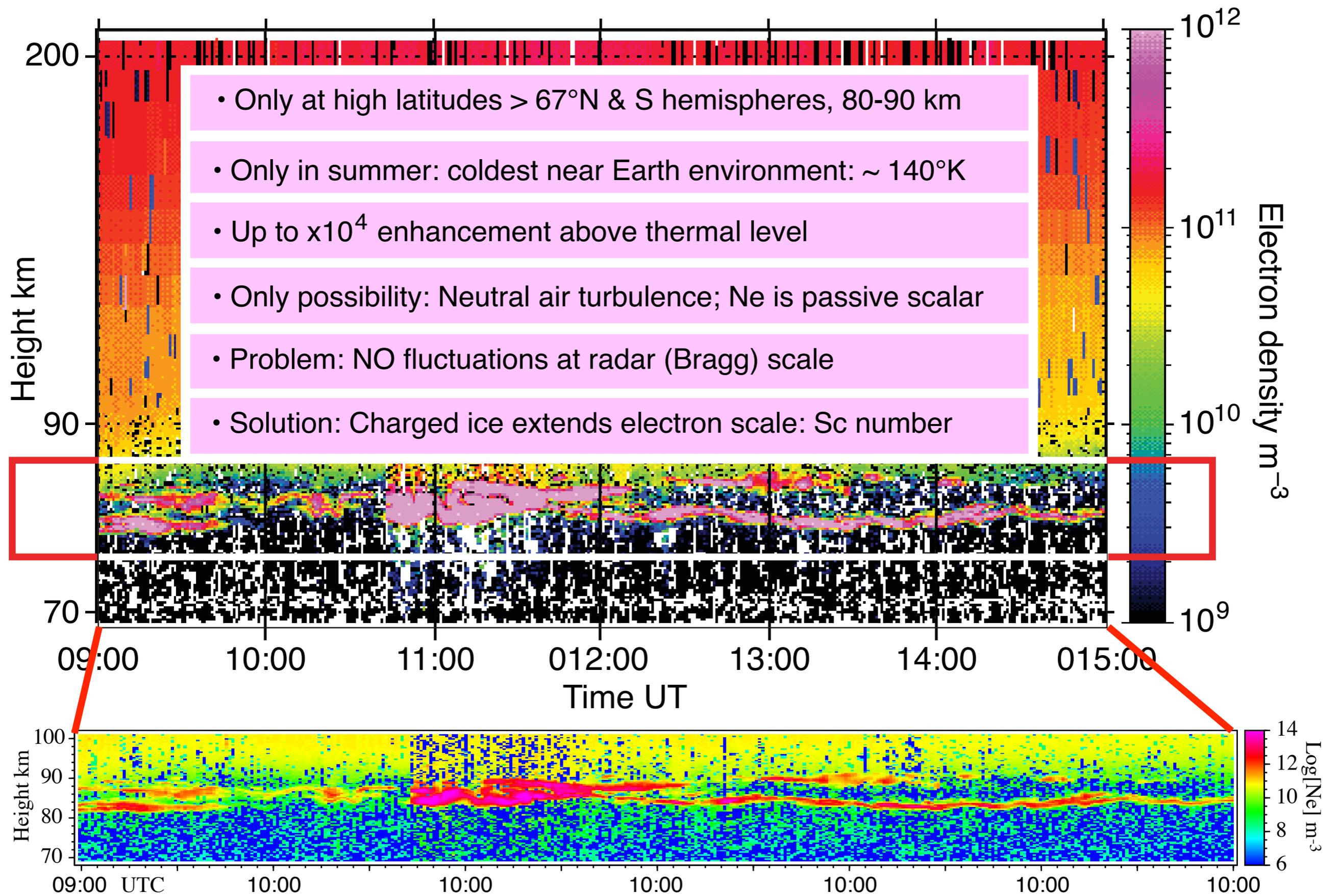
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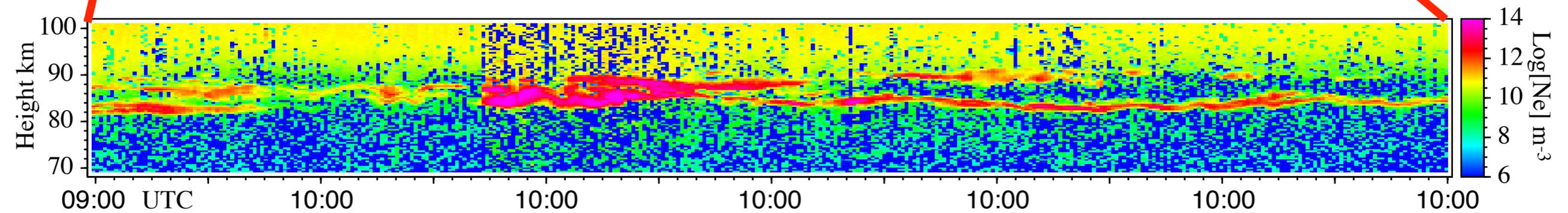
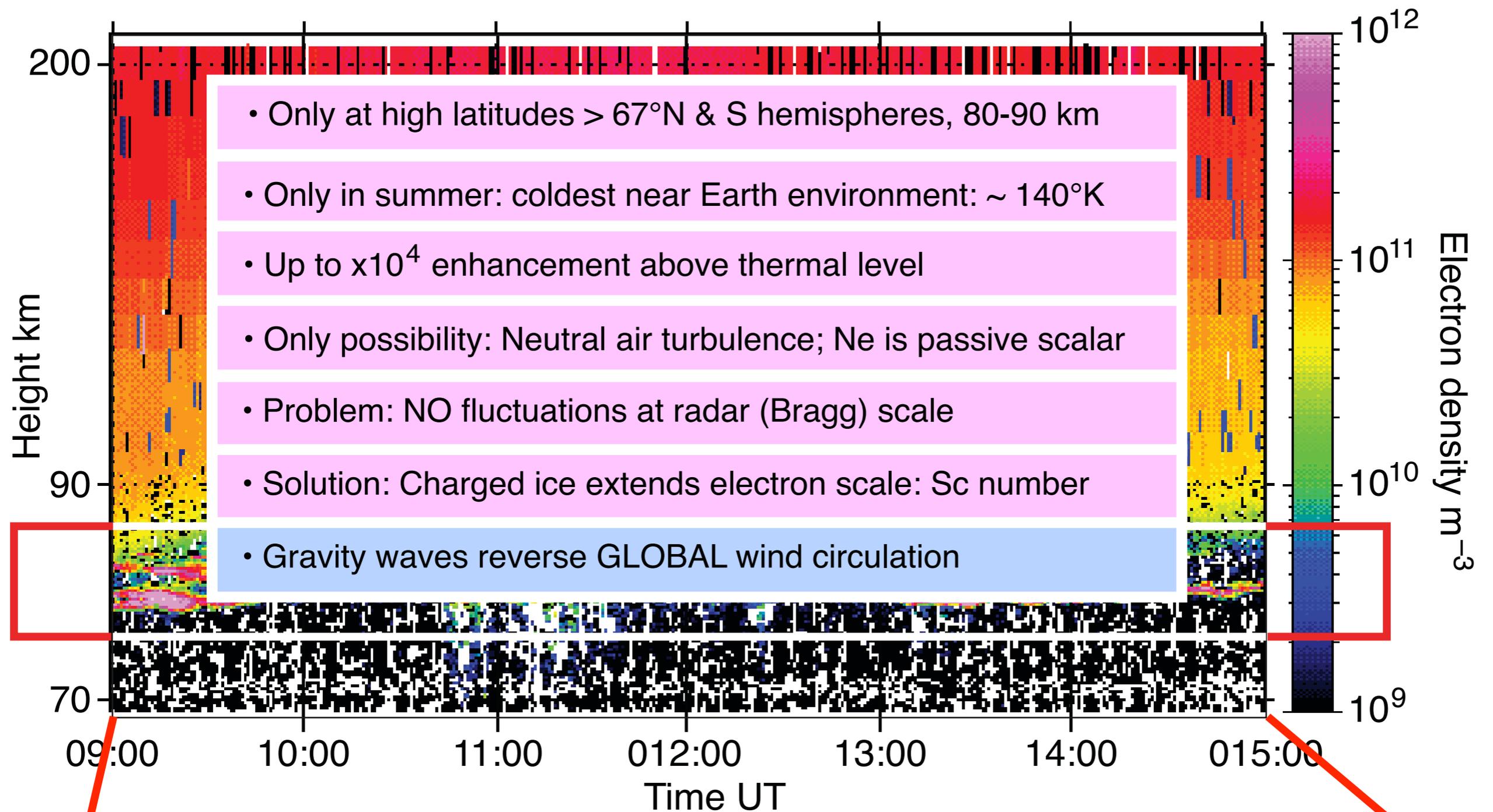
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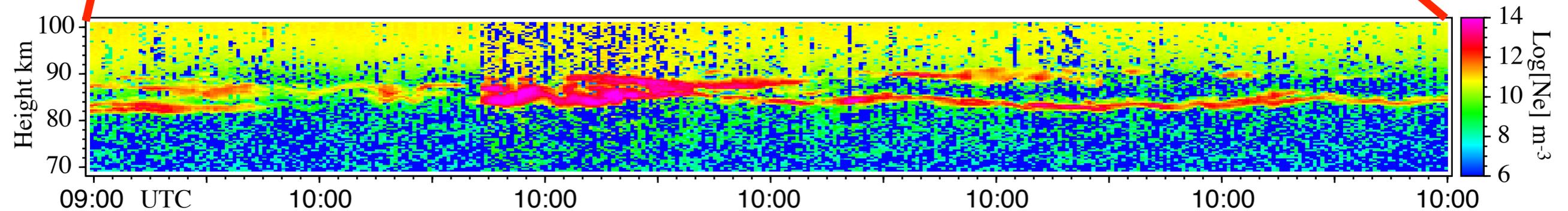
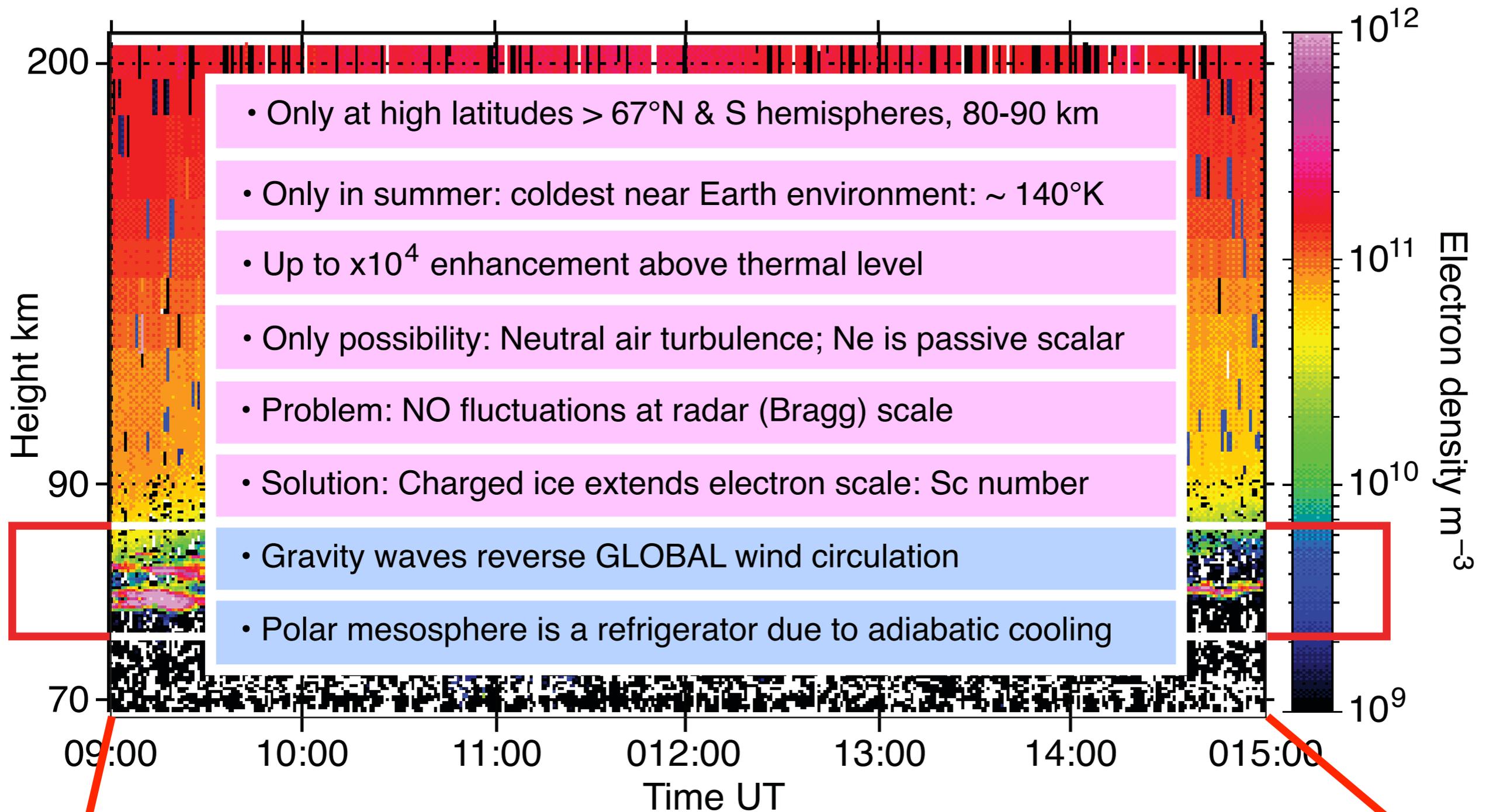
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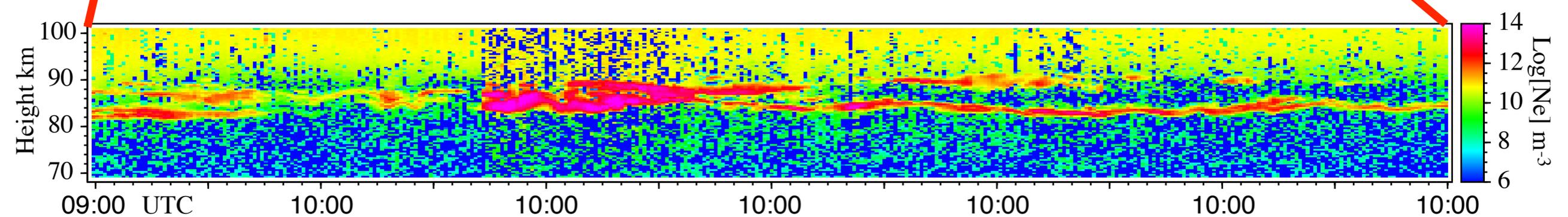
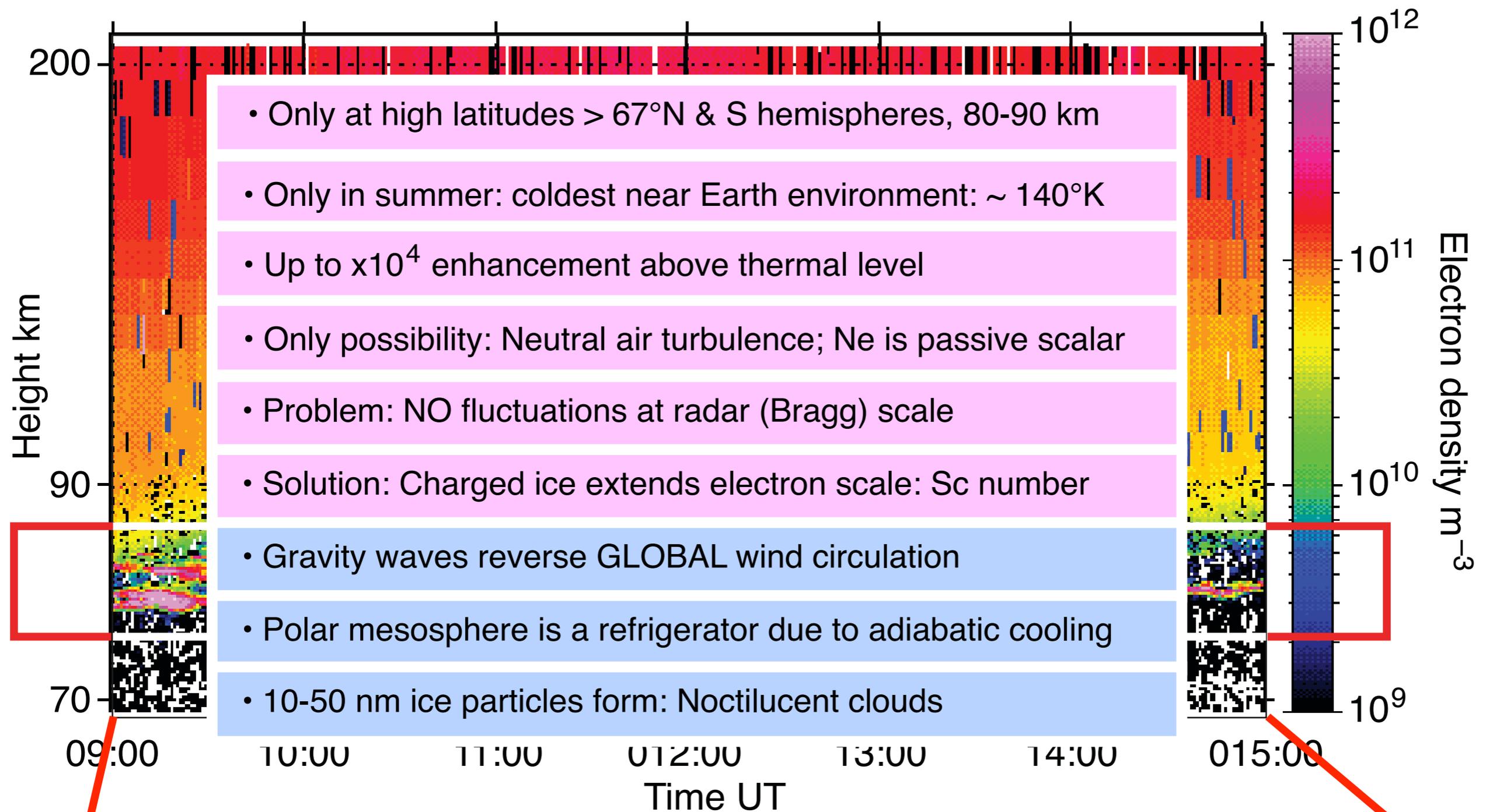
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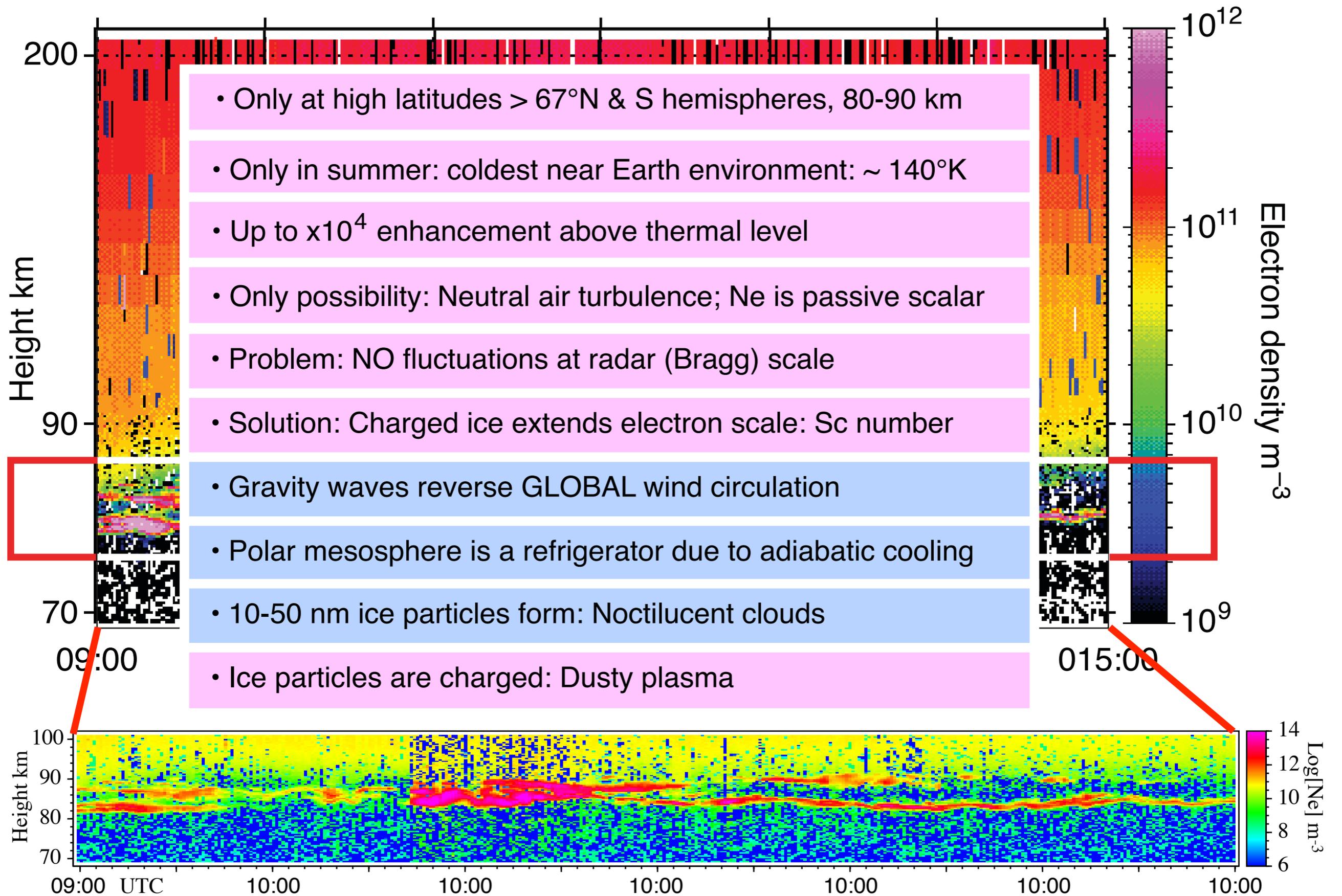
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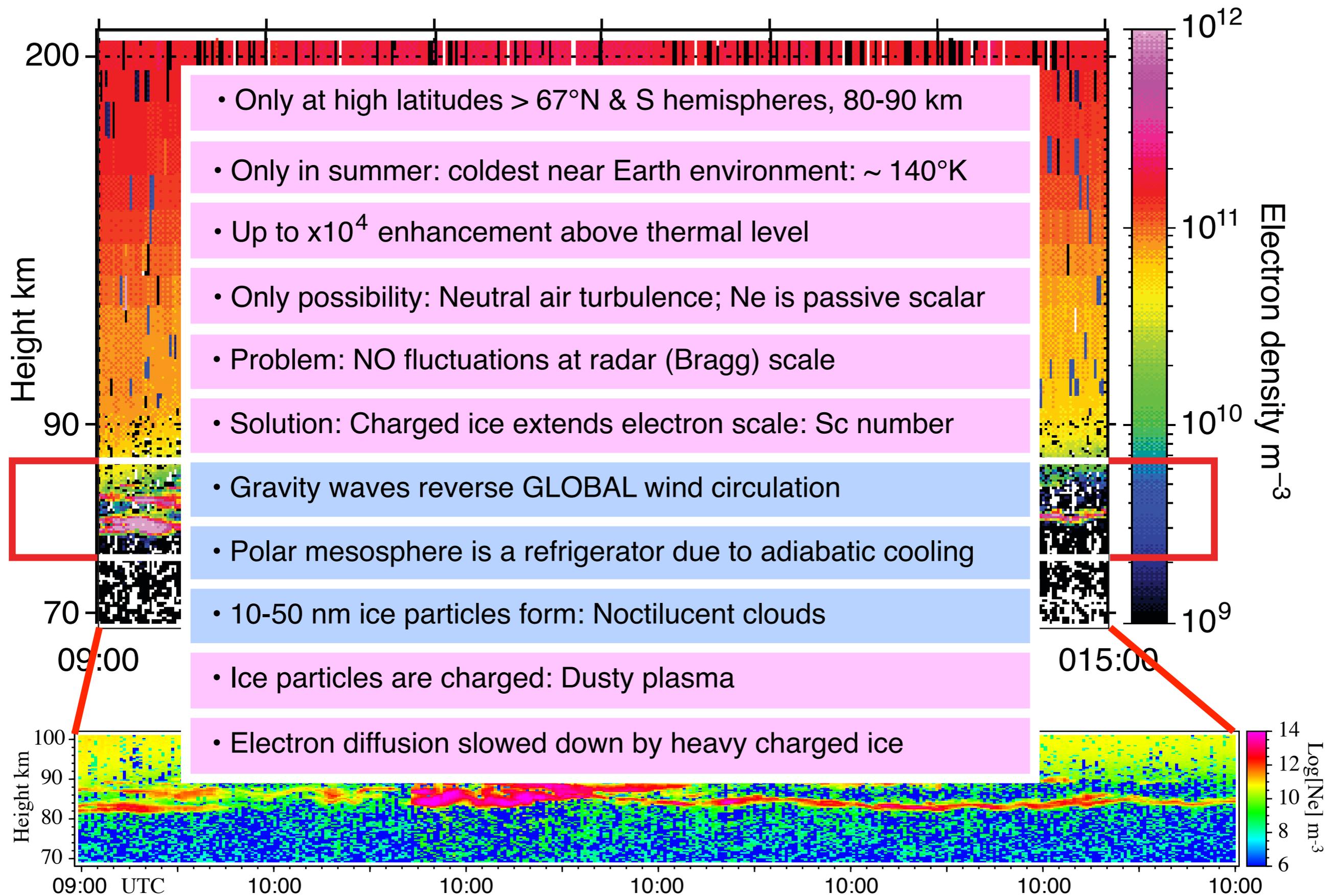
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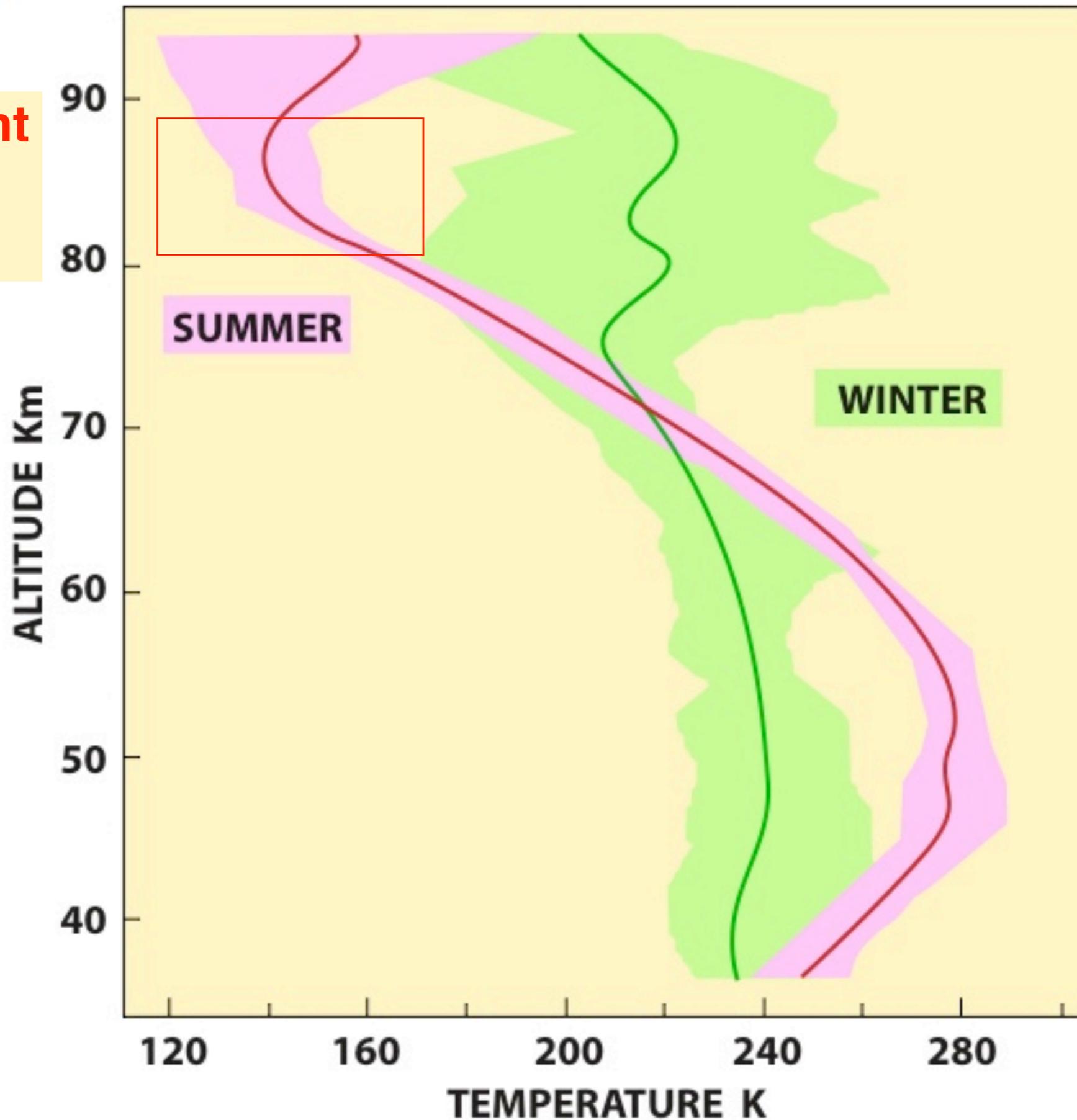
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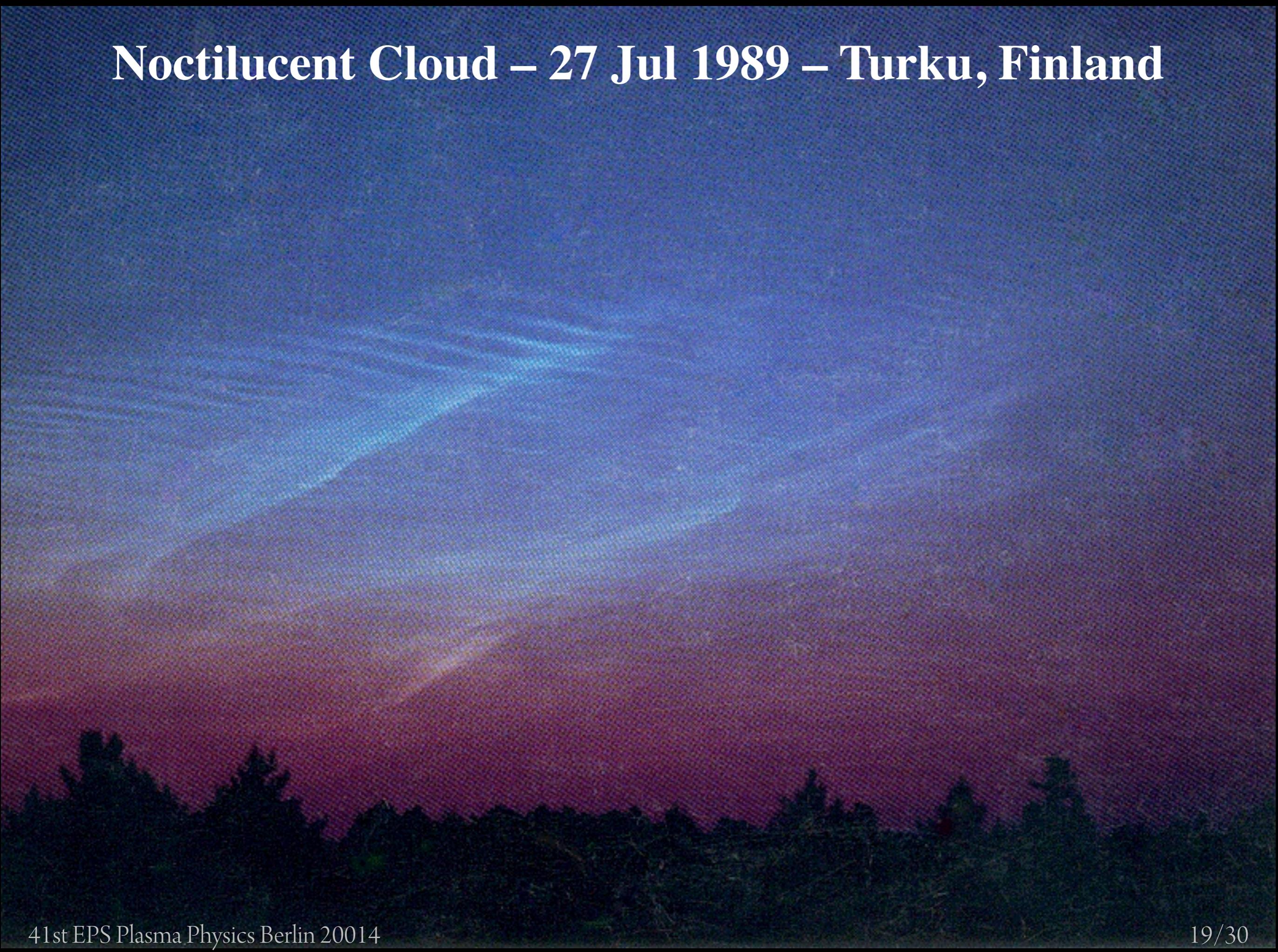
# Seasonal Temperatures – Alaska, 71° N

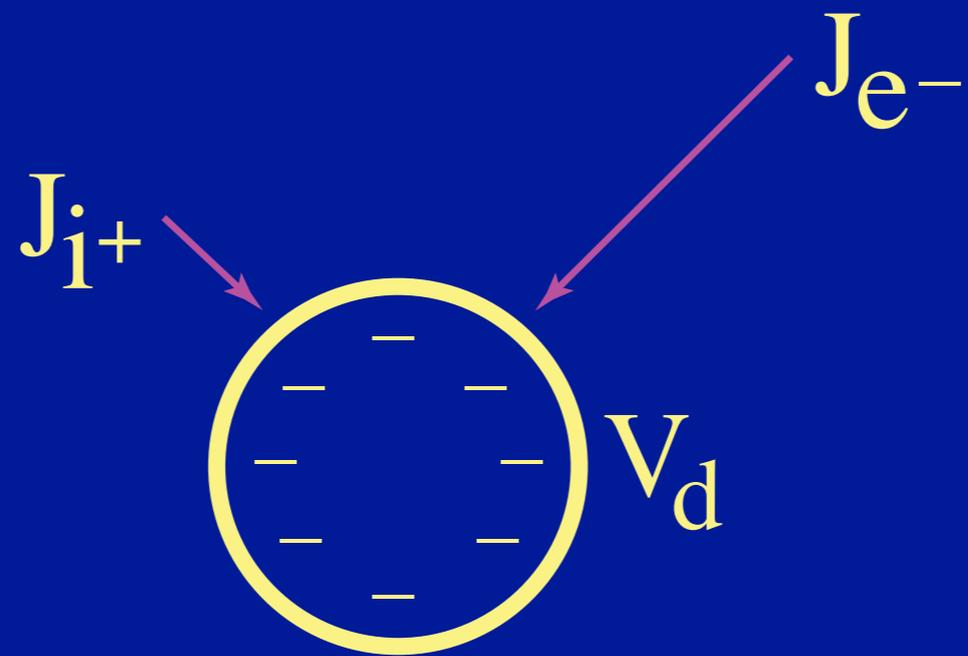
Noctilucent  
Clouds  
& PMSE



Small Ice  
Particles

# Noctilucent Cloud – 27 Jul 1989 – Turku, Finland



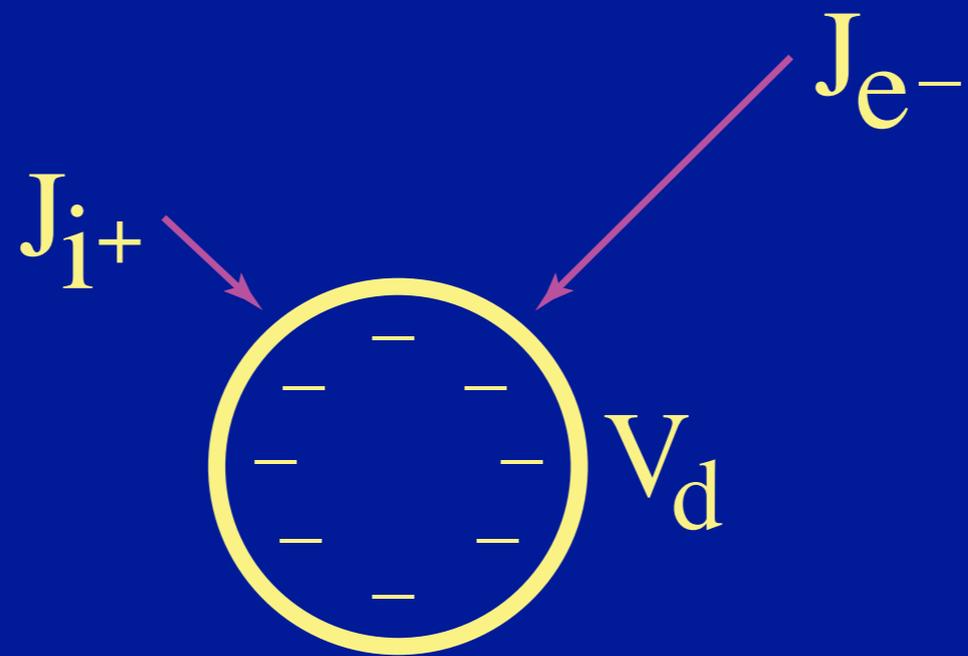


$$J = n v_{\text{thermal}} \quad v_e \gg v_i \quad J_e \gg J_i$$

$$n_e = n_i$$

$$J_{i+} + J_{e-} = 0 \Rightarrow V_d \neq 0$$

The mesosphere has free electrons and ions:  
 thermal current equilibrium results in negative charge on the dust particles



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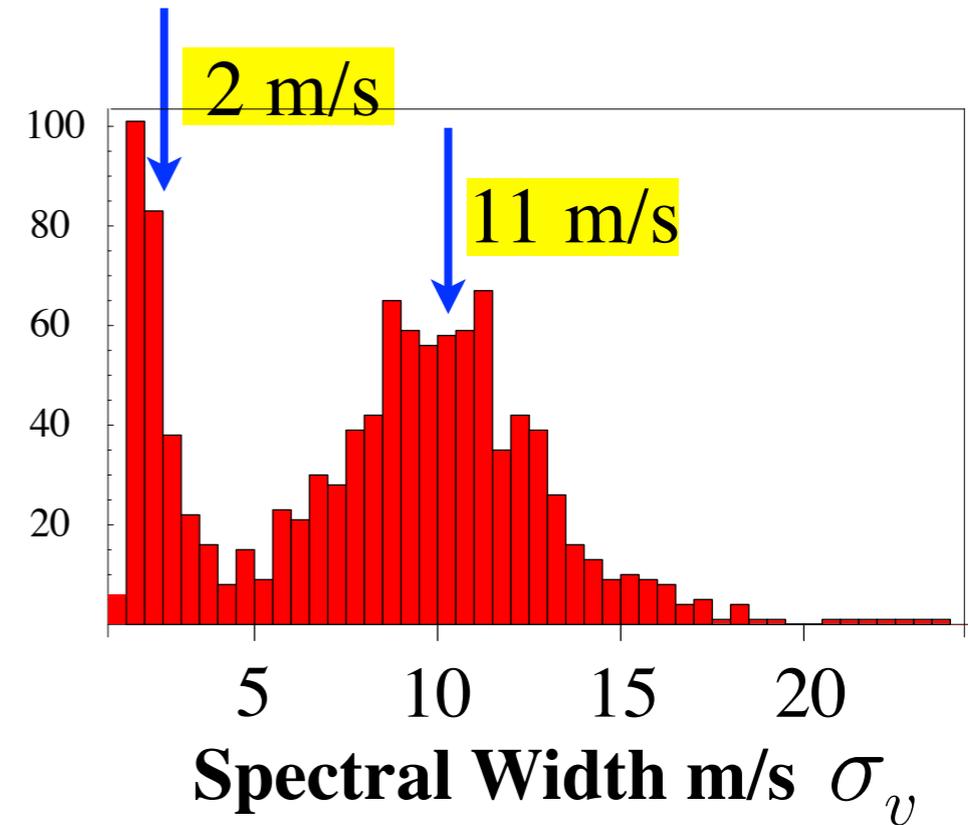
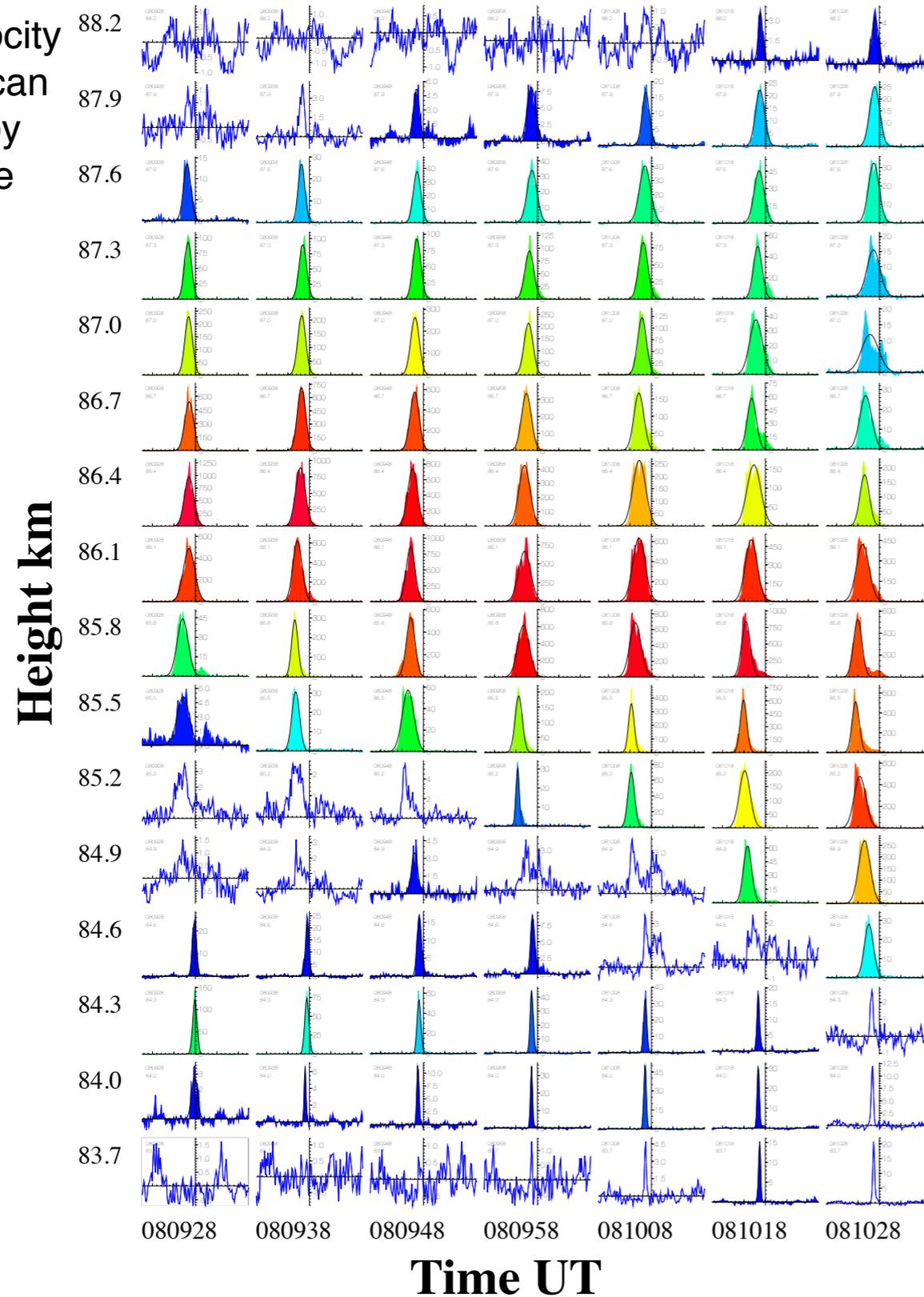
The mesosphere has free electrons and ions:  
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**Electrons diffuse with the mass of the dust due to Coulomb force**

# PMSE Doppler spectra: velocity variance

EISCAT VHF 13 July 2004

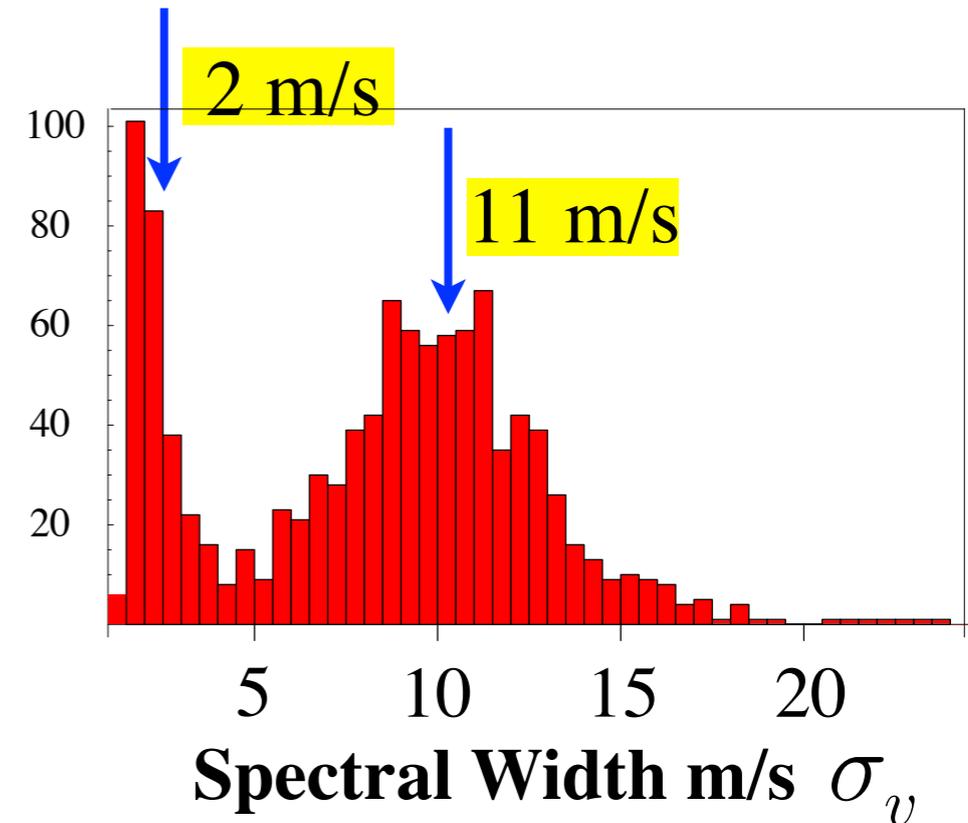
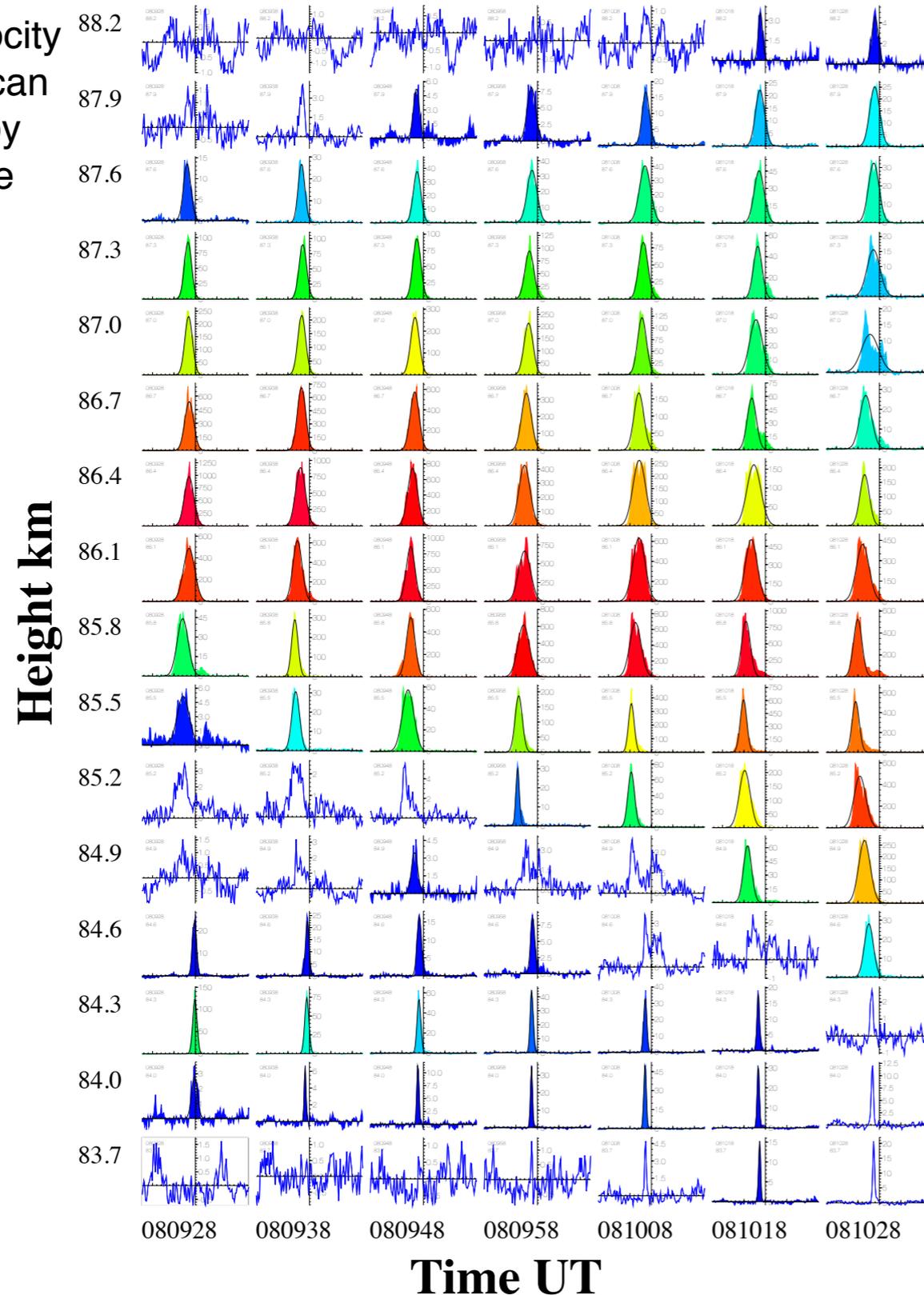
Electron velocity fluctuations can be induced by air turbulence



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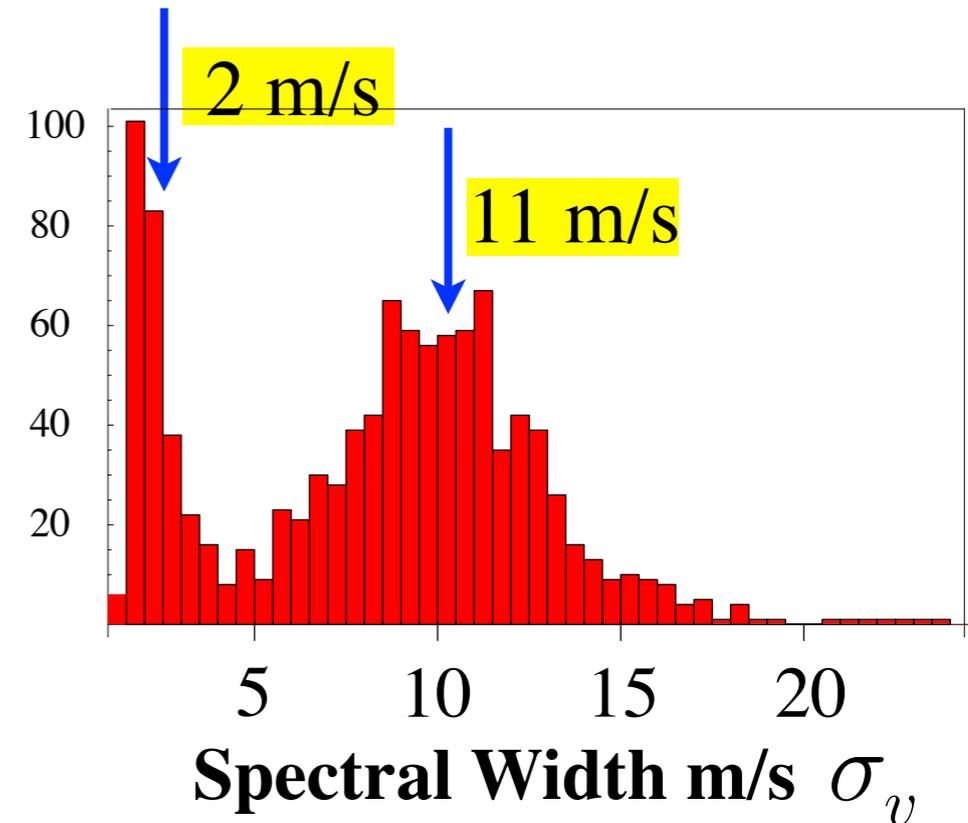
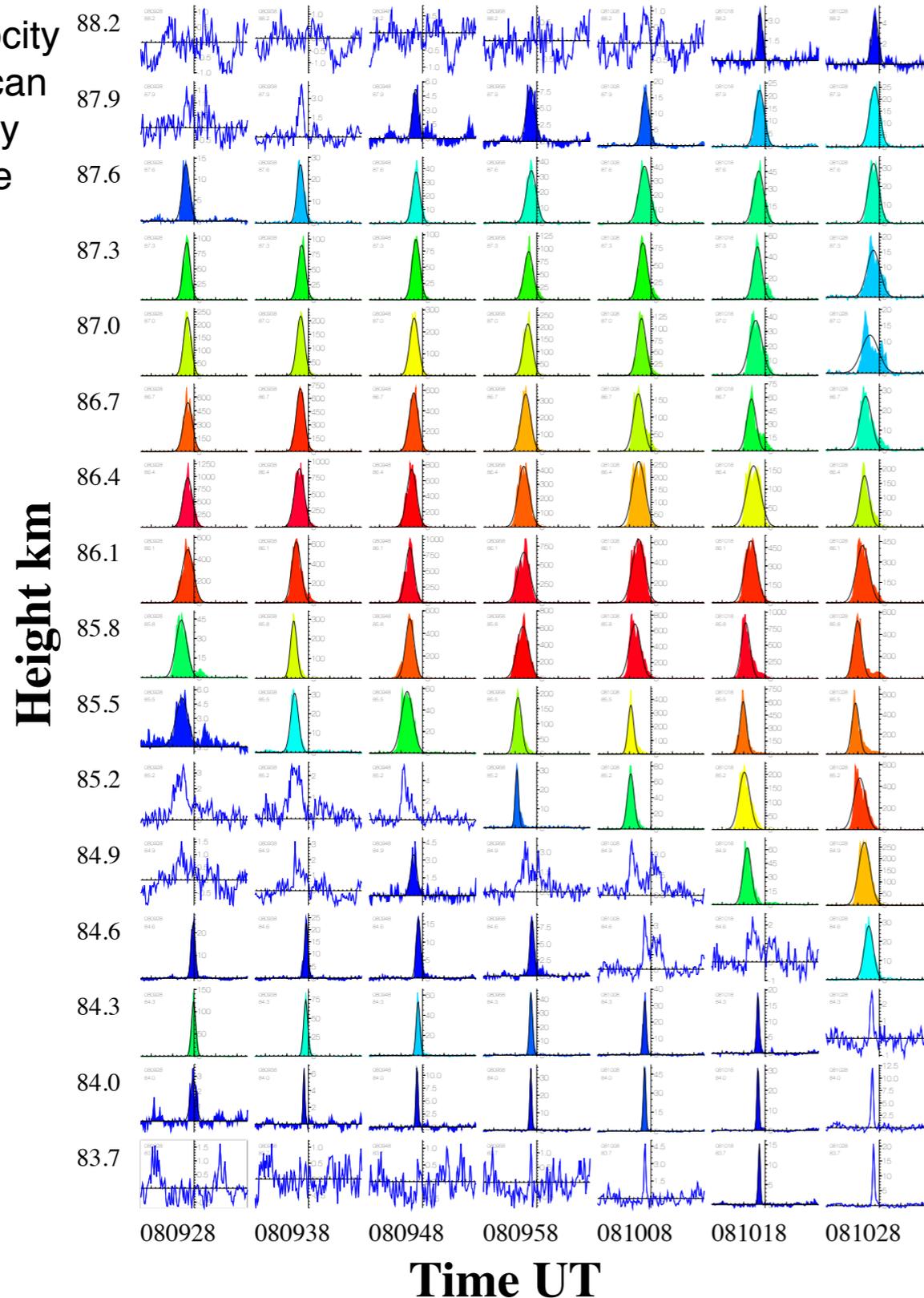
Energy Dissipation Rate of Turbulence

$$\epsilon = \alpha \sigma_v^2$$

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EISCAT VHF 13 July 2004

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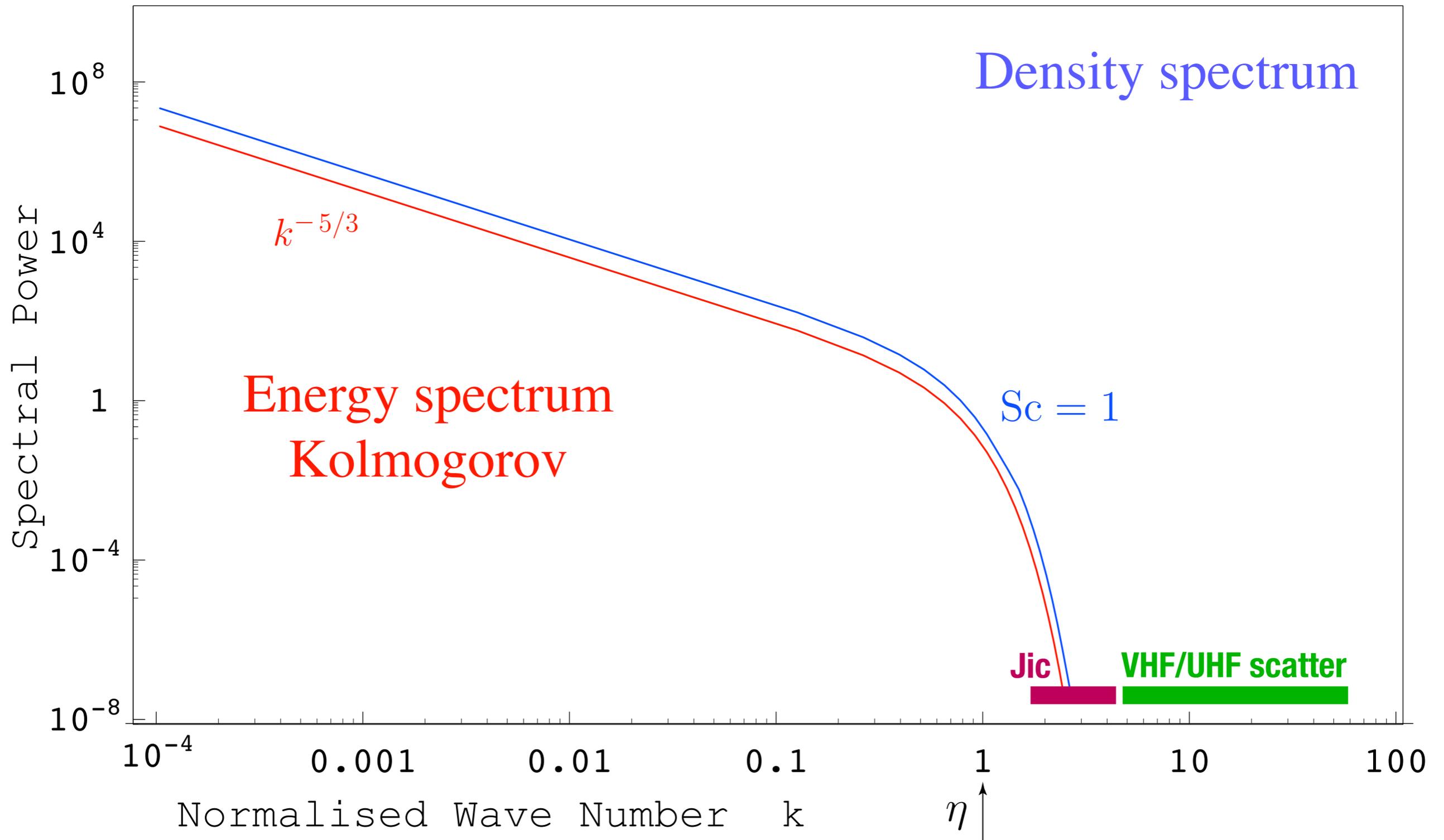
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Kolmogorov turbulence spectrum

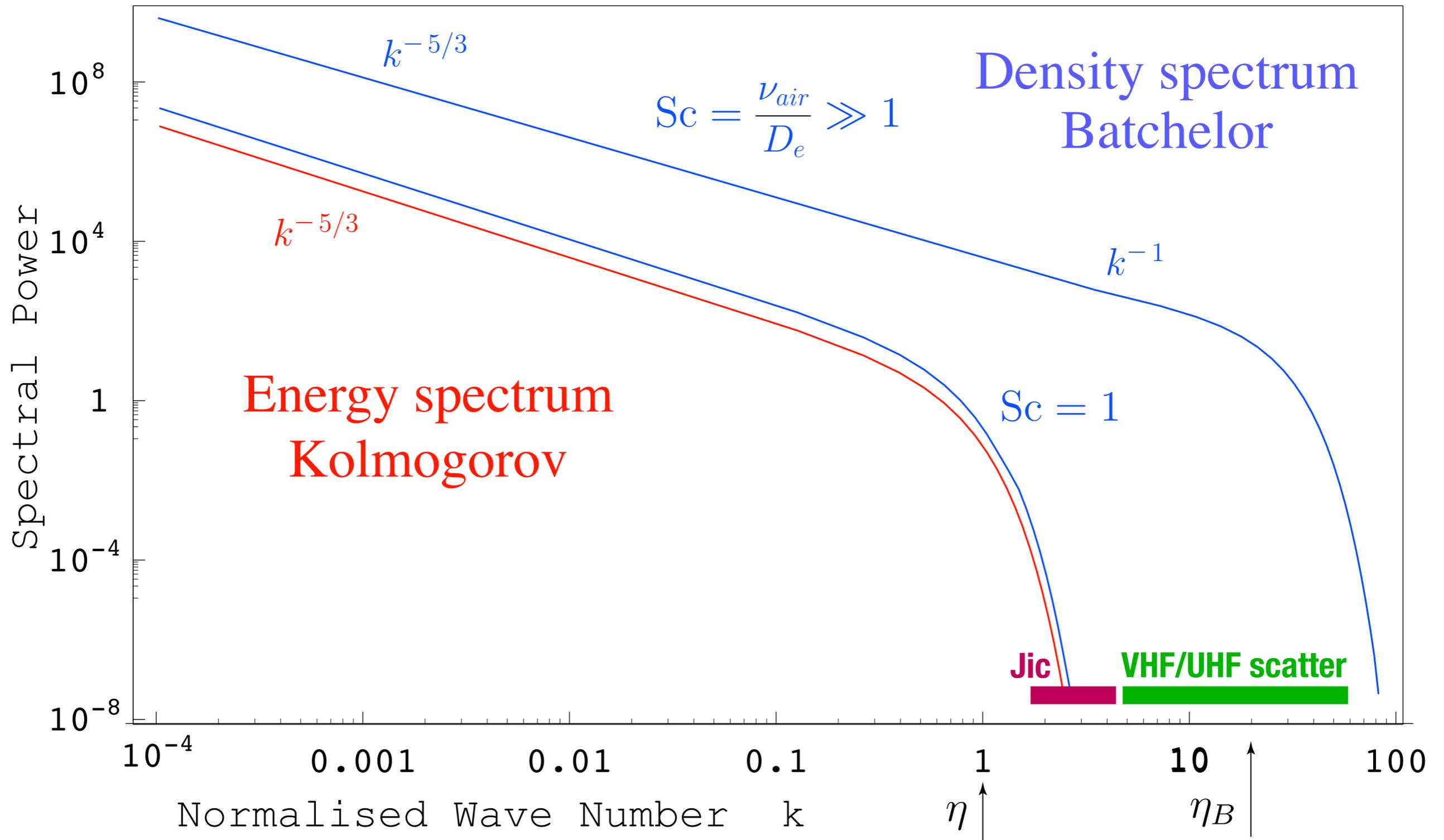
# Possible scattering with enhanced Schmidt number

Kolmogorov scale  $\eta = \left(\frac{\nu_a^3}{\epsilon}\right)^{1/4}$        $Sc = \frac{\nu_a}{D_e}$



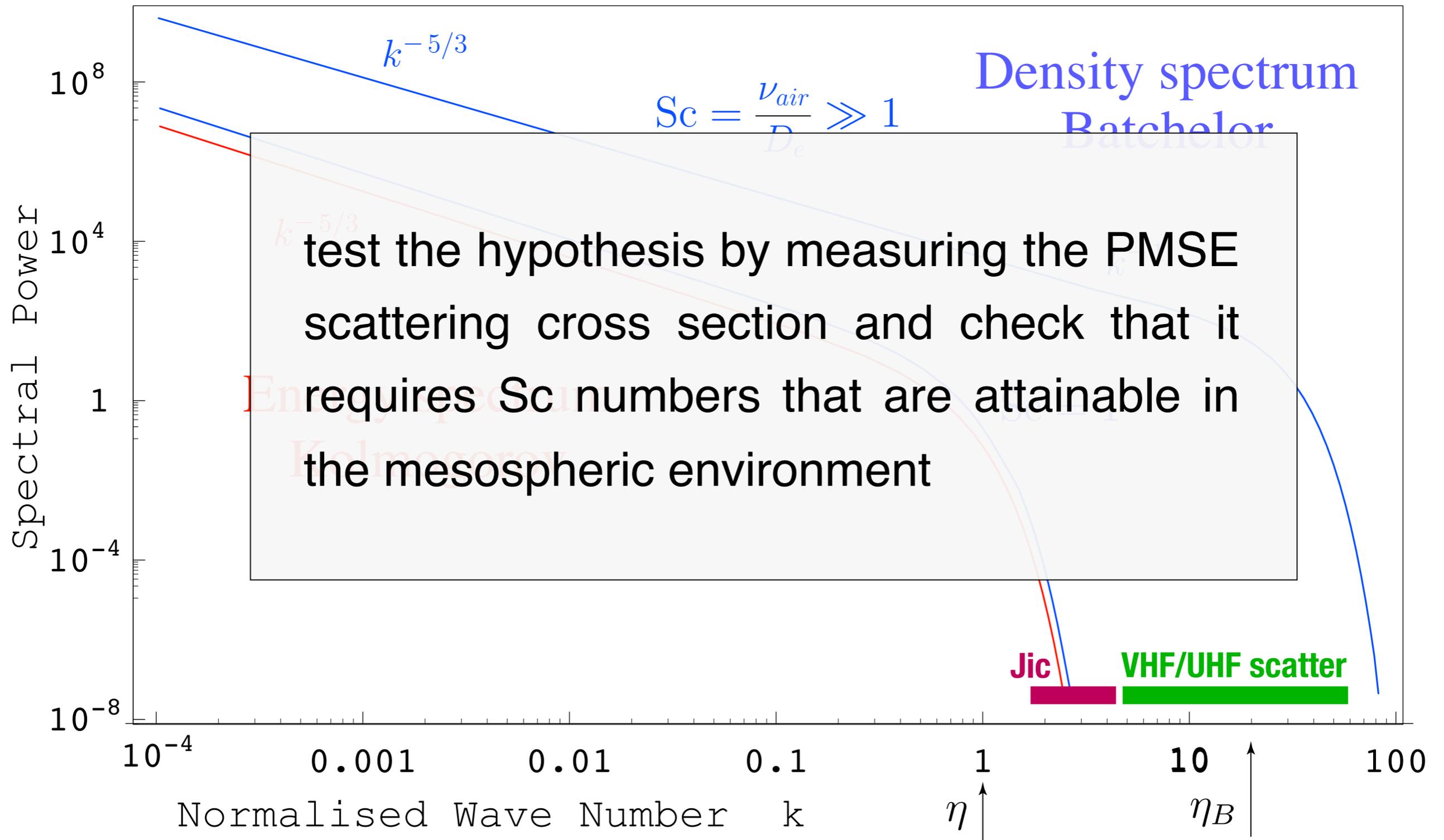
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# Possible scattering with enhanced Schmidt number

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 $Sc = \frac{\nu_a}{D_e}$ 
 $\eta_B = \left(\frac{\nu_a D_e^2}{\epsilon}\right)^{1/4}$  Batchelor scale



# Scattering cross section with Sc number

Measured:

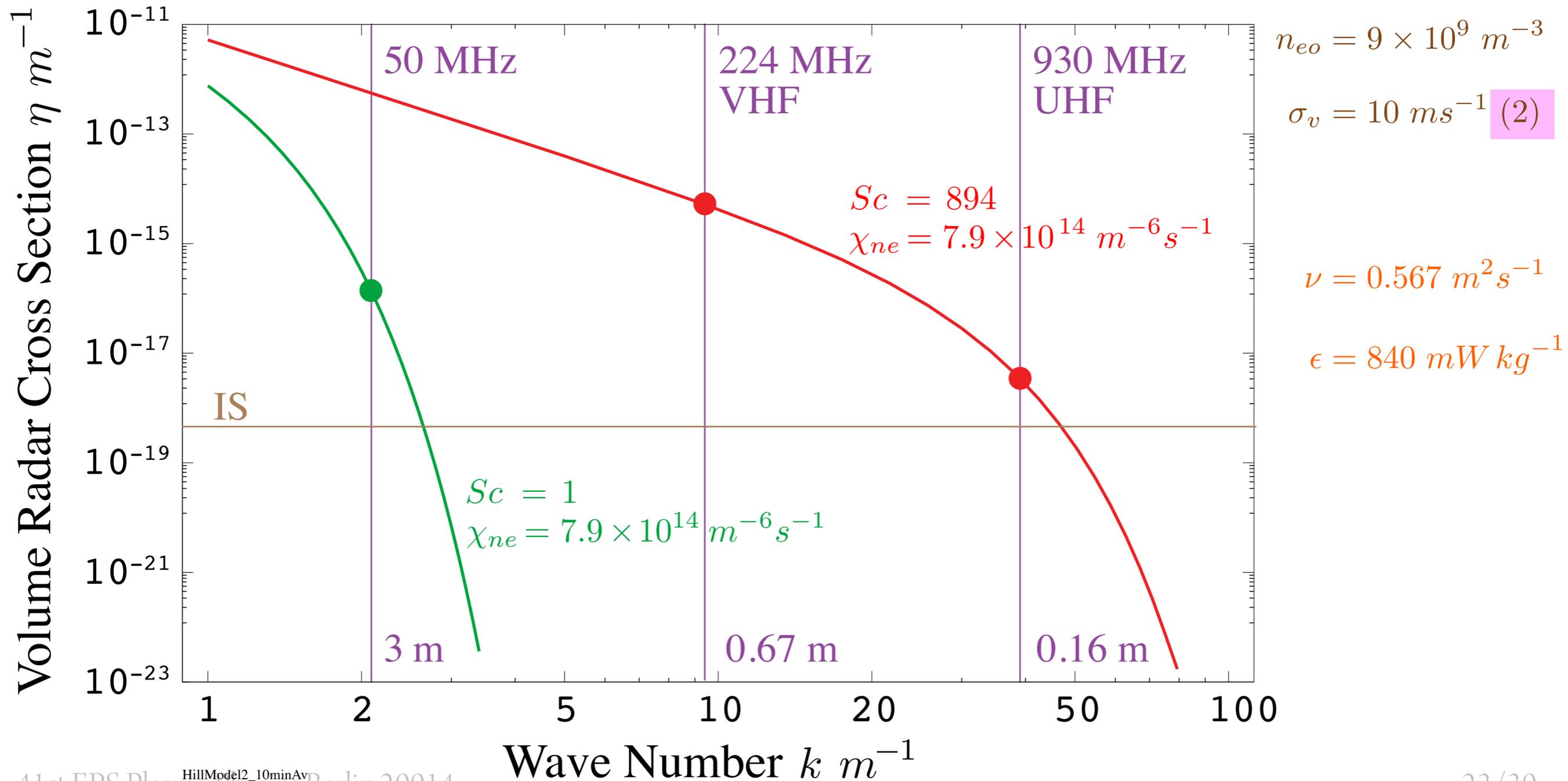
$$\eta_{rad}(\text{VHF}) = 5250 \times 10^{-18} \text{ m}^{-1}$$

$$\eta_{rad}(\text{UHF}) = 3.5 \times 10^{-18}$$

Fitted:

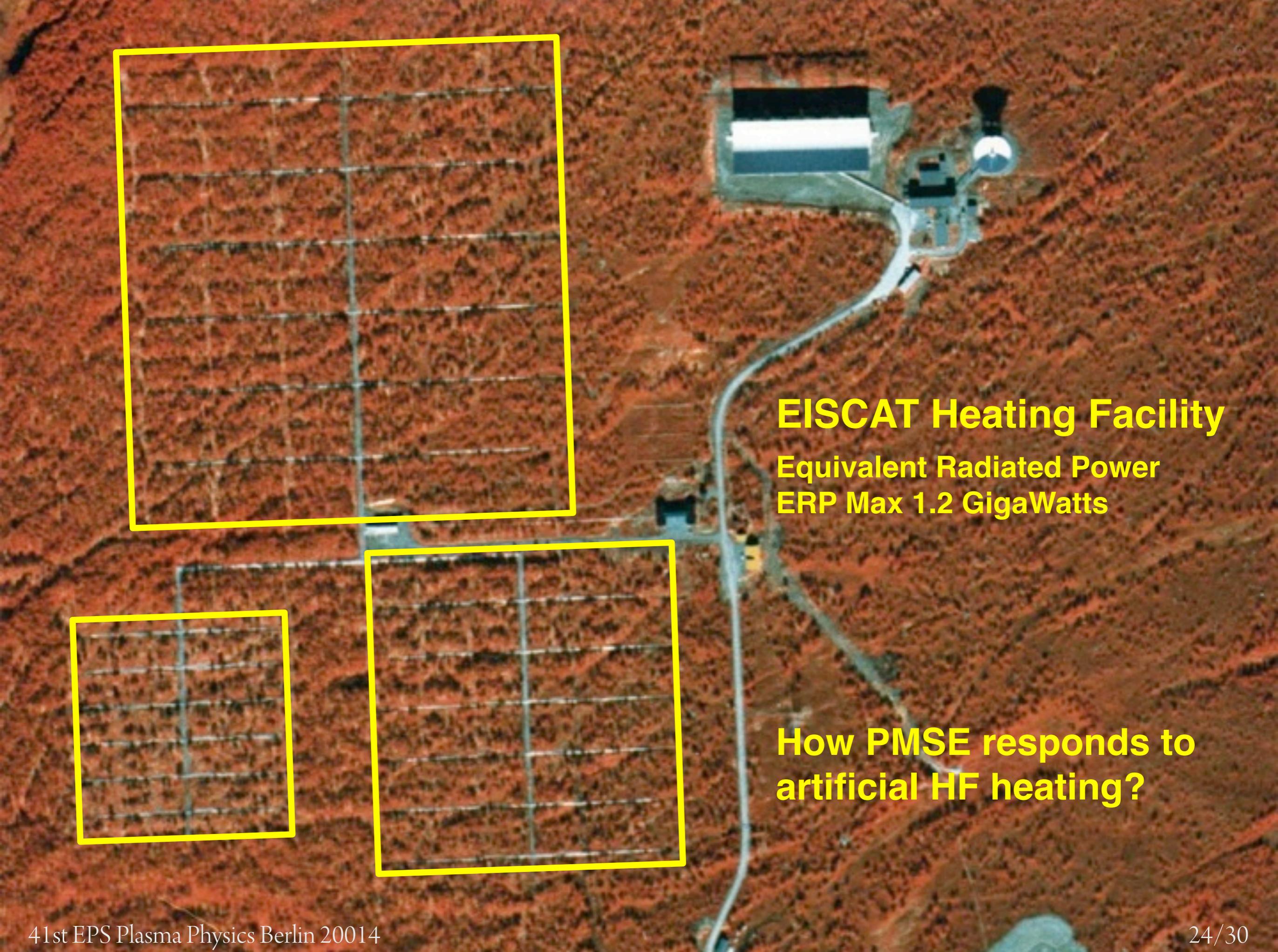
$$Sc = 894 \text{ (4470)}$$

$$\chi_{ne} = 7.9 \times 10^{14} \text{ m}^{-6} \text{ s}^{-1}$$





**EISCAT Heating Facility**  
Equivalent Radiated Power  
ERP Max 1.2 GigaWatts

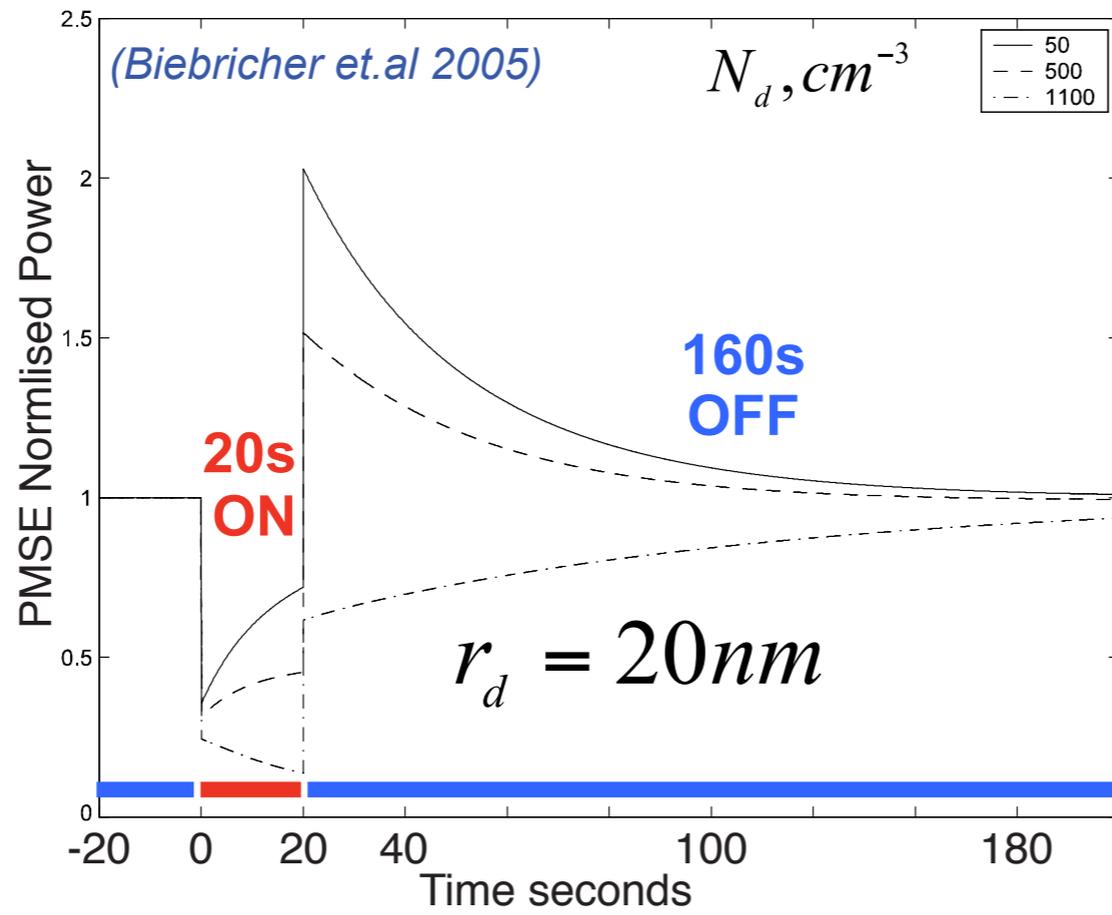


## EISCAT Heating Facility

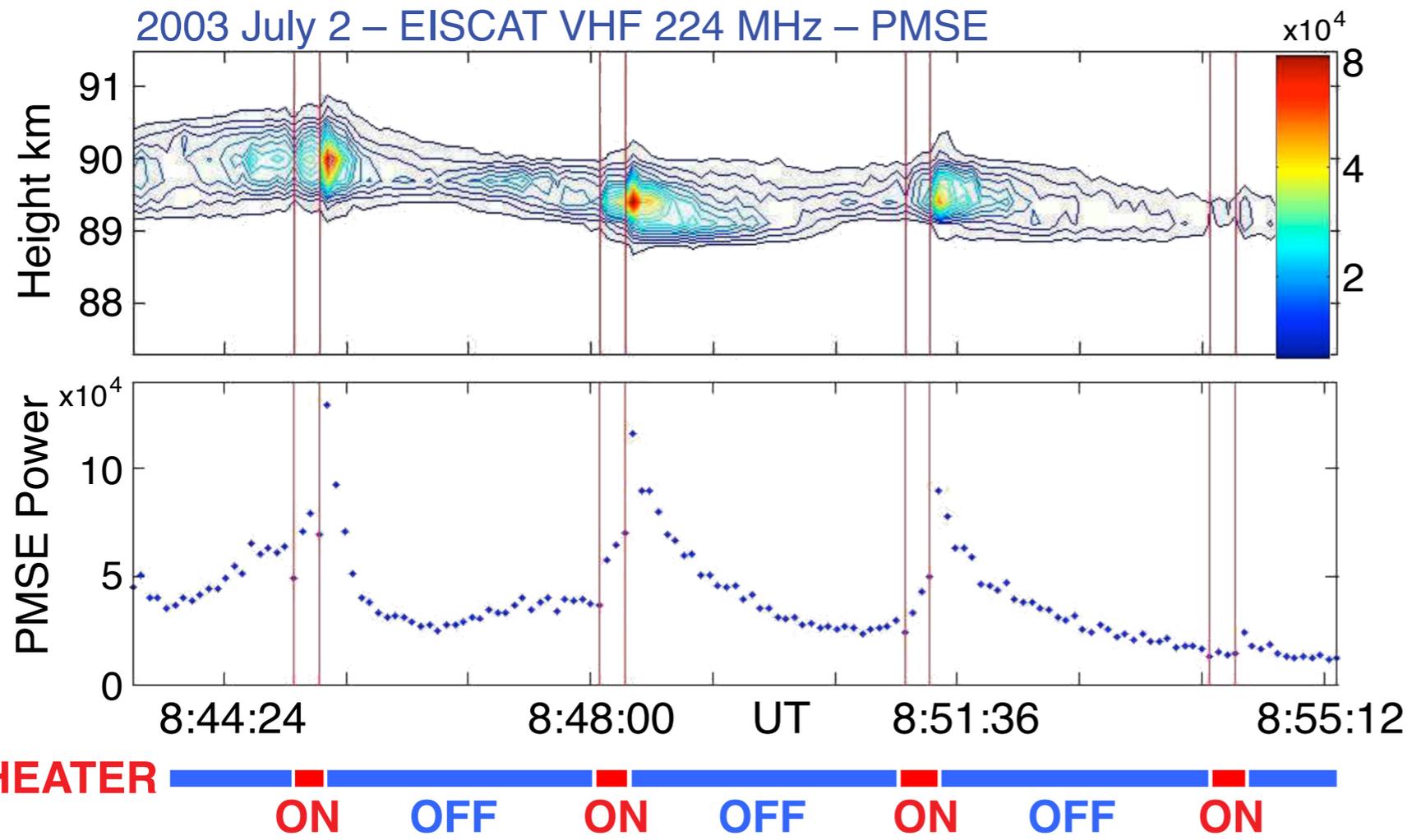
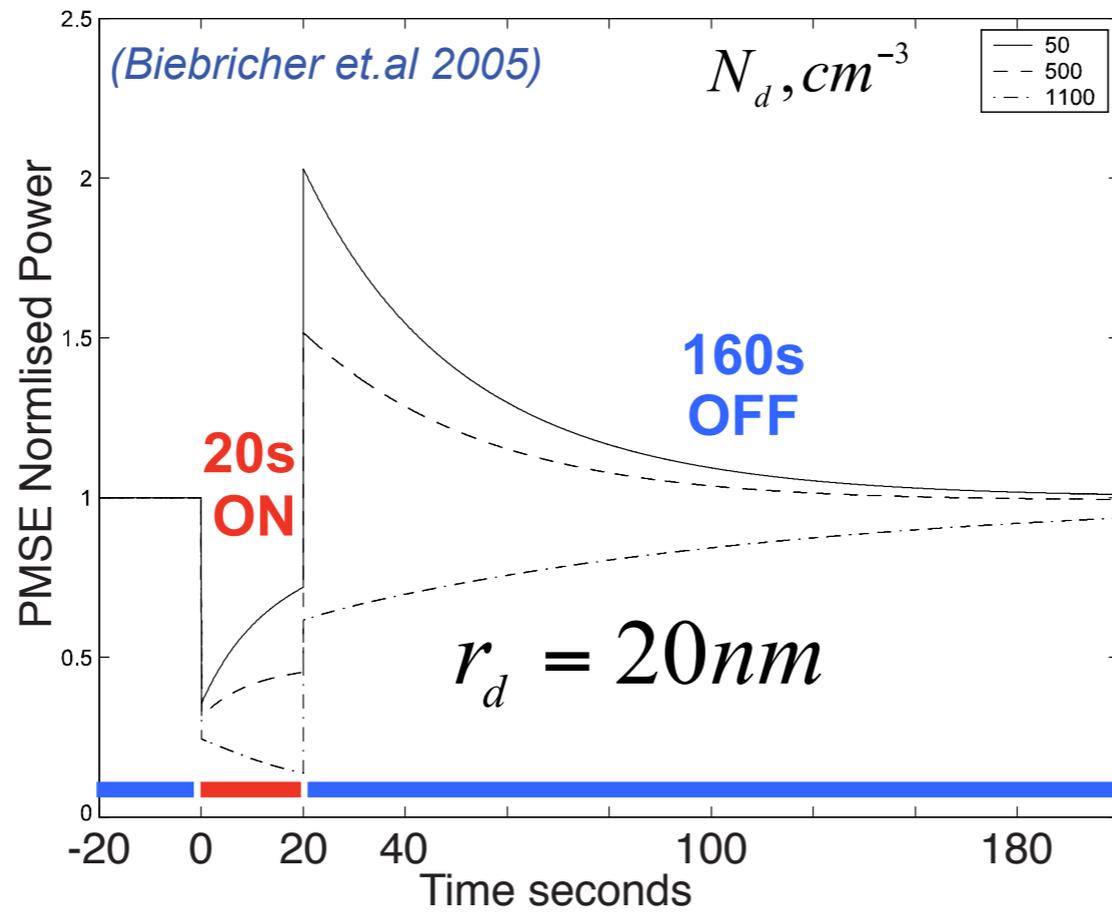
Equivalent Radiated Power  
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How PMSE responds to  
artificial HF heating?

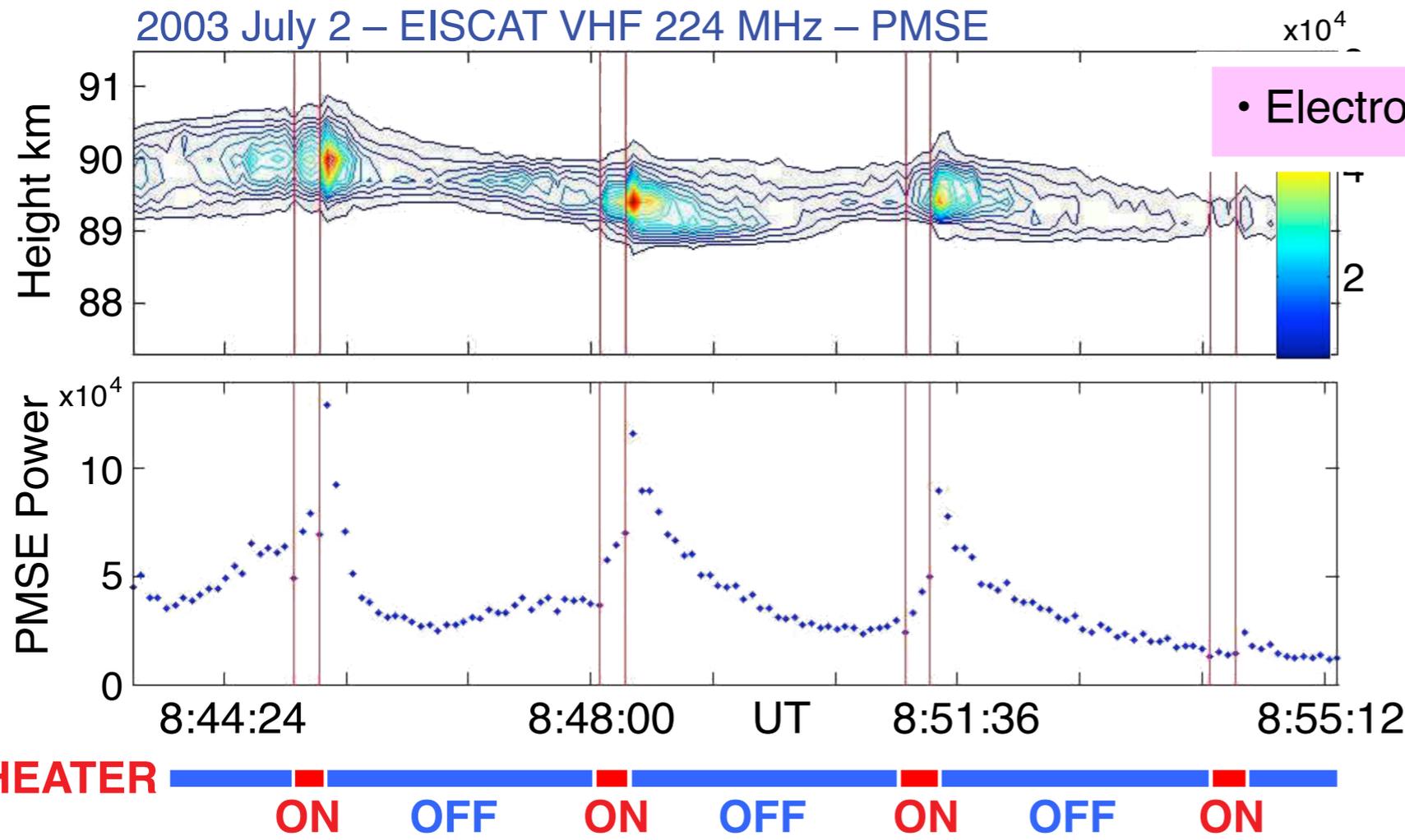
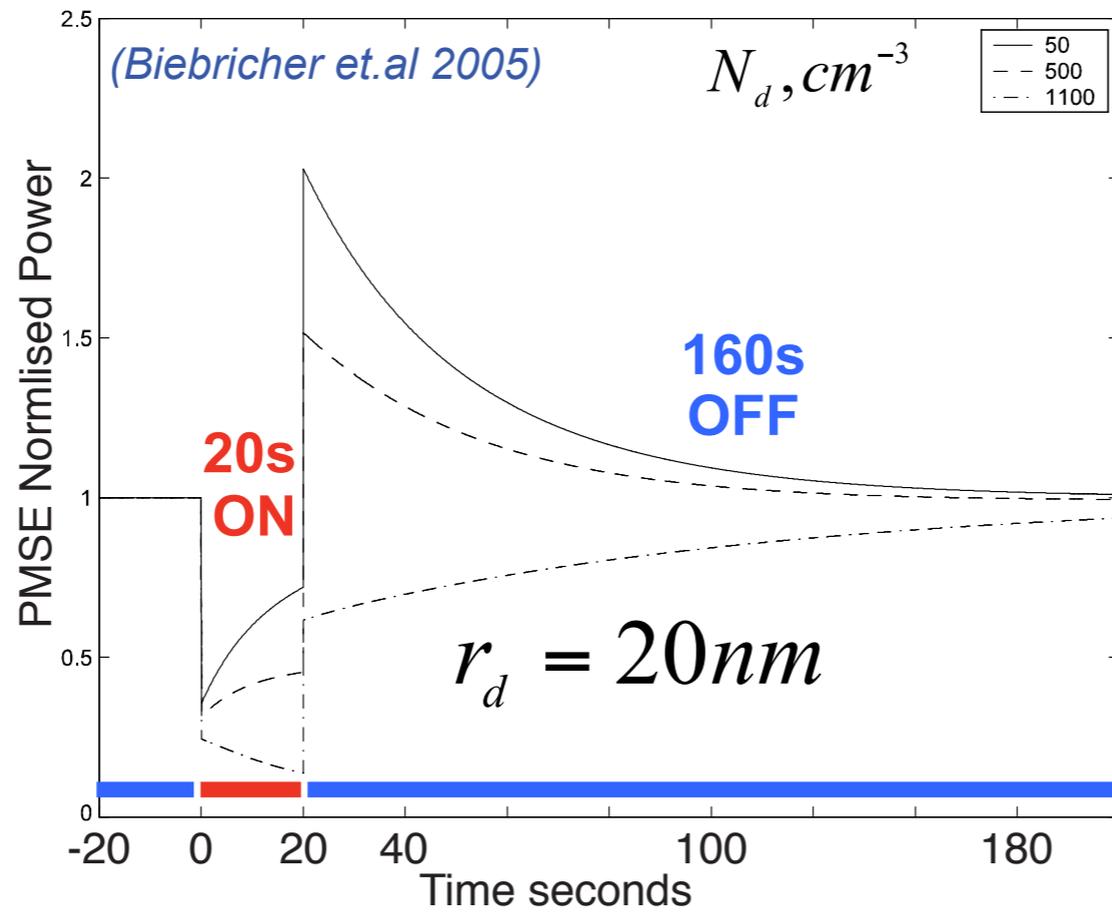
**Ove Havnes (2001)  
predicted the  
Overshoot effect**



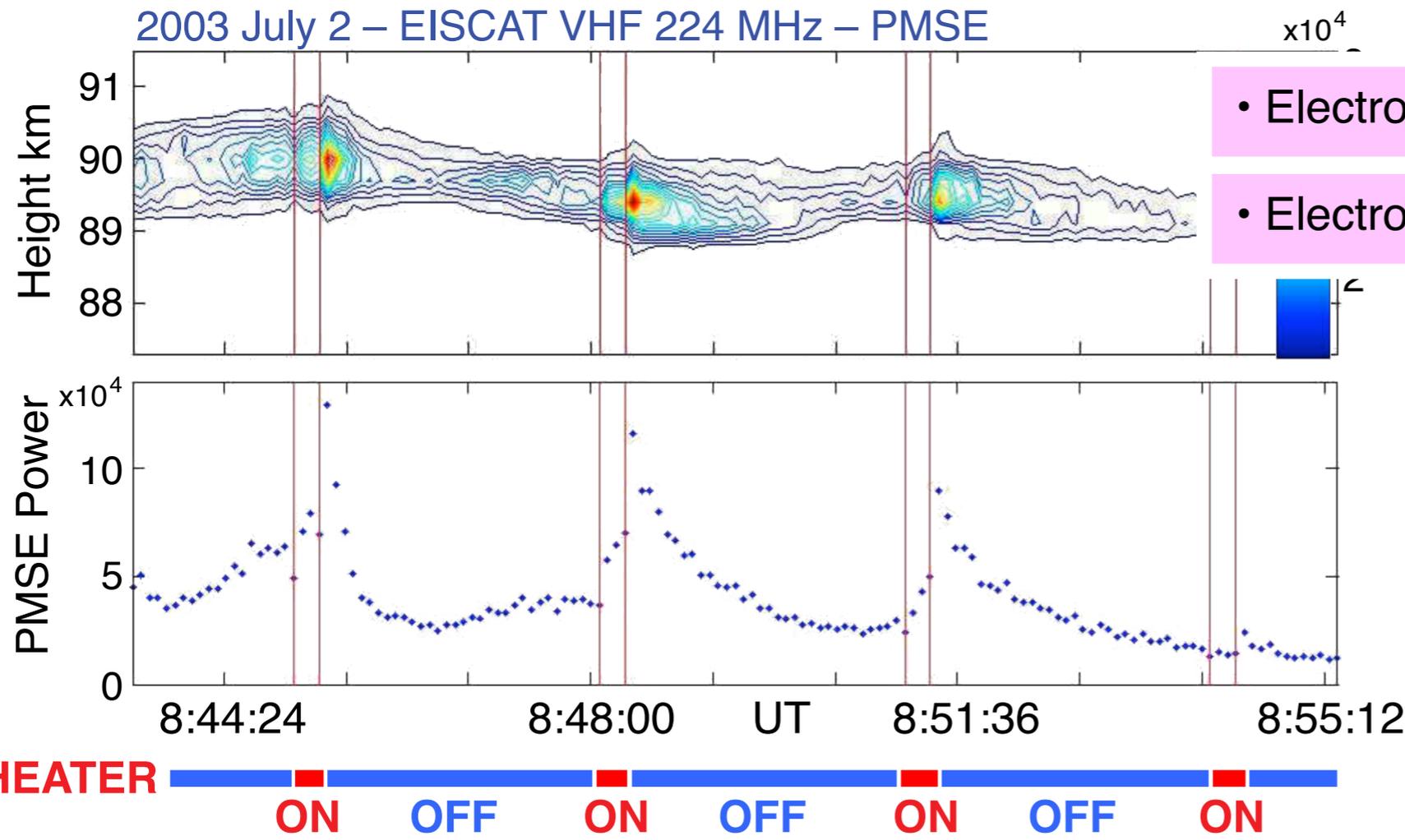
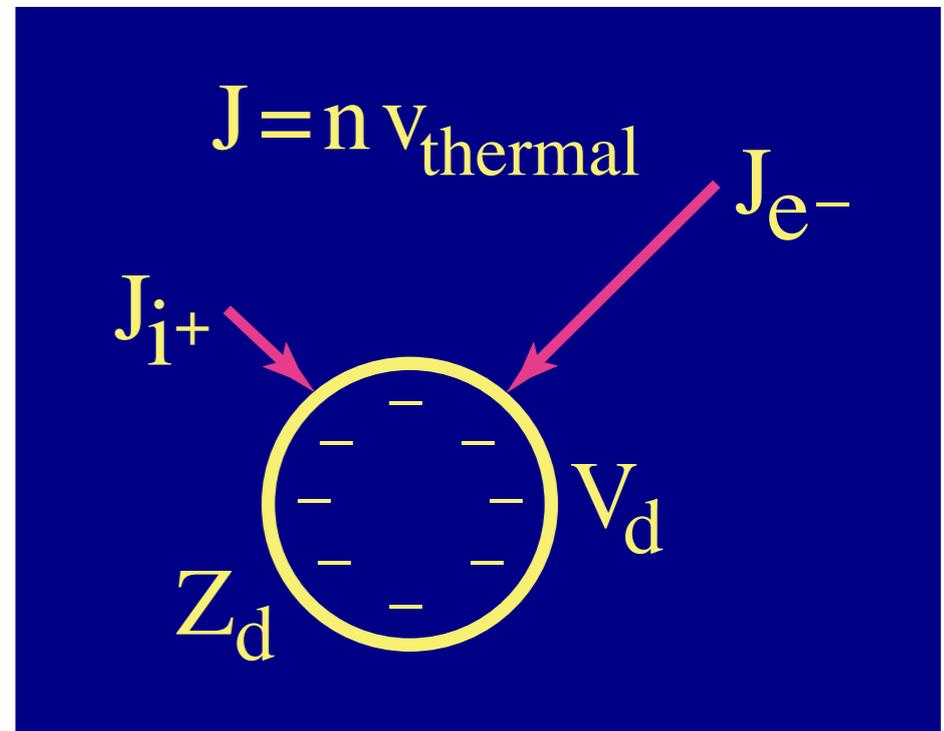
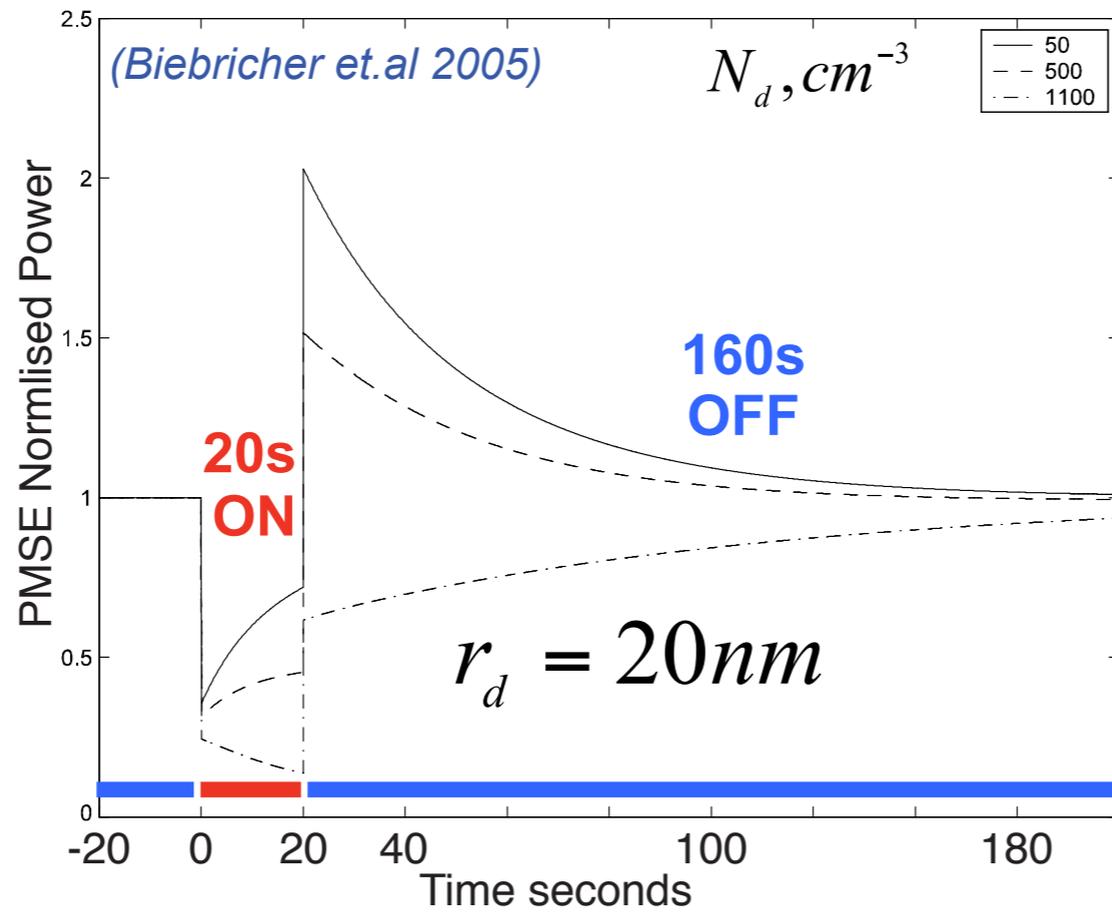
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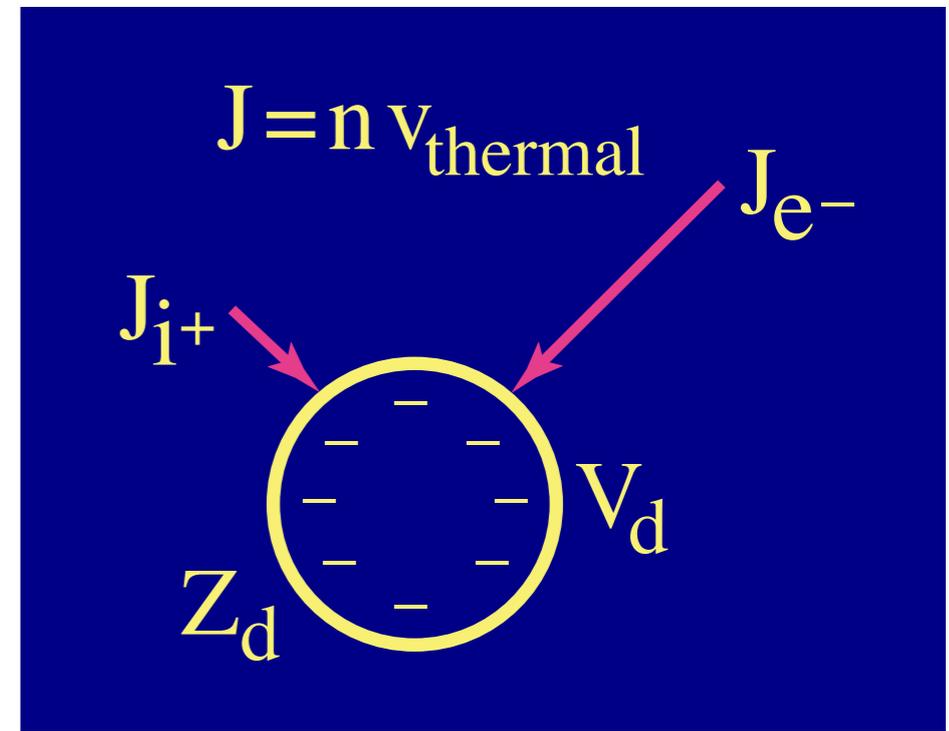
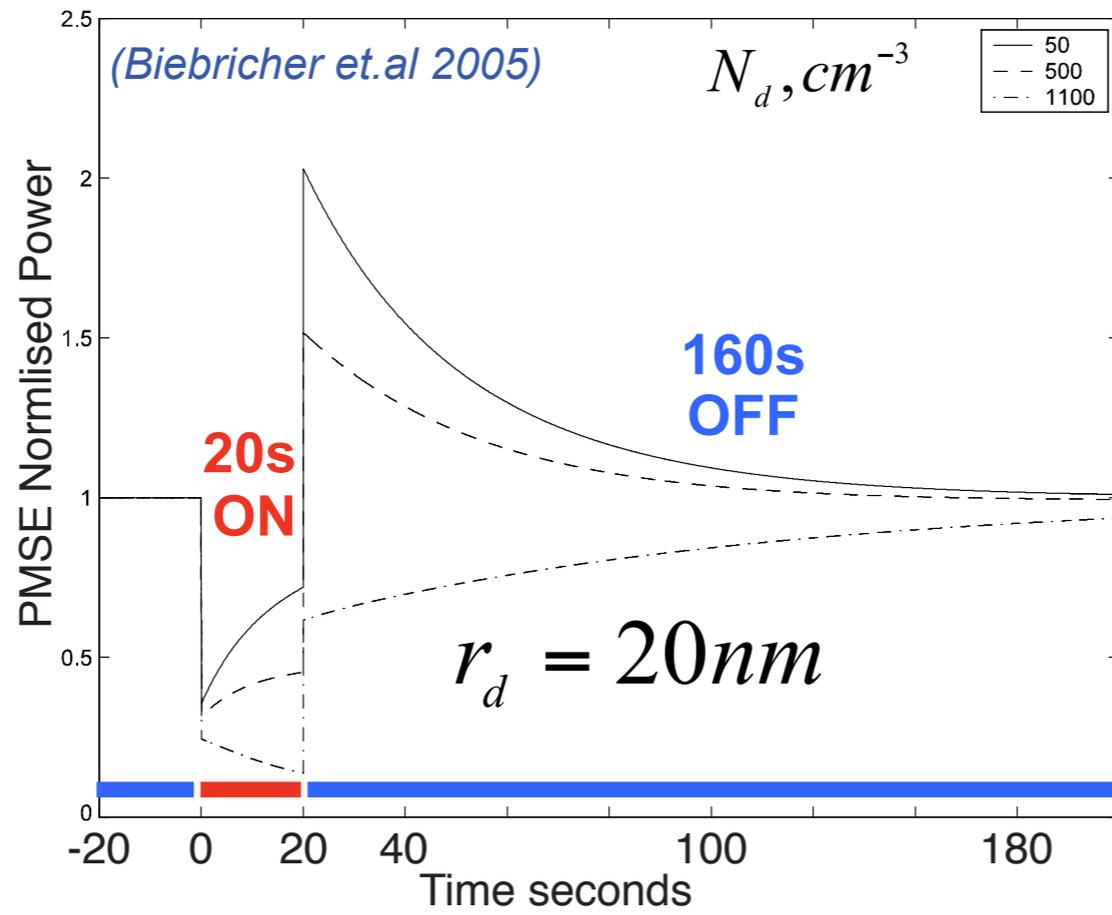


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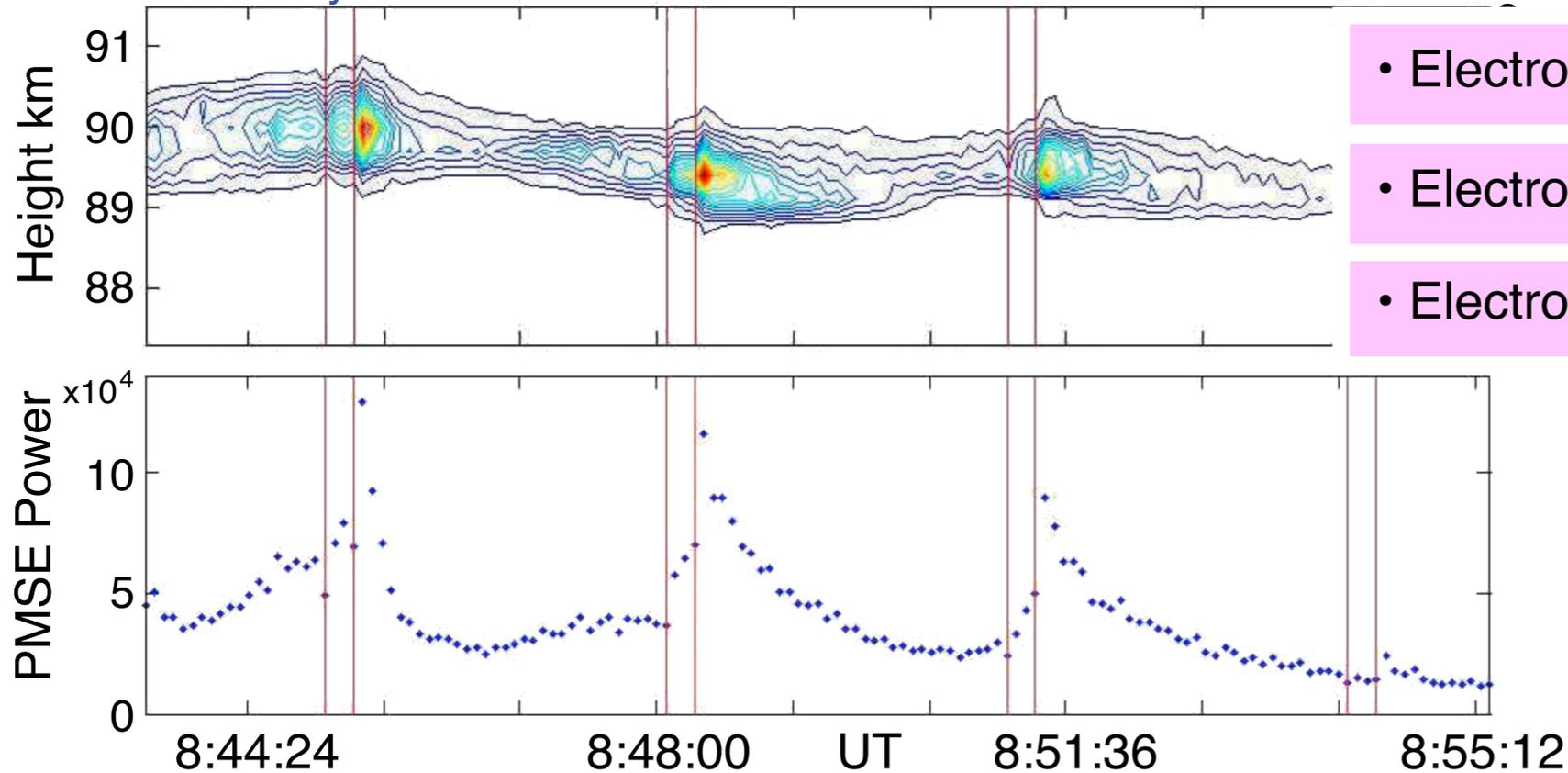


- Electron temperature  $T_e$  increases
- Electron thermal velocity increases

Ove Havnes (2001) predicted the Overshoot effect



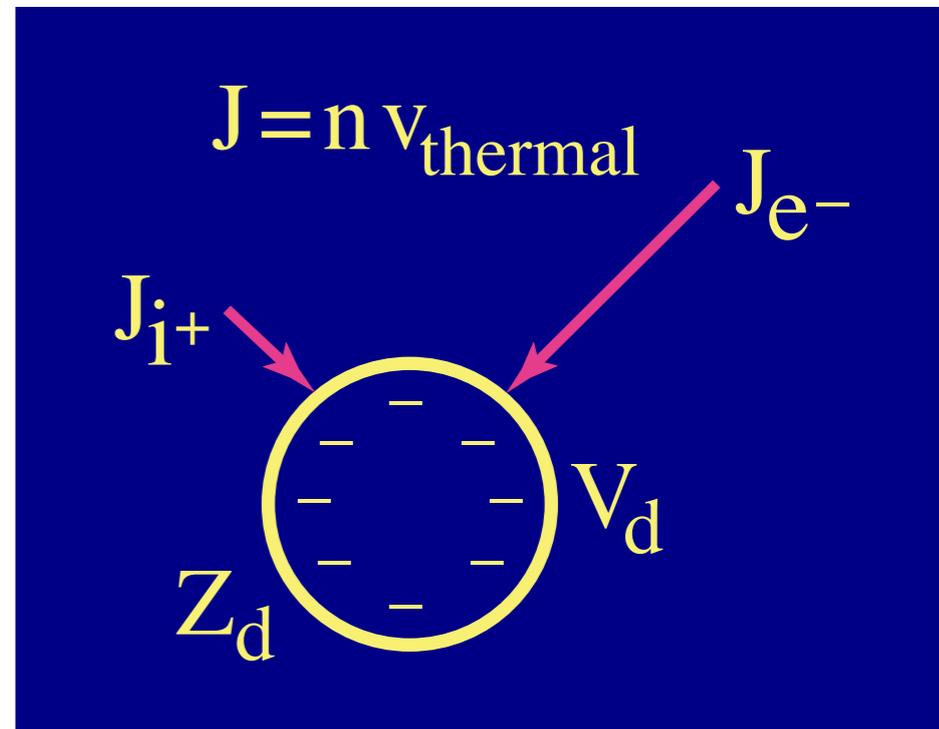
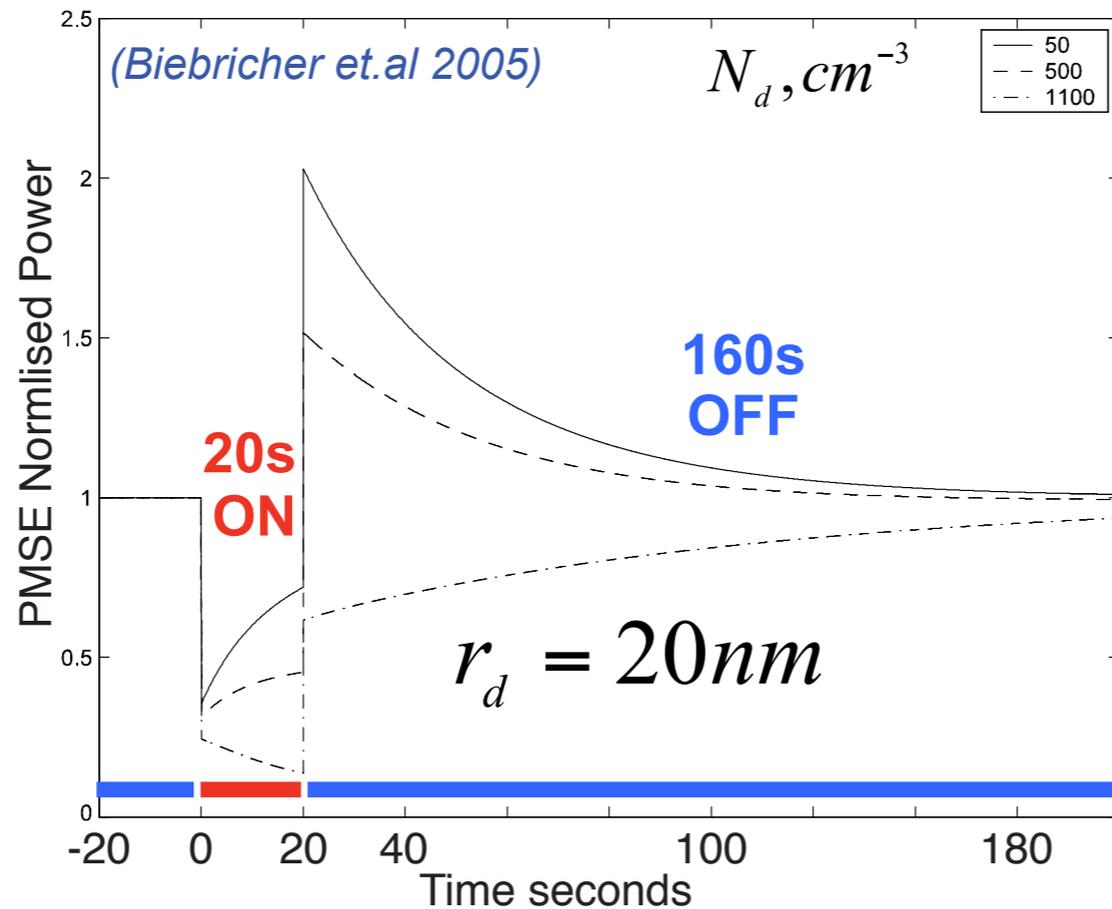
2003 July 2 – EISCAT VHF 224 MHz – PMSE



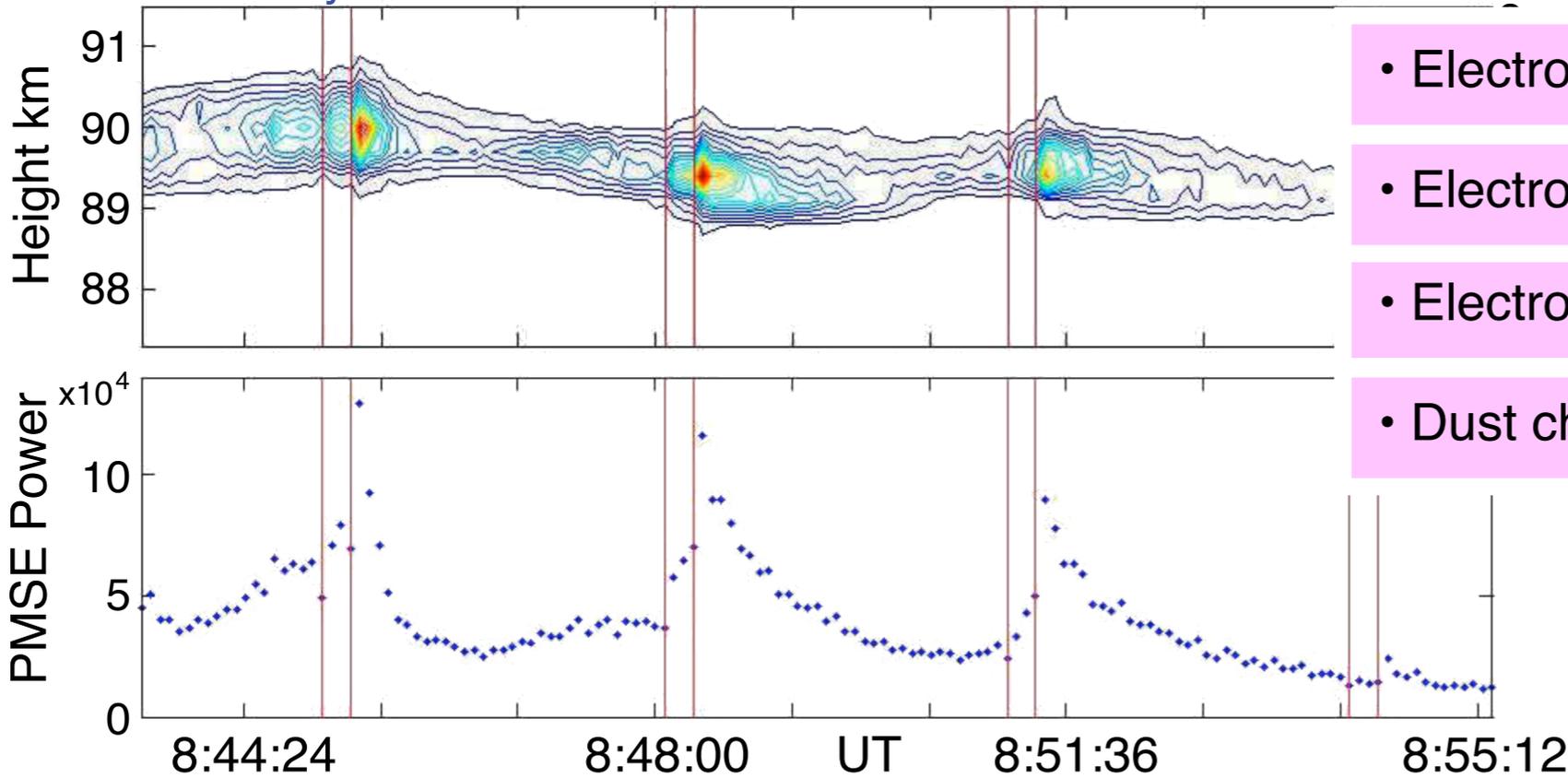
- Electron temperature  $T_e$  increases
- Electron thermal velocity increases
- Electron current density  $J_e$  increases



Ove Havnes (2001) predicted the Overshoot effect



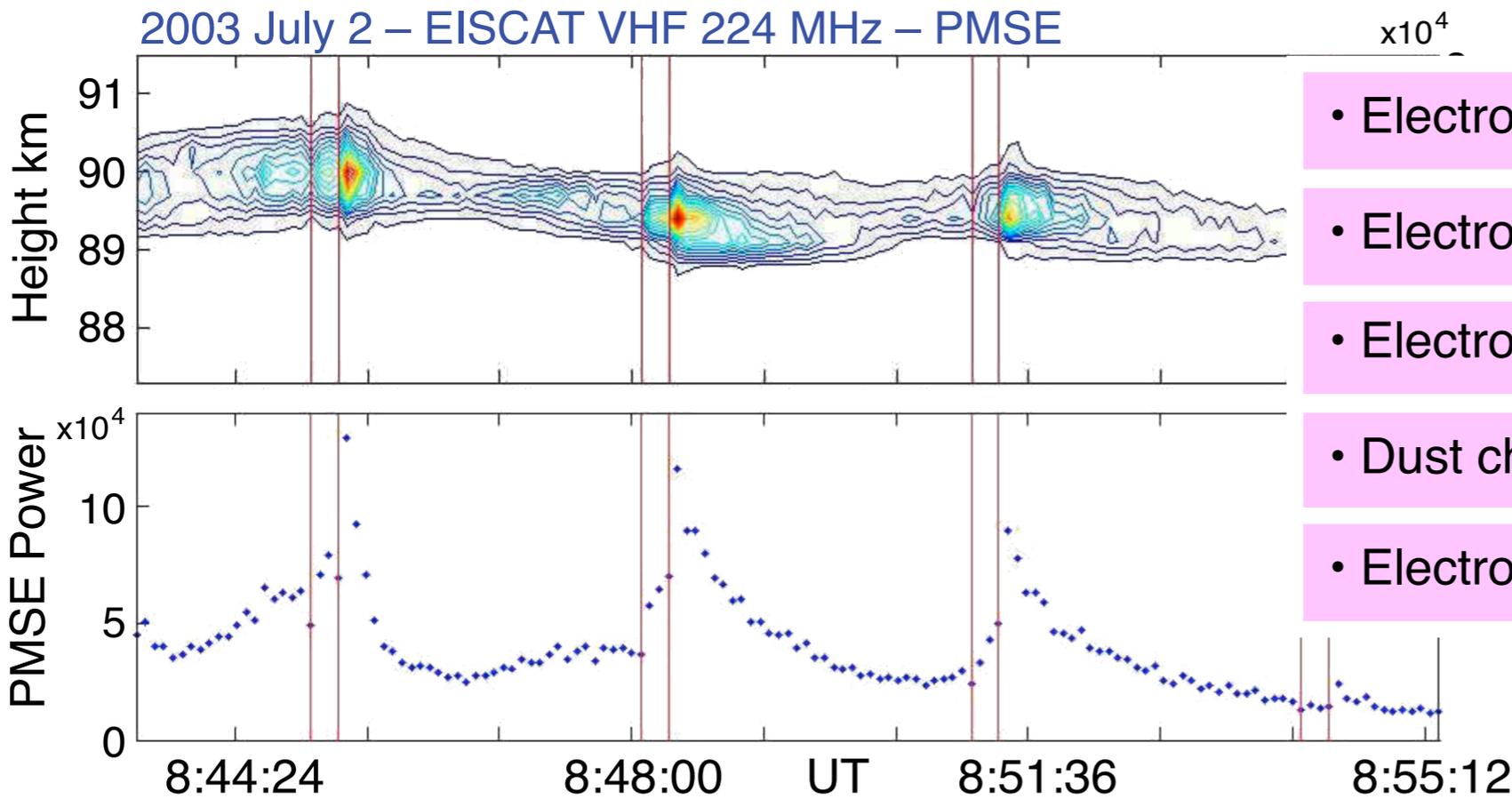
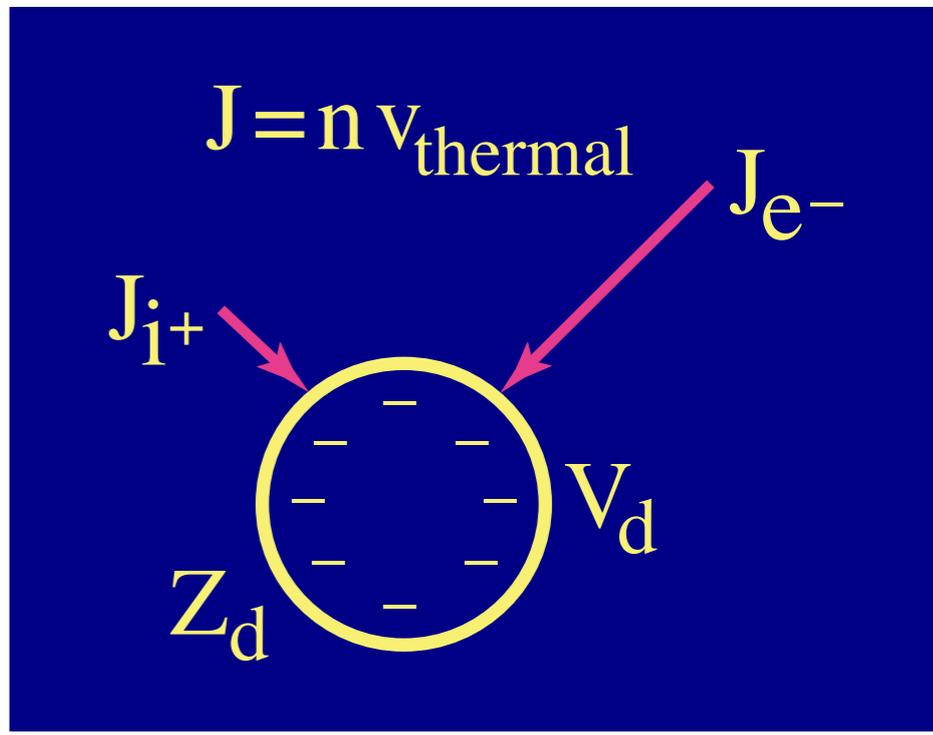
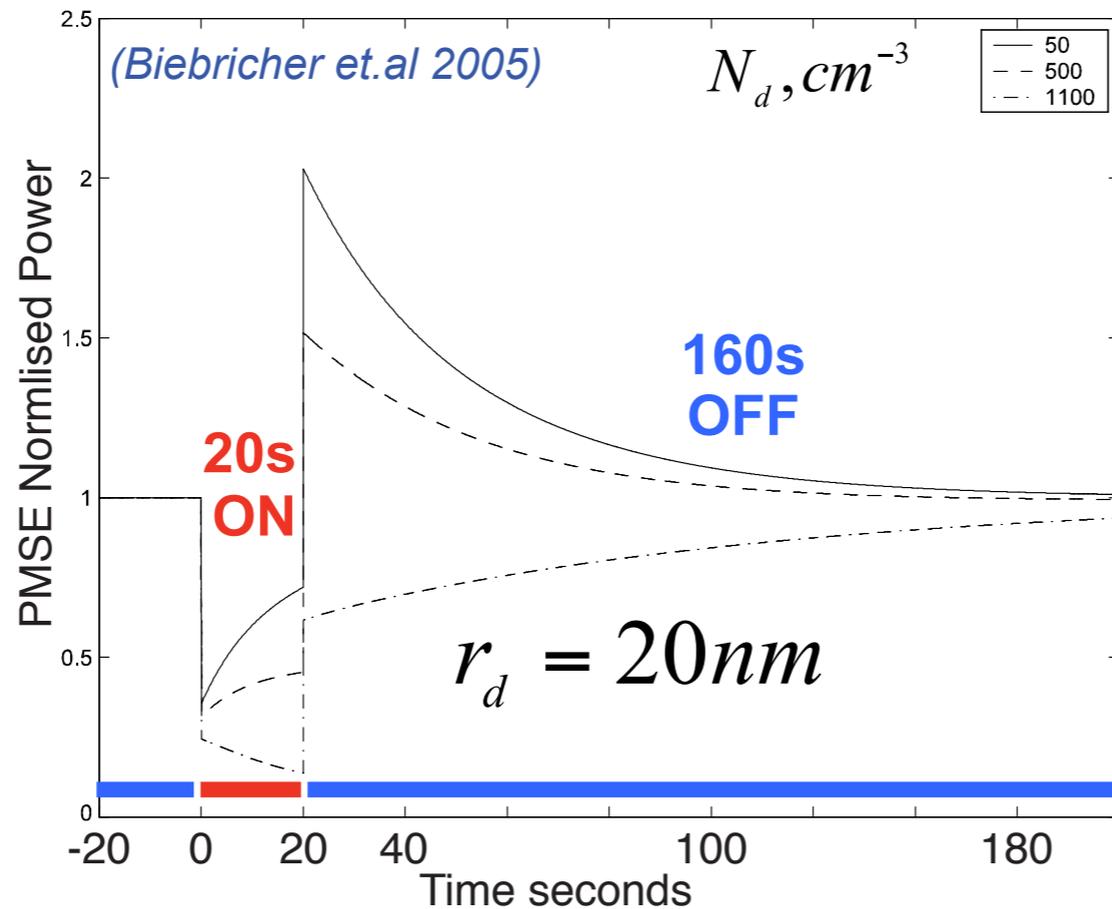
2003 July 2 – EISCAT VHF 224 MHz – PMSE



- Electron temperature  $T_e$  increases
- Electron thermal velocity increases
- Electron current density  $J_e$  increases
- Dust charge  $Z_d$  increases



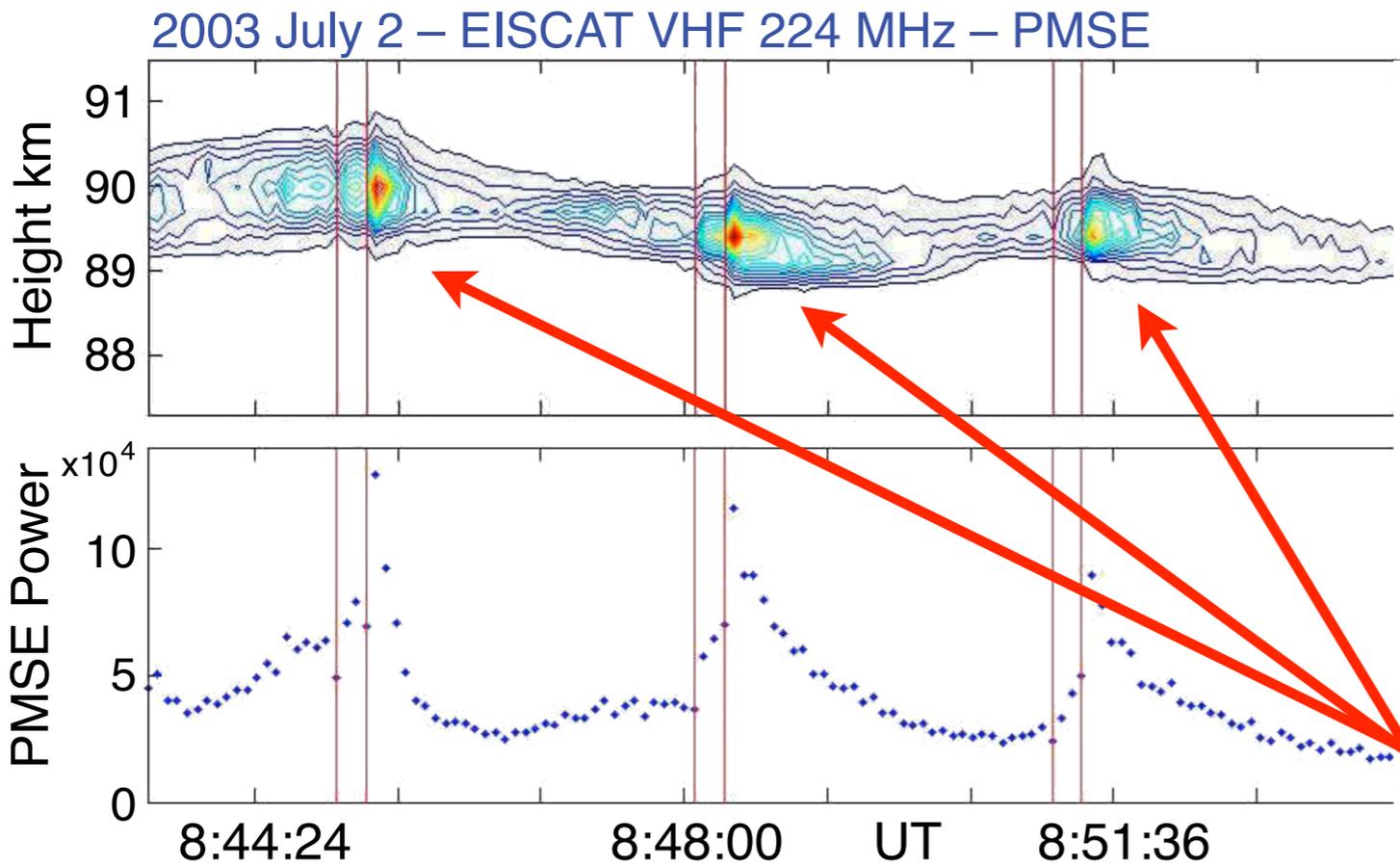
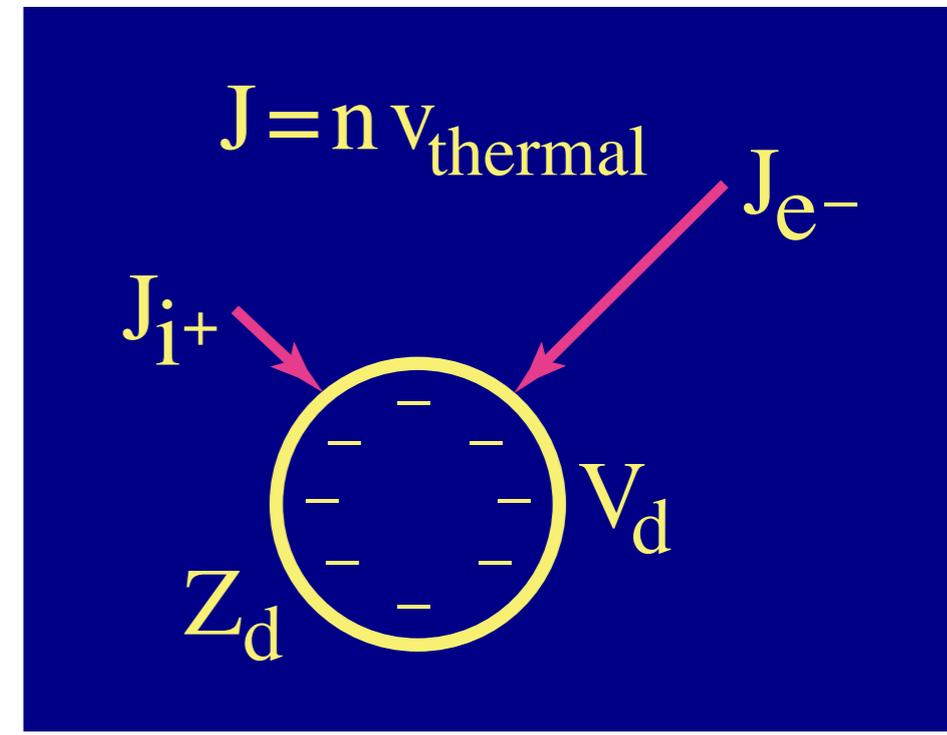
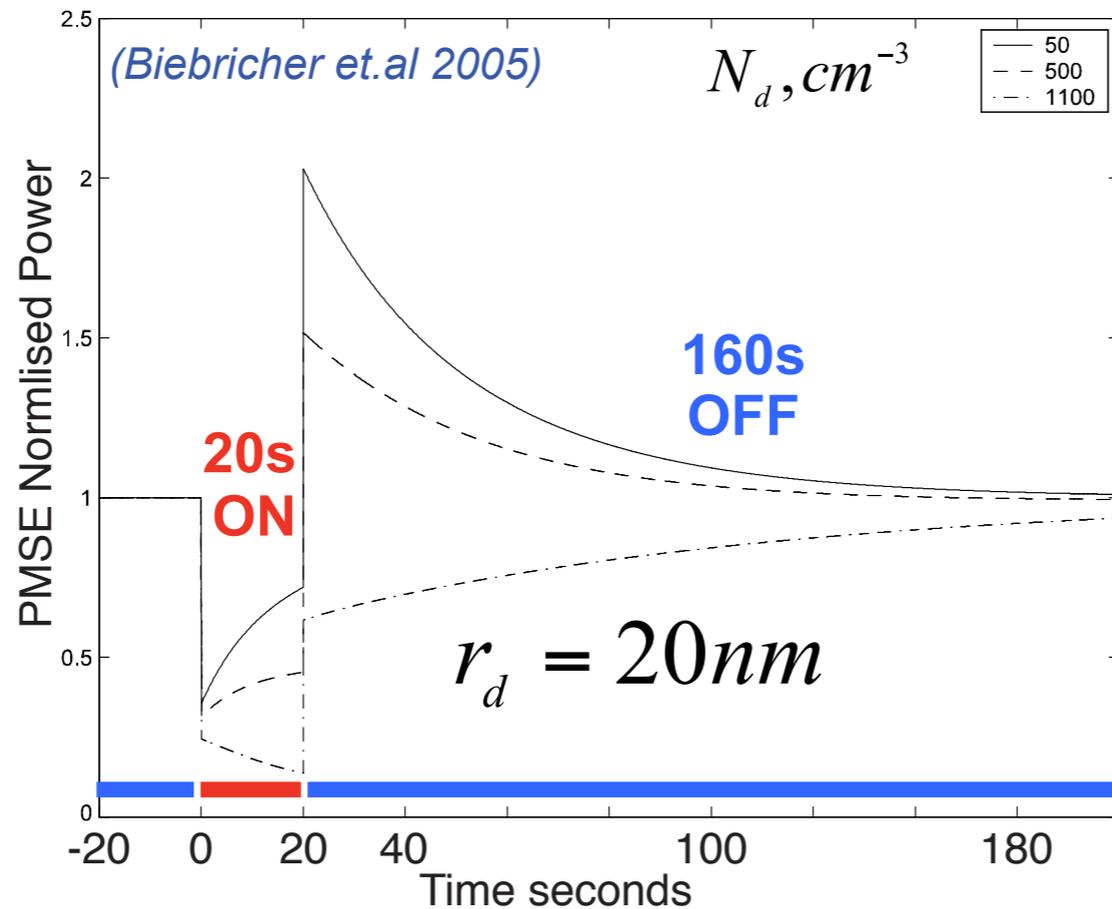
Ove Havnes (2001) predicted the Overshoot effect



- Electron temperature  $T_e$  increases
- Electron thermal velocity increases
- Electron current density  $J_e$  increases
- Dust charge  $Z_d$  increases
- Electron density gradients increase



Ove Havnes (2001) predicted the Overshoot effect

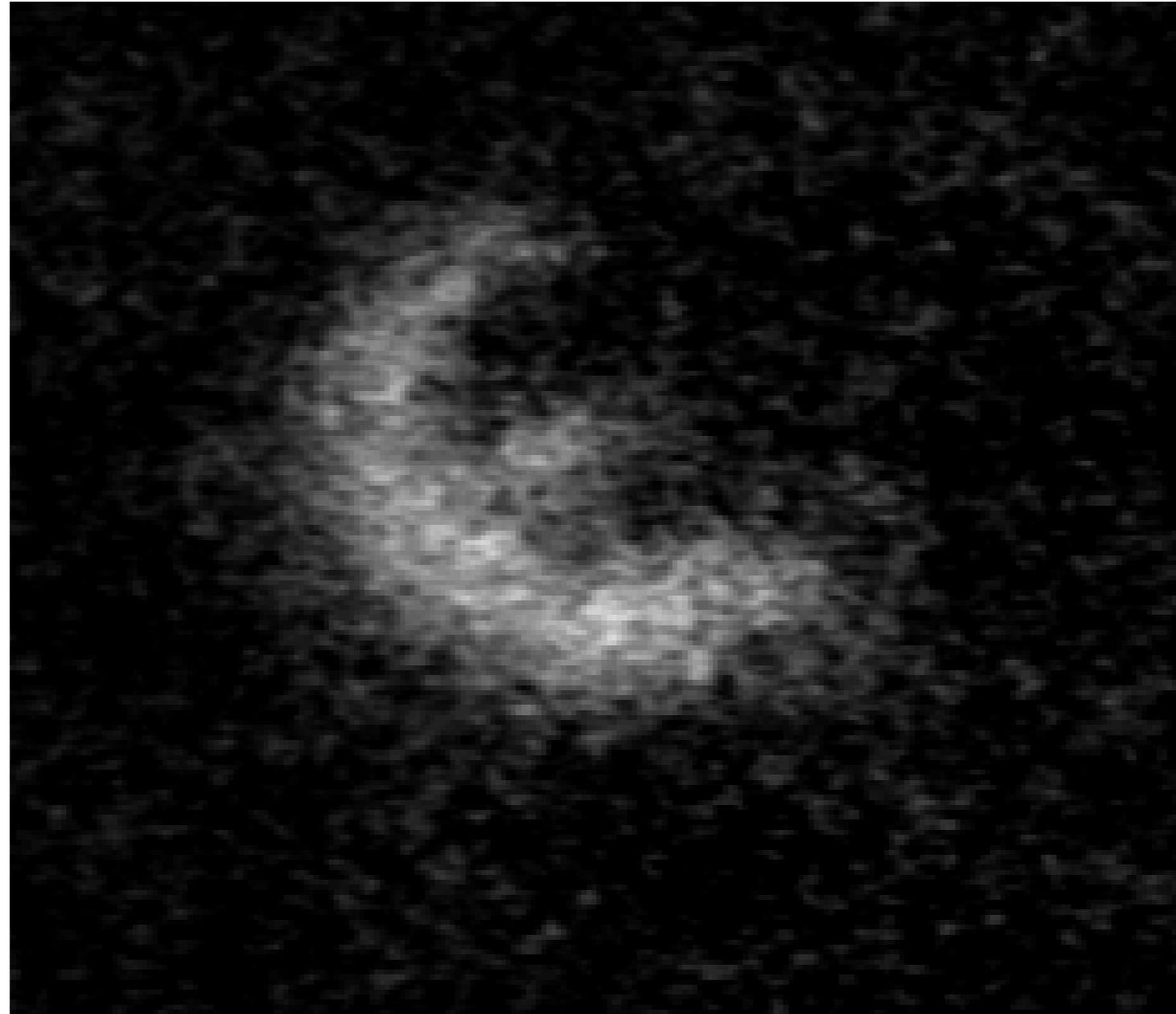


- Electron temperature  $T_e$  increases
- Electron thermal velocity increases
- Electron current density  $J_e$  increases
- Dust charge  $Z_d$  increases
- Electron density gradients increase
- Intensification of radar scattering



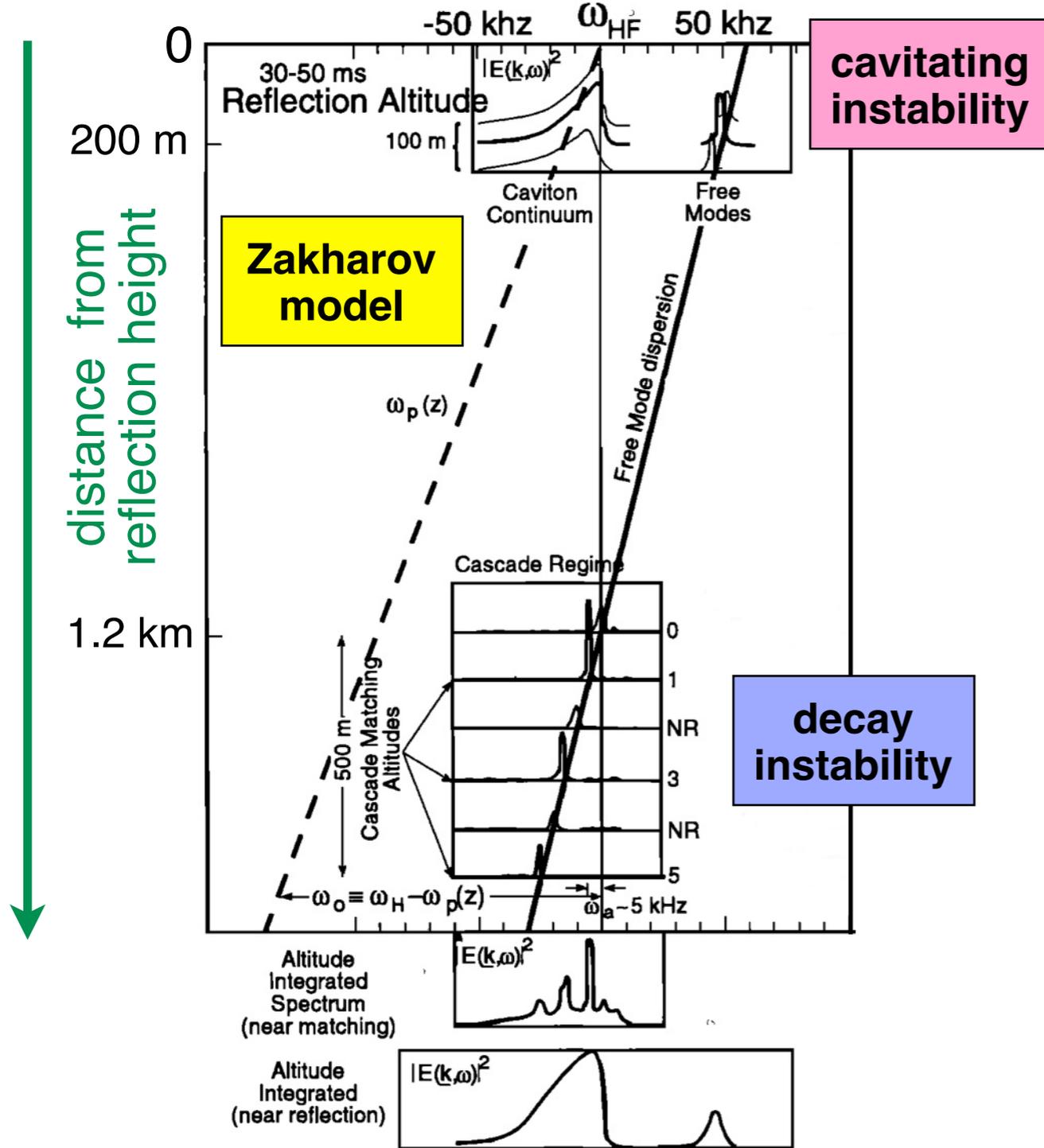
**Painting the sky with the EISCAT Heater:  
The world's first  
*EURORA***

# Painting the sky with the EISCAT Heater: The world's first *EURORA*

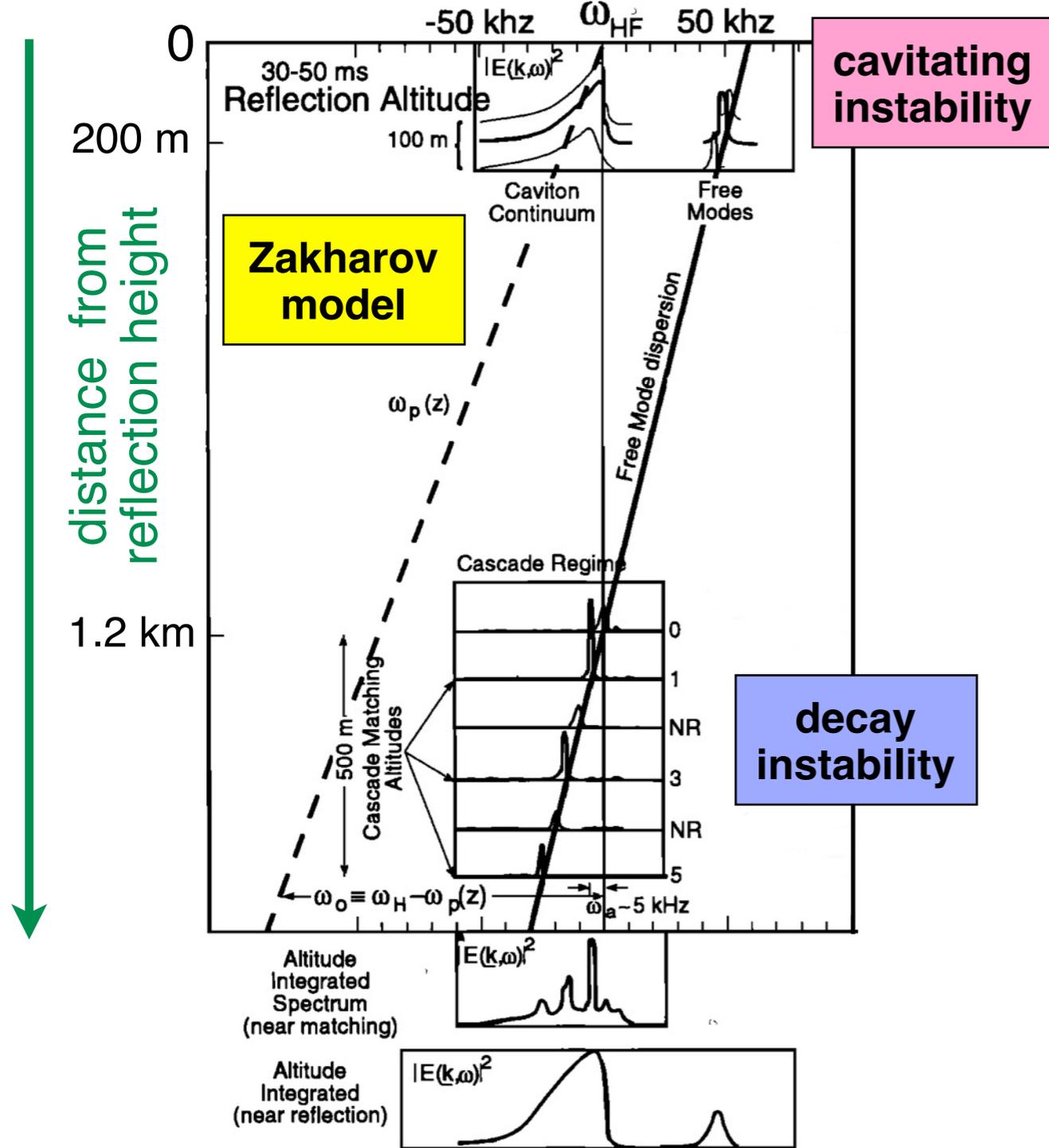


This unique artificial aurora formation was unexpectedly generated by the super-Heater, operating at 630 MW, on 12 November 2001 at 16:41:20 UT with the beam tilted 9° South. The wavelength is 557.7 nm and the image integration is 5 sec.

# 4. Langmuir Turbulence

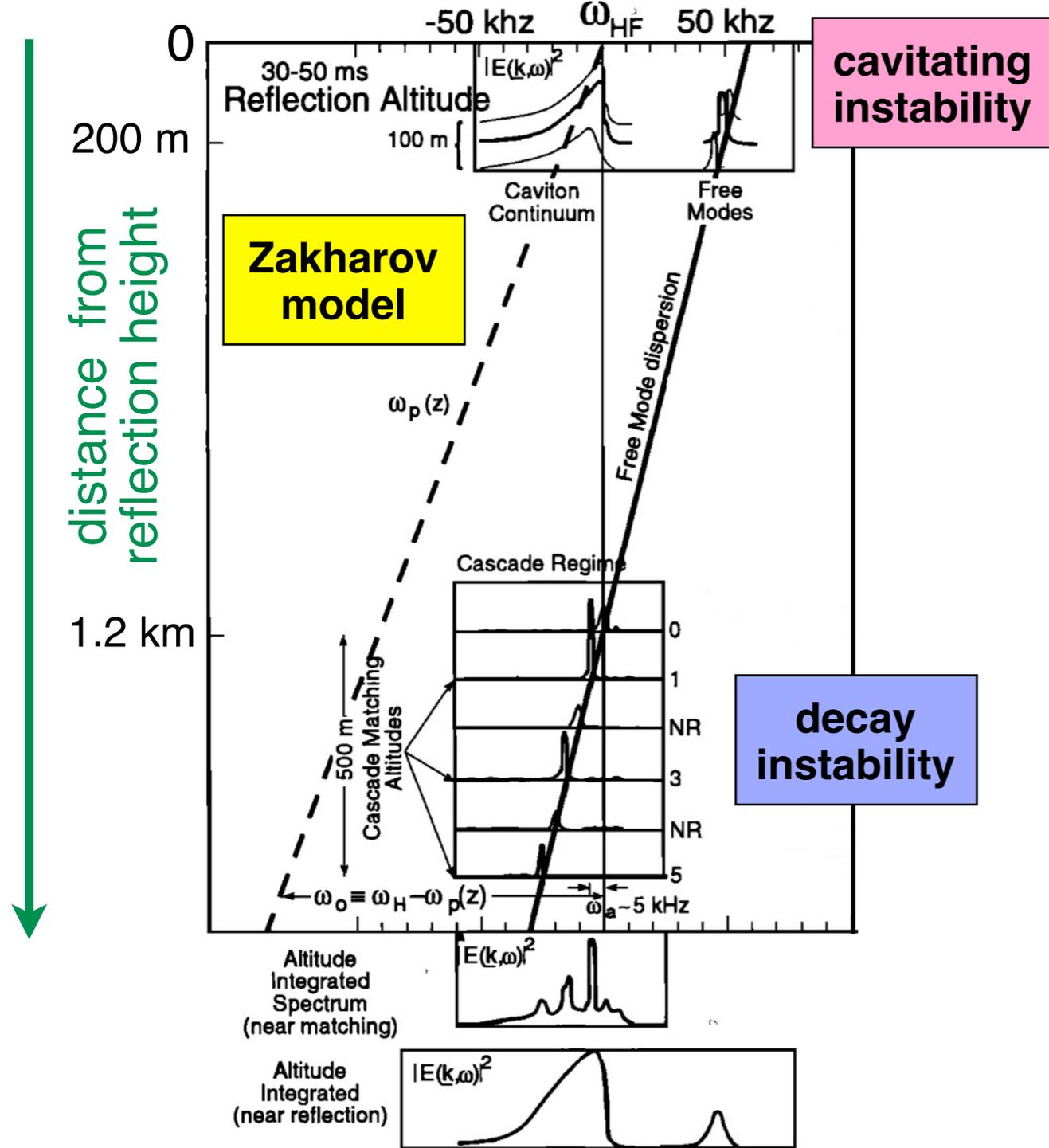


# 4. Langmuir Turbulence



$$\omega_{pe}^2 = \frac{n_e e^2}{\epsilon_0 m_e}$$

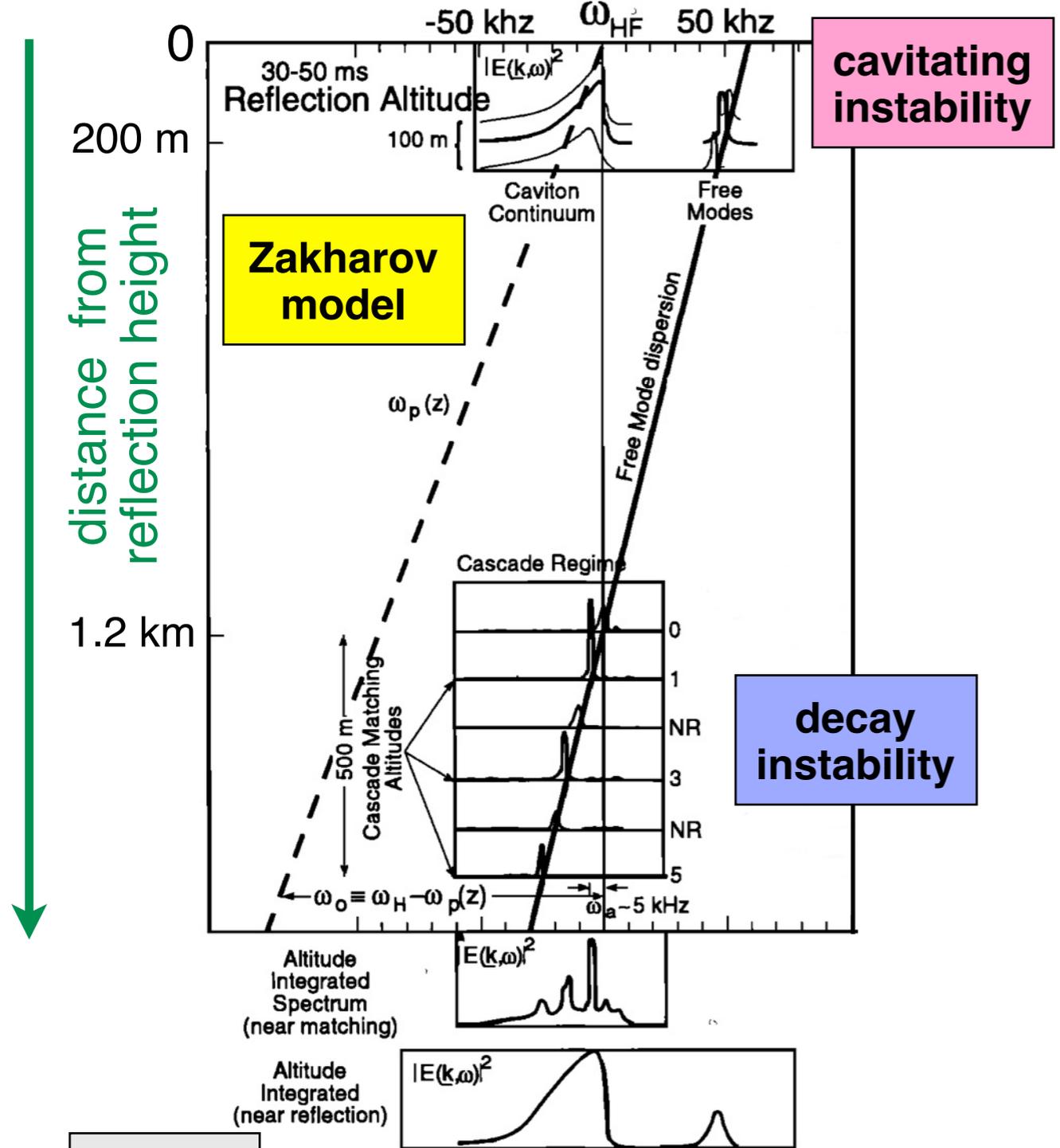
# 4. Langmuir Turbulence



$$\omega_{pe}^2 = \frac{n_e e^2}{\epsilon_0 m_e}$$

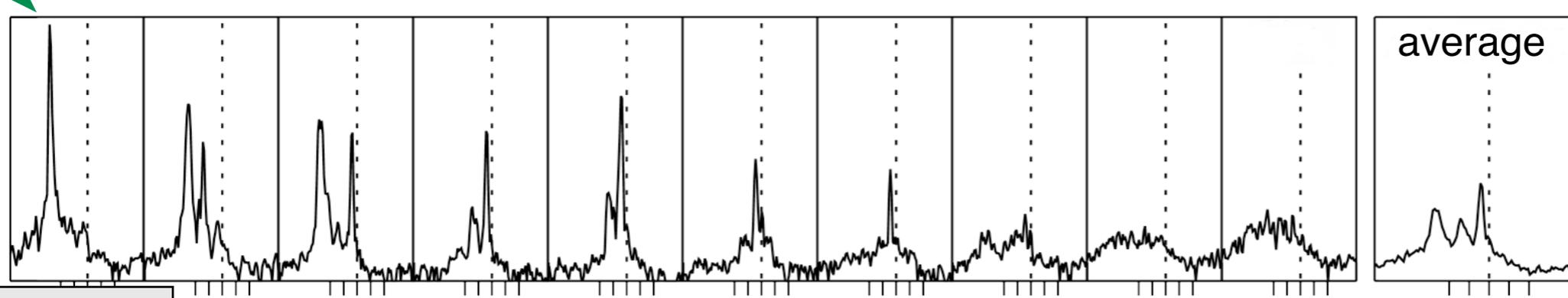
$$\omega_L^2 = \omega_{pe}^2 + 3k_z v_{e,th}^2$$

# 4. Langmuir Turbulence



EISCAT

3000 m

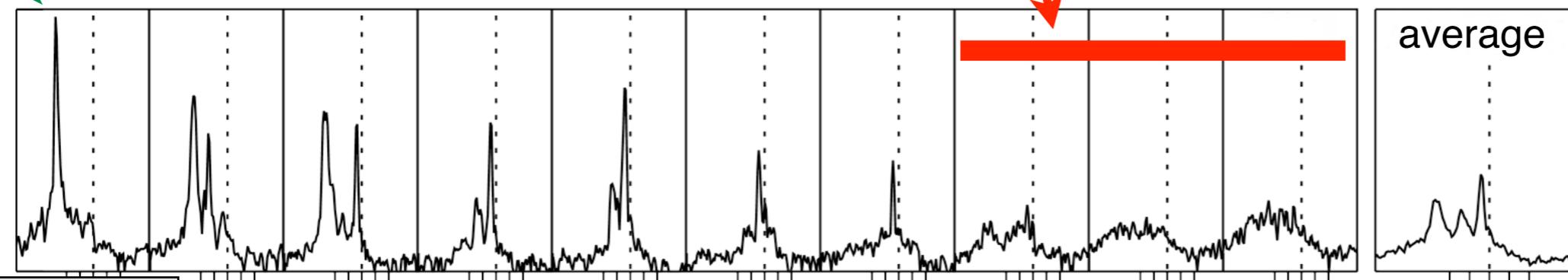
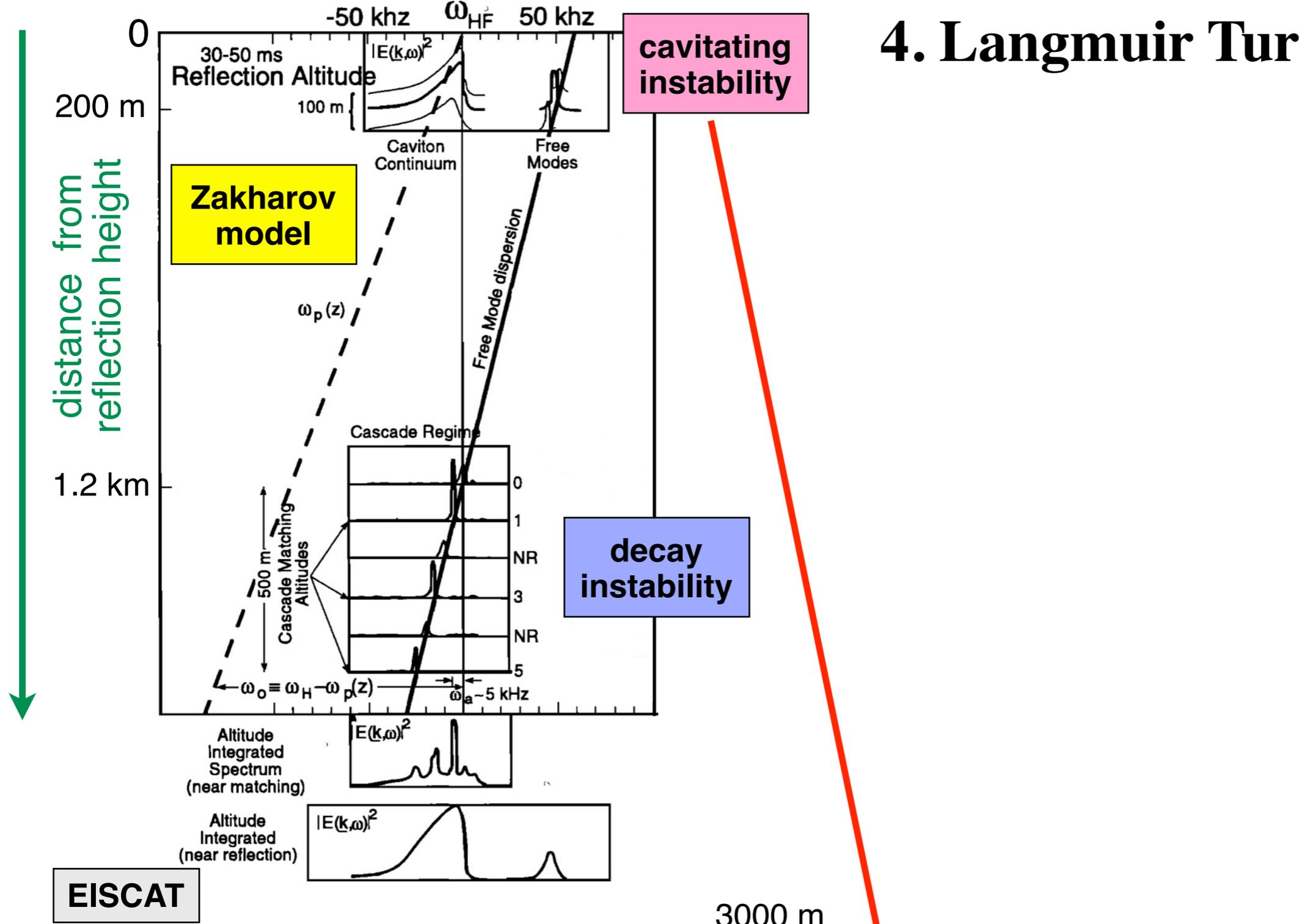


$$\omega_{pe}^2 = \frac{n_e e^2}{\epsilon_0 m_e}$$

$$\omega_L^2 = \omega_{pe}^2 + 3k^2 v_{e,th}^2$$

±50 kHz

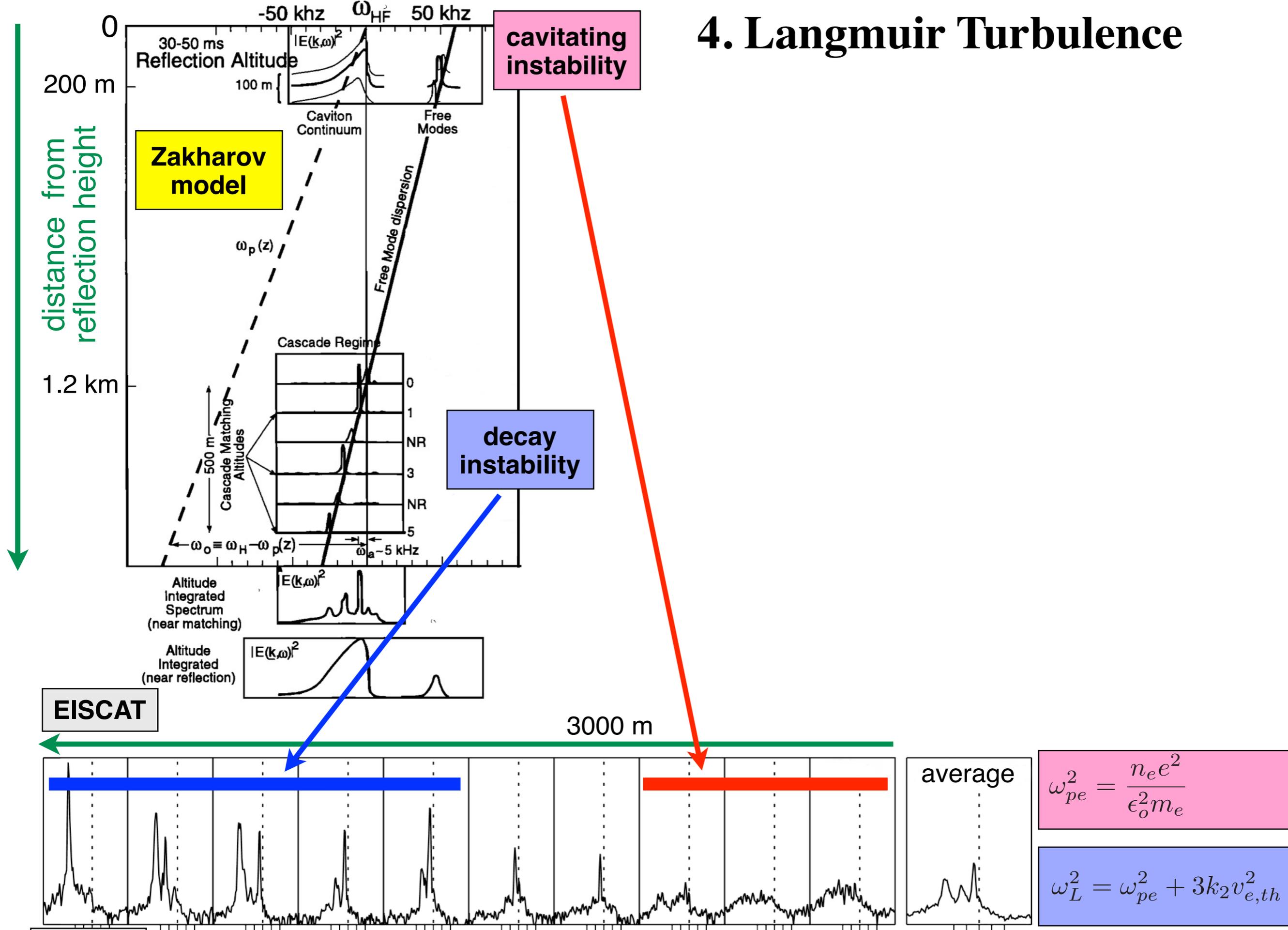
# 4. Langmuir Turbulence



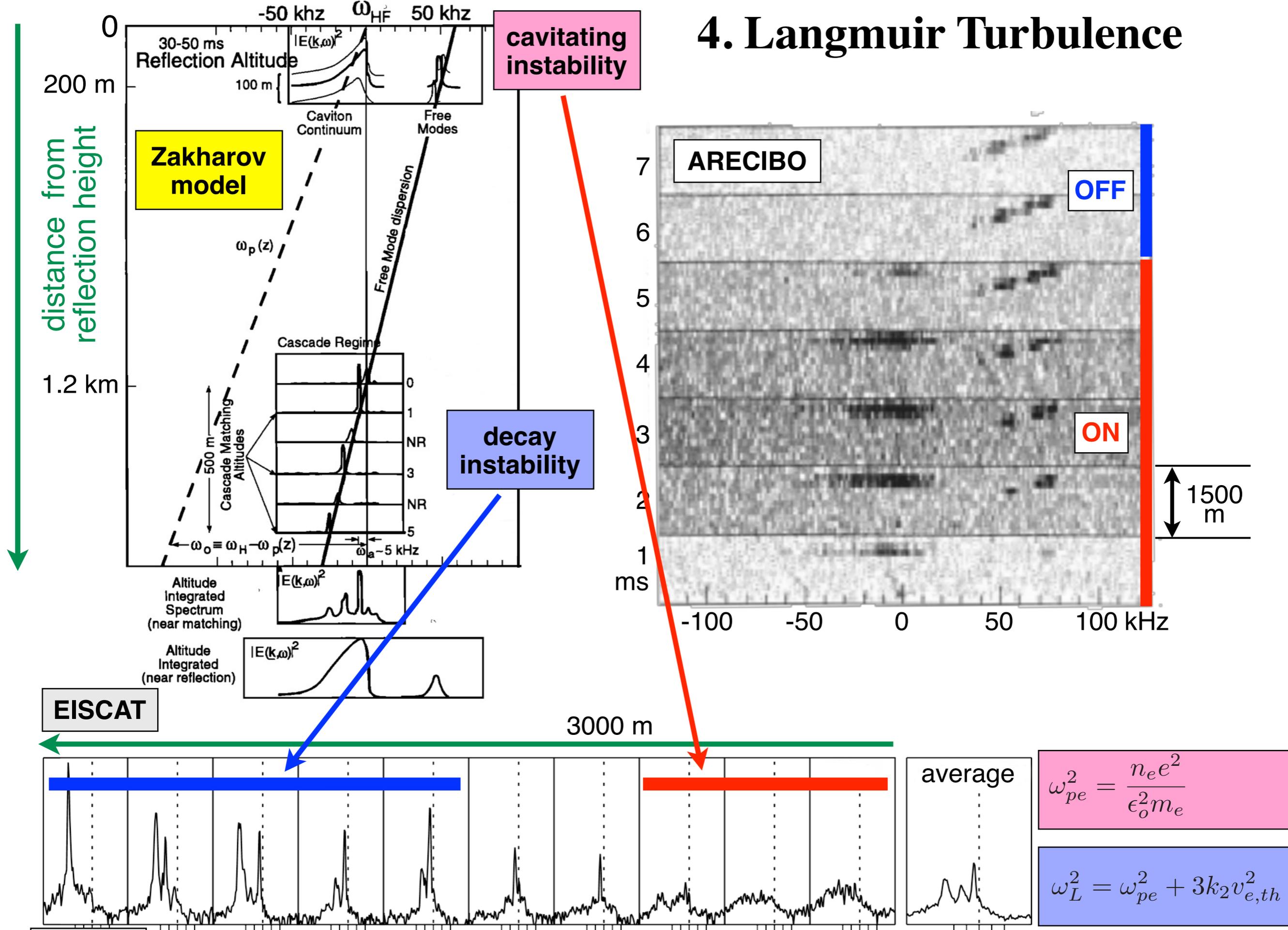
$$\omega_{pe}^2 = \frac{n_e e^2}{\epsilon_0 m_e}$$

$$\omega_L^2 = \omega_{pe}^2 + 3k_2 v_{e,th}^2$$

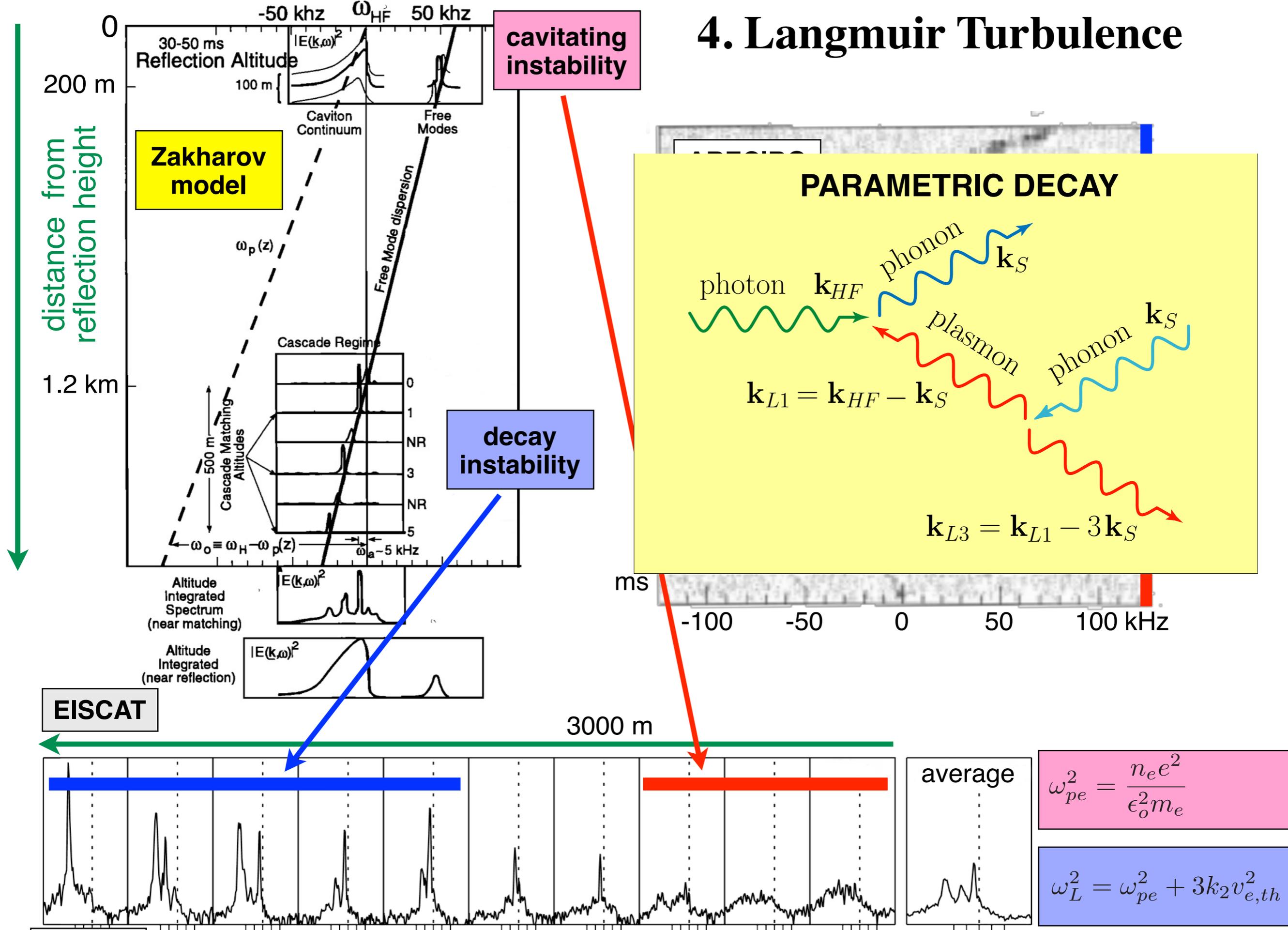
# 4. Langmuir Turbulence



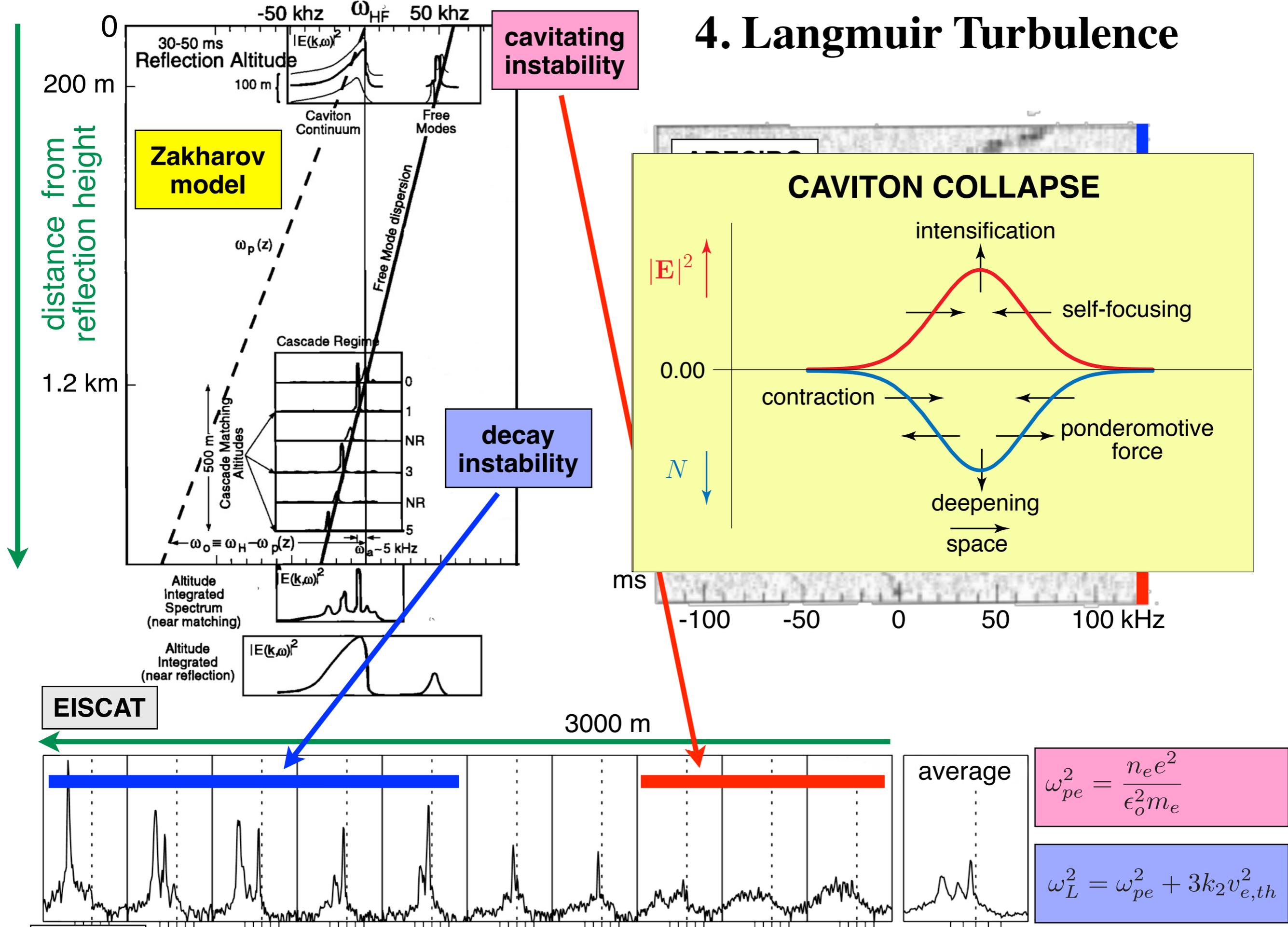
# 4. Langmuir Turbulence



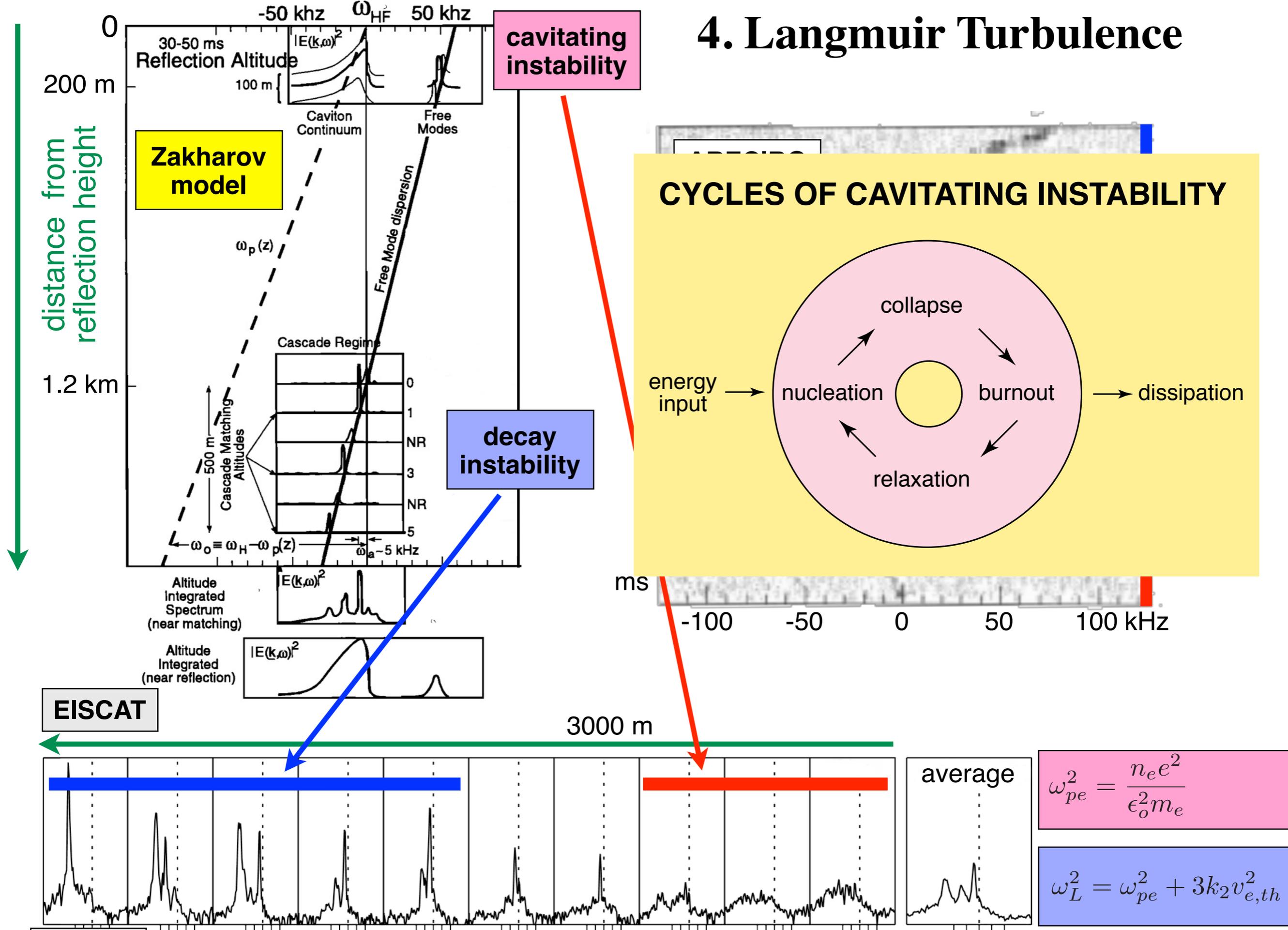
# 4. Langmuir Turbulence



# 4. Langmuir Turbulence



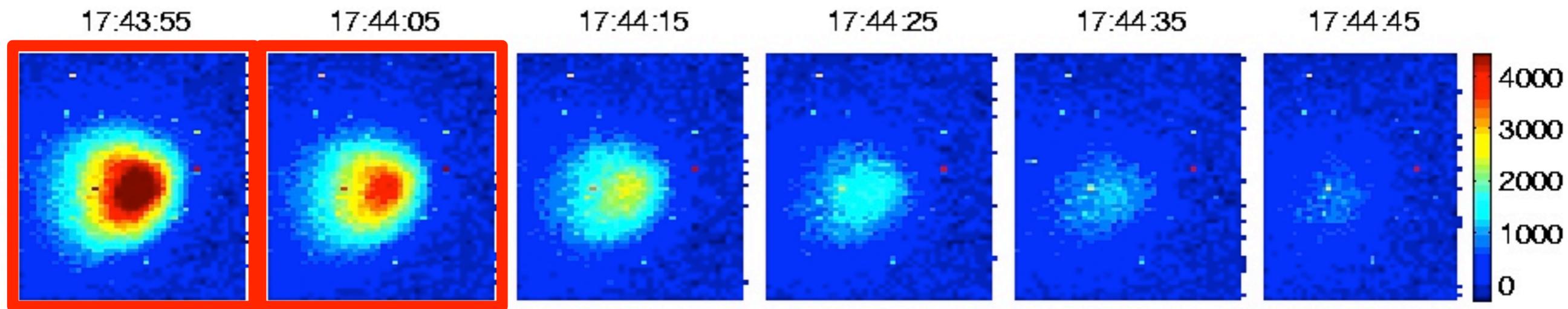
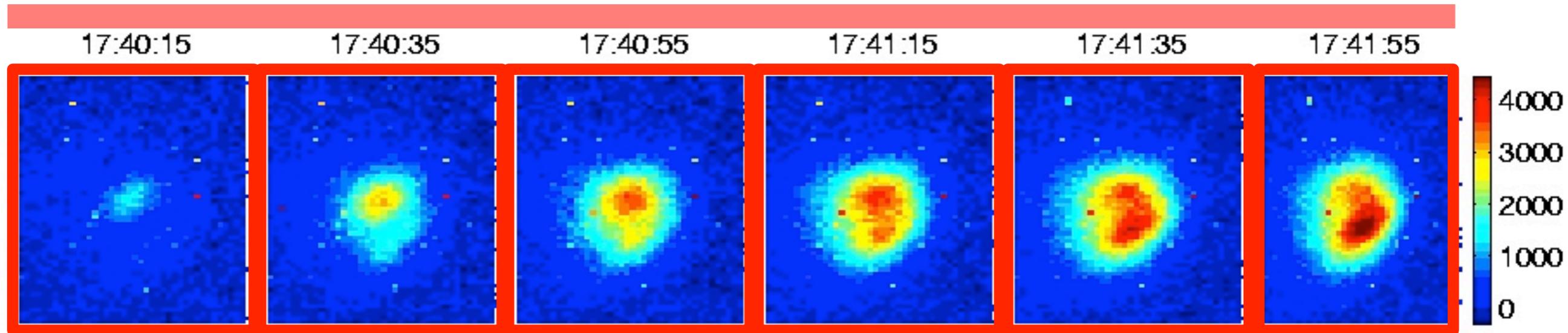
# 4. Langmuir Turbulence



# ARTIFICIAL AURORA

16 Feb 1999 4.04 MHz ERP = 75 MW O-mode

**17:40 HF ON**



**17:44 HF OFF**

# the future: EISCAT\_3D



# the future: EISCAT\_3D

- 4th generation IS radar
- in the roadmap of ESFRI
- raising funds at present
- cost EUR 130 million
- construction 2015–2021

incoherent scatter theory is one of the first and most compelling successes of linear plasma physics theory.

**Don Farley**

... the predictions of the 2-D Langmuir turbulence theory in [ionospheric heating] are now well verified. It is one of the best verified regimes of plasma turbulence.

**Don DuBois**

thank you !

# RADAR SOUNDING OF THE AURORAL PLASMA

by

CESAR LA HOZ

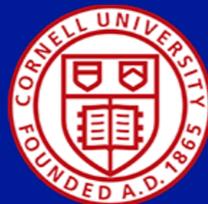
[cesar.la.hoz@uit.no](mailto:cesar.la.hoz@uit.no)

with contributions by my friends

Brett Isham, Mike Kosch and Mike Rietveld

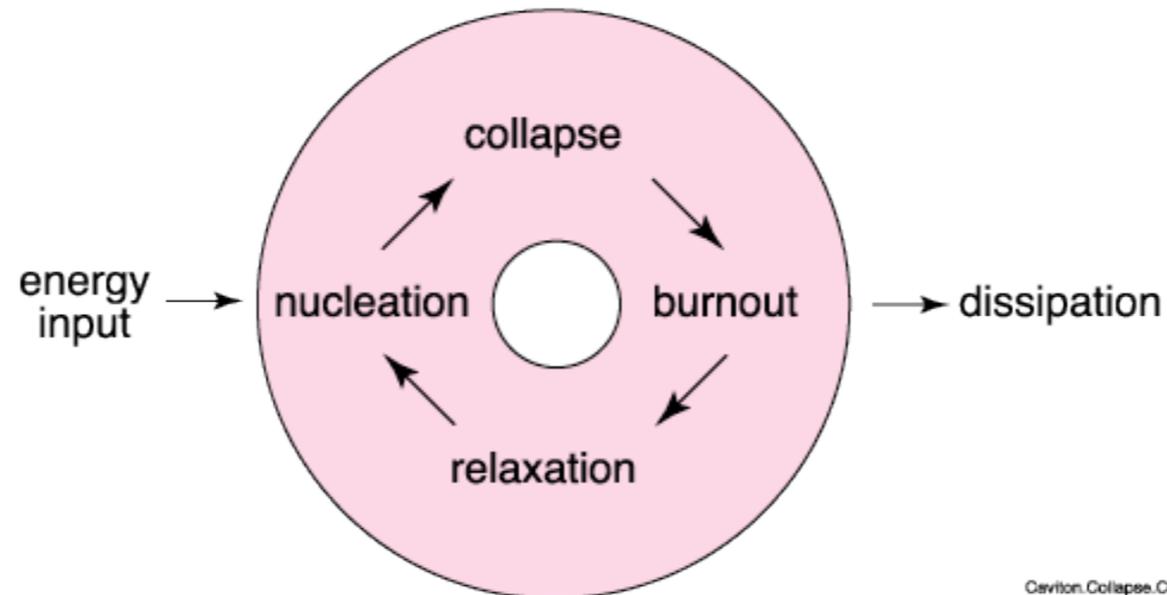
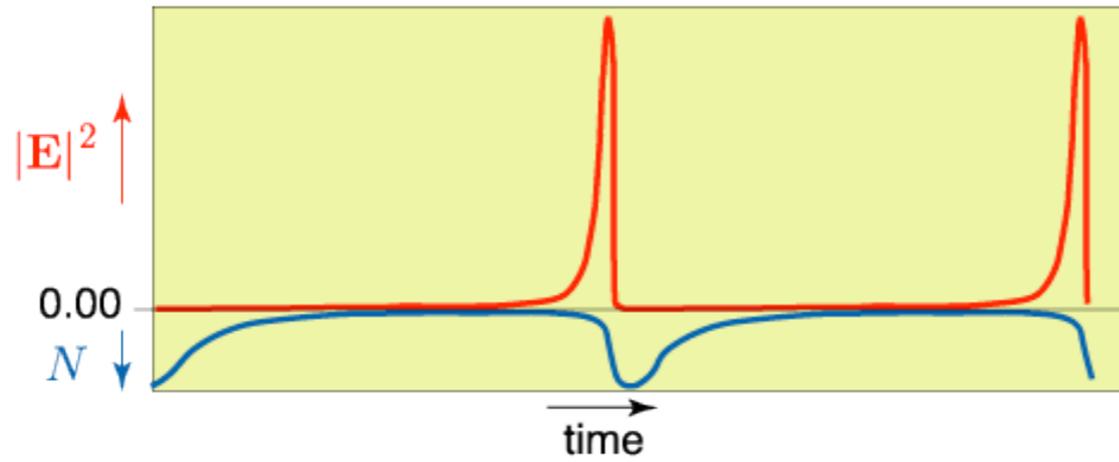
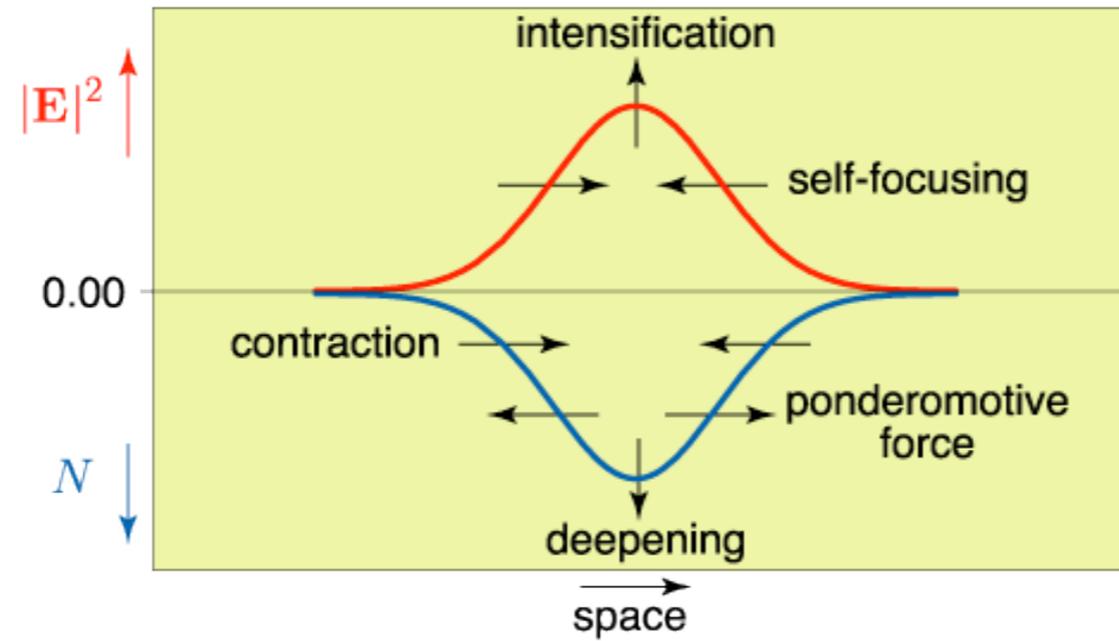


THE ARCTIC UNIVERSITY OF NORWAY



CORNELL UNIVERSITY

# STRONG LANGMUIR TURBULENCE CAVITON COLLAPSE



$\Delta t = 10 \text{ s}$

18:19:30

18:19:40

18:19:50

18:20:00

UT time

285.2

289.0

292.7

298.5

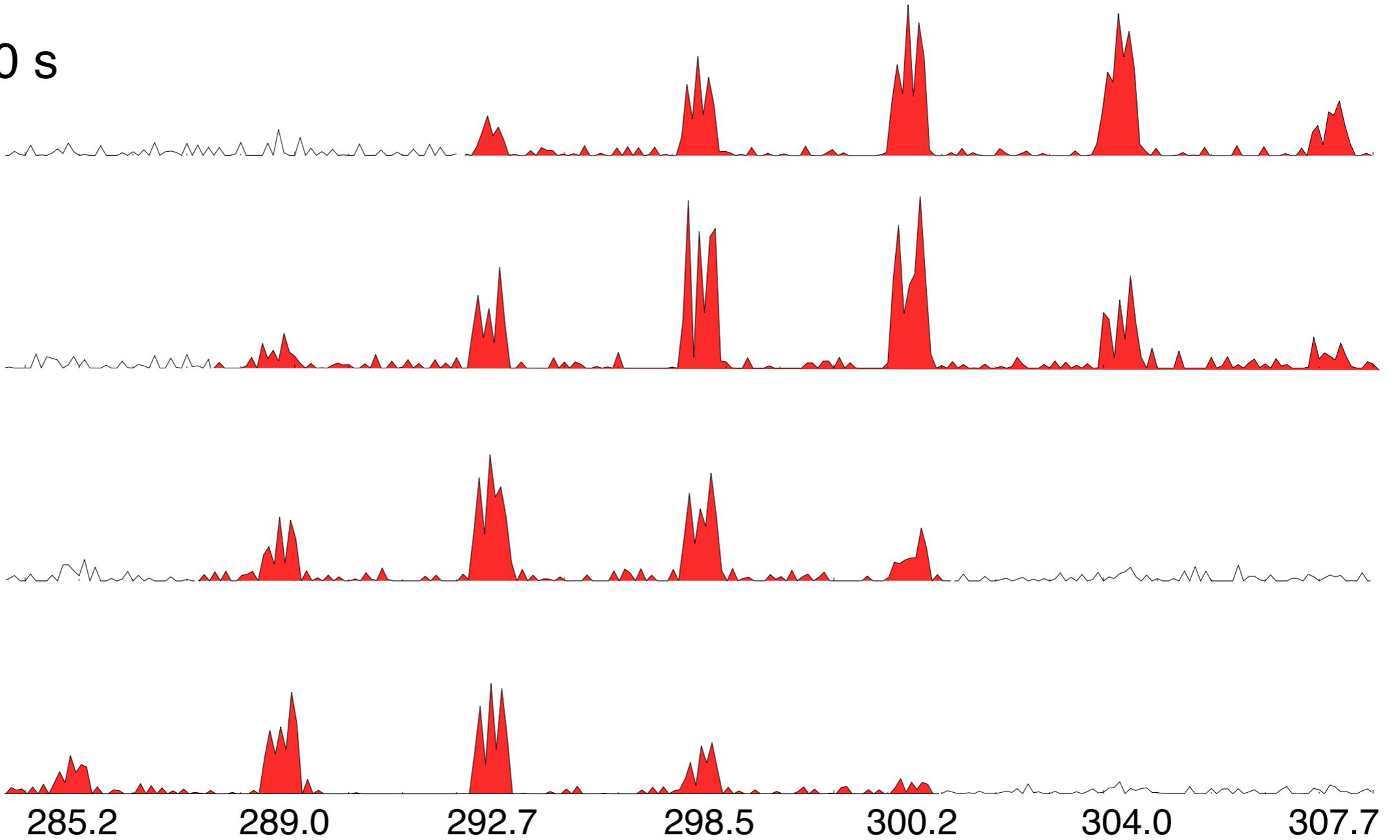
300.2

304.0

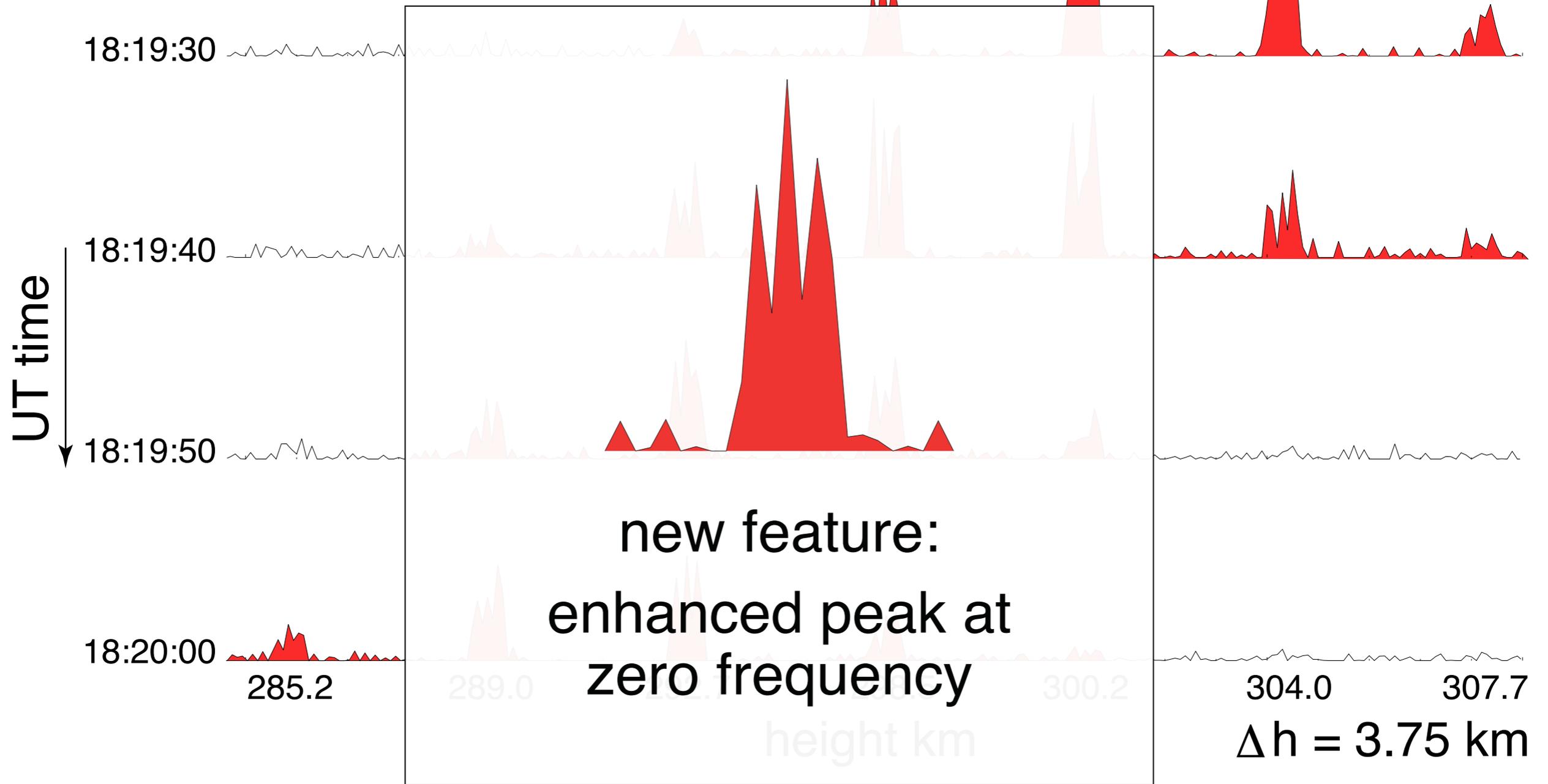
307.7

height km

$\Delta h = 3.75 \text{ km}$



$\Delta t = 10 \text{ s}$



$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

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$$\epsilon(\mathbf{k}, \omega) = 0$$

# Ion Line $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

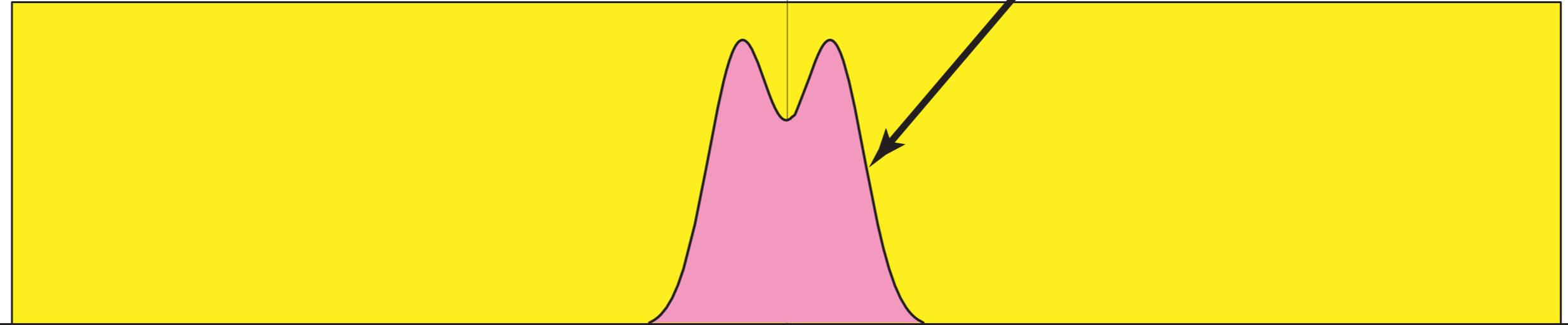
$$\epsilon(\mathbf{k}, \omega) = 0$$

$$\omega_{ia}(k) \approx k \sqrt{\frac{T_e + 3 T_i}{m_i}}$$

IS.SpecFormula4.ai6

$-\omega_{il}$        $\omega_{il}$

**Ion Line**



## Plasma Line $S_{PL}(\mathbf{k}, \omega)$

## Ion Line $S_{IL}(\mathbf{k}, \omega)$

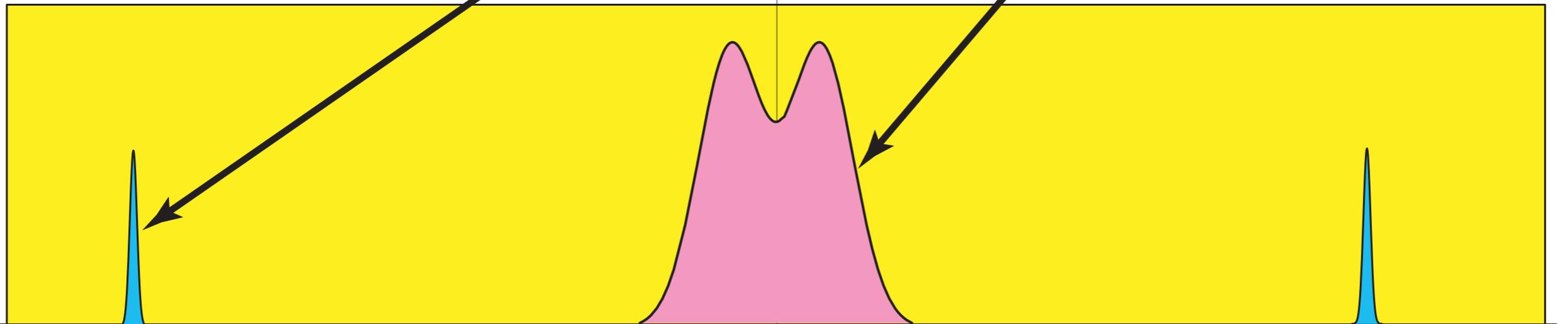
$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

$$\epsilon(\mathbf{k}, \omega) = 0$$

$$\omega_{pl}(k) \approx \omega_{pe} (1 + 3 \lambda_D^2 k^2)$$

$$\omega_{ia}(k) \approx k \sqrt{\frac{T_e + 3 T_i}{m_i}}$$

IS.SpecFormula4.ai6



$$-\omega_{pl}$$

**downshifted  
Plasma Line**

$$-\omega_{il} \quad \omega_{il}$$

**Ion Line**

$$\omega_{pl}$$

**upshifted  
Plasma Line**

**Plasma Line**  $S_{PL}(\mathbf{k}, \omega)$

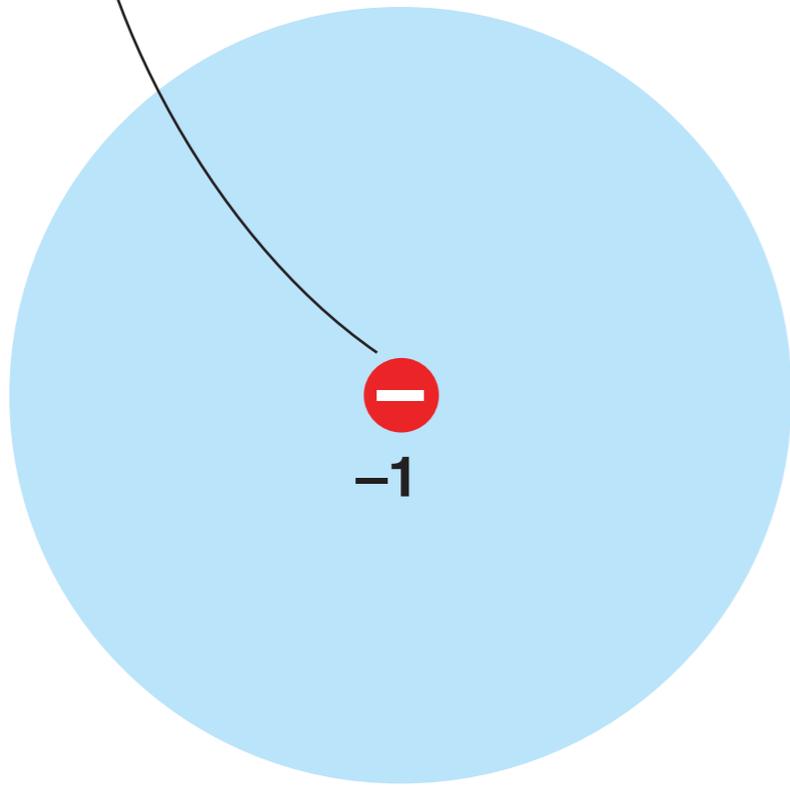
**Ion Line**  $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

## Plasma Line $S_{PL}(\mathbf{k}, \omega)$

## Ion Line $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

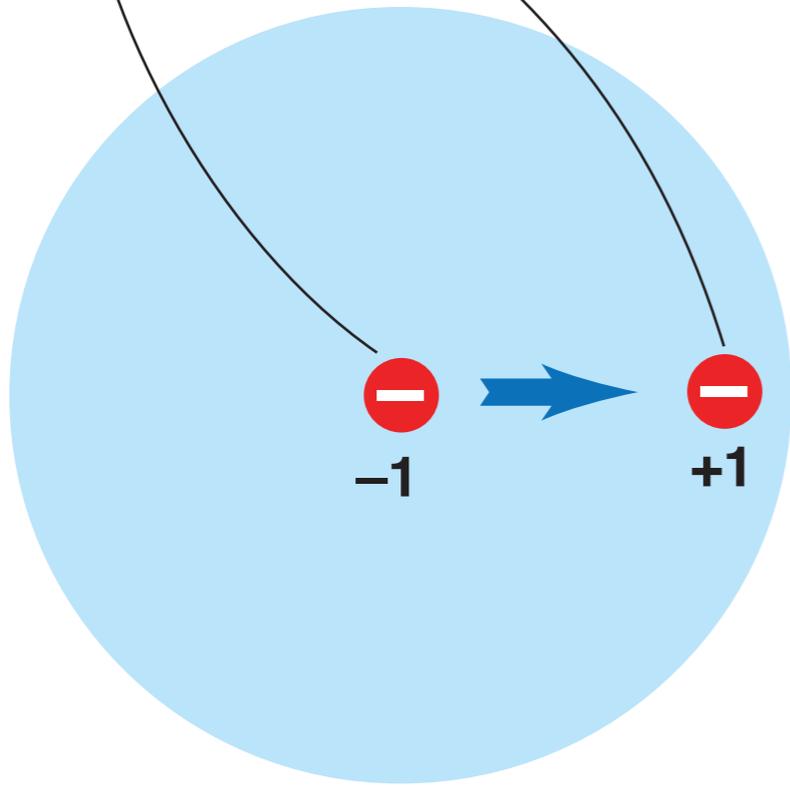


## Plasma Line $S_{PL}(\mathbf{k}, \omega)$

## Ion Line $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

electron  
with cloud

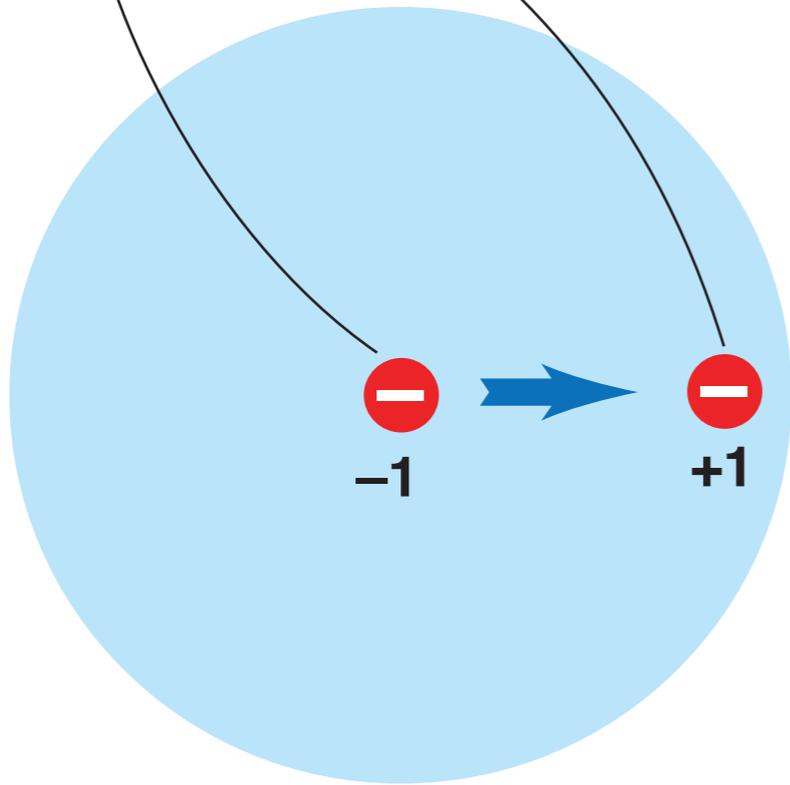


## Plasma Line $S_{PL}(\mathbf{k}, \omega)$

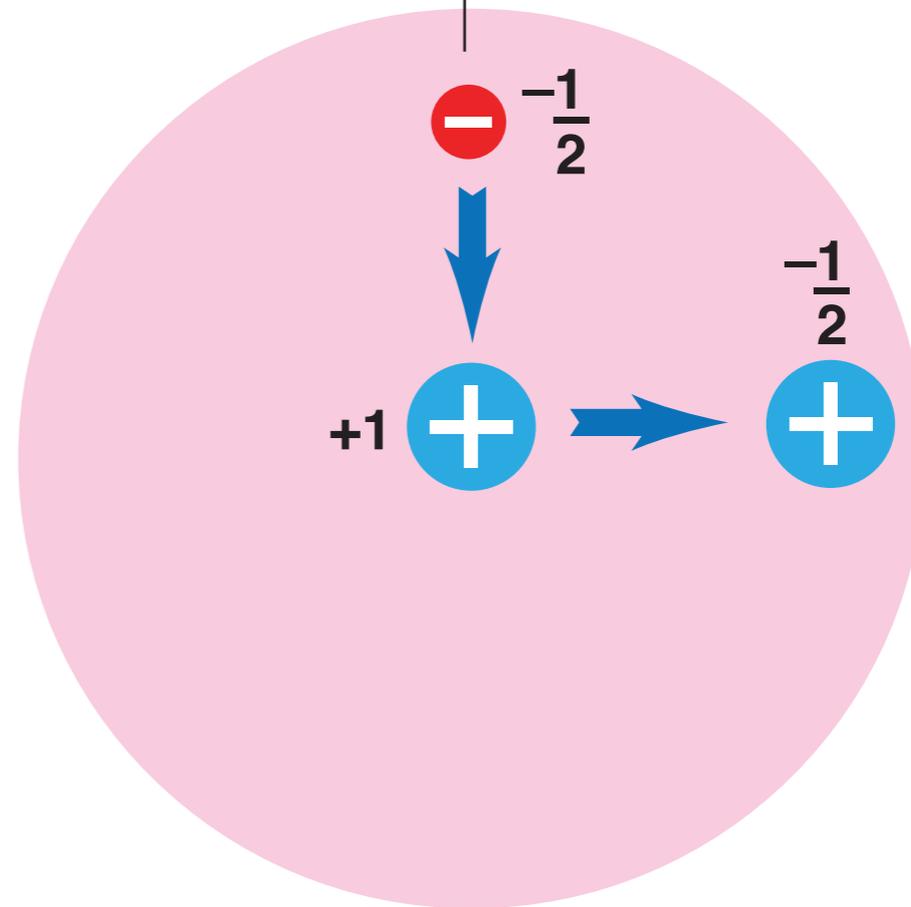
## Ion Line $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

electron  
with cloud



ion with  
cloud

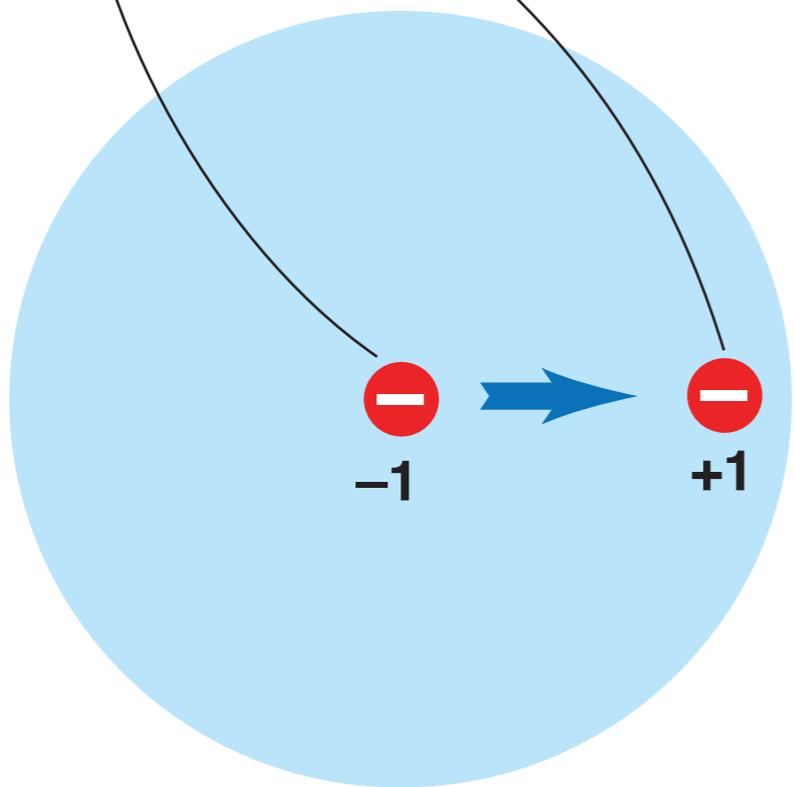


## Plasma Line $S_{PL}(\mathbf{k}, \omega)$

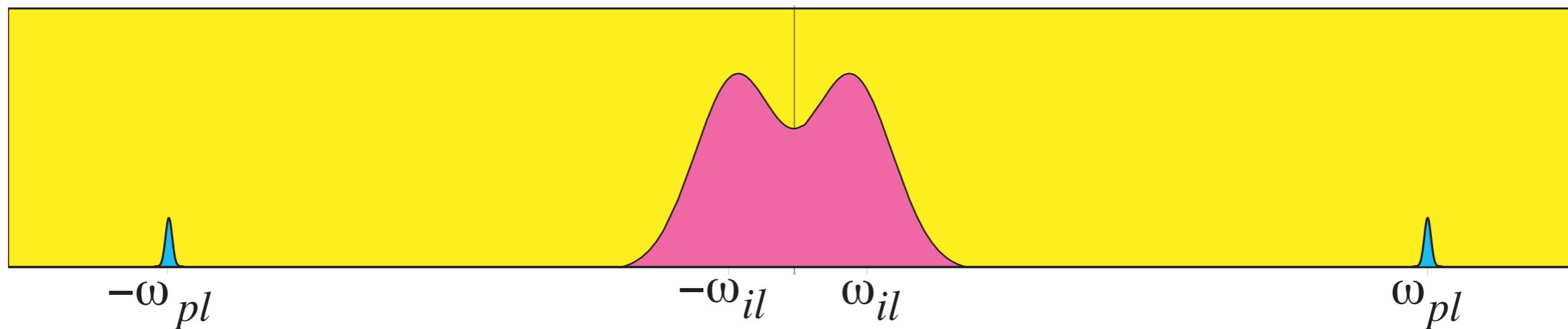
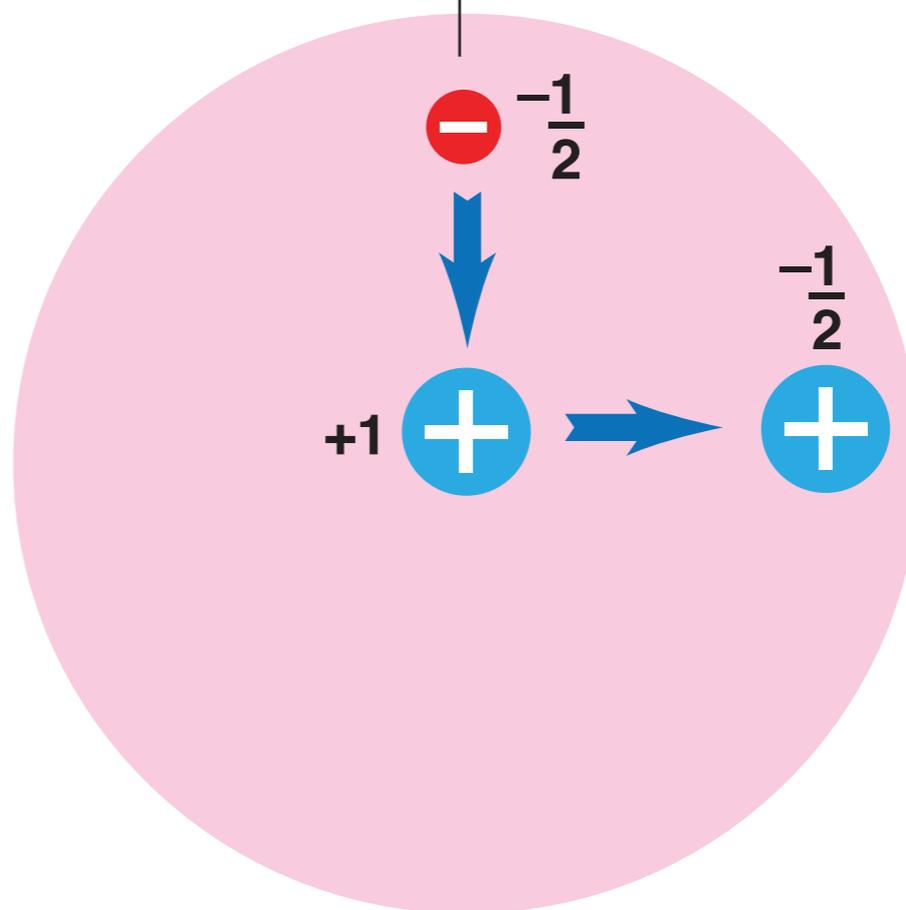
## Ion Line $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v} + \sum_i N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) d^3 \mathbf{v}$$

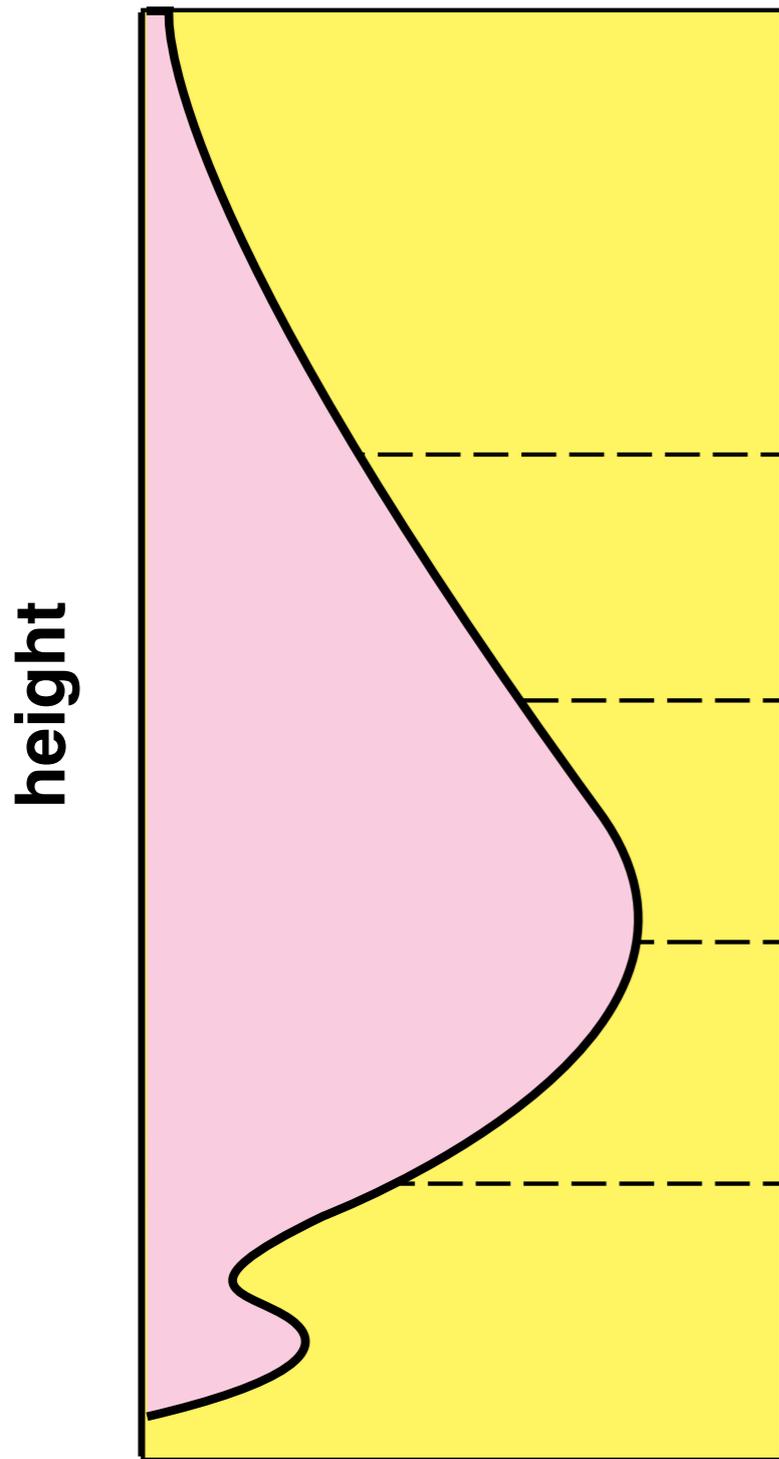
electron  
with cloud



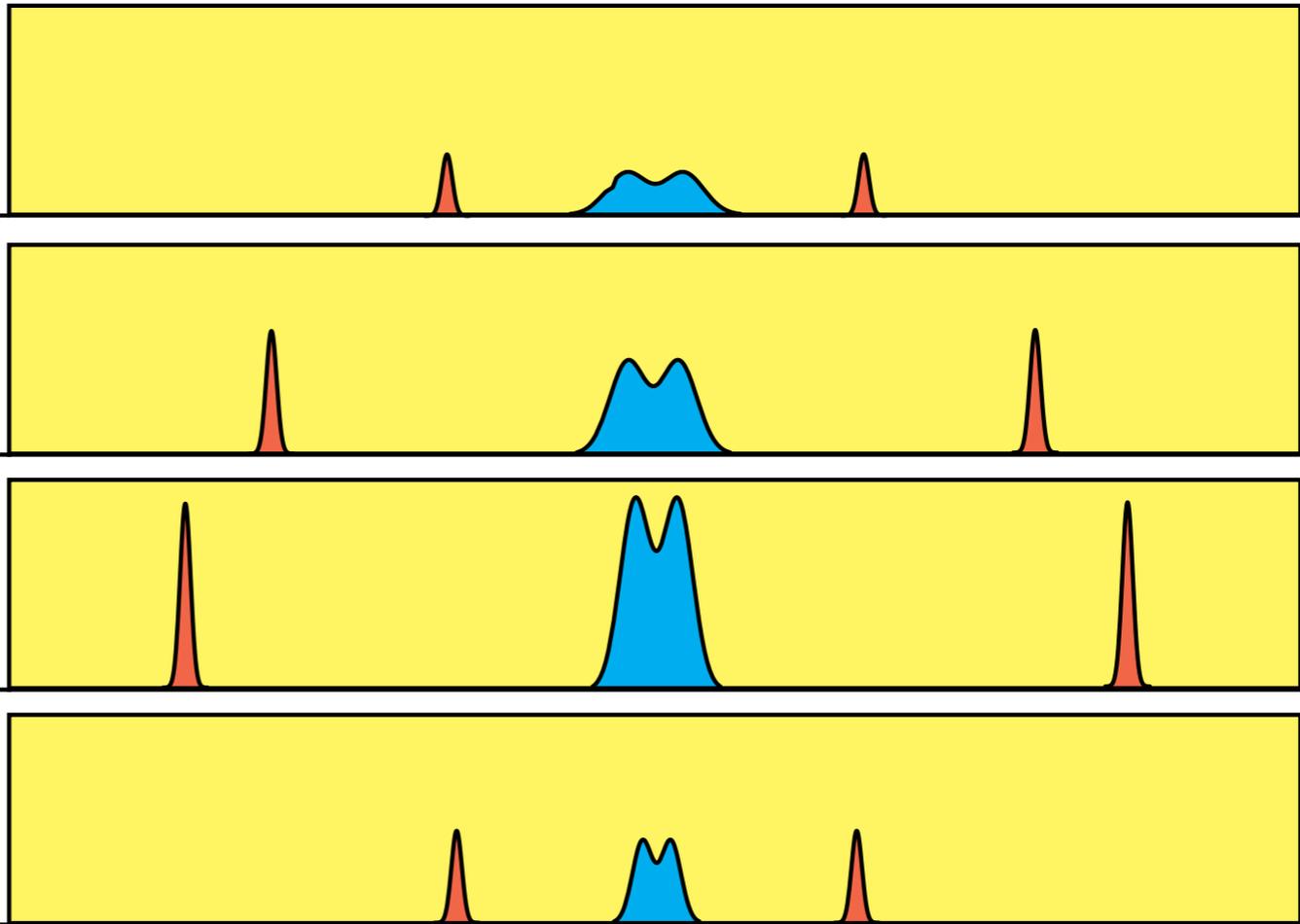
ion with  
cloud



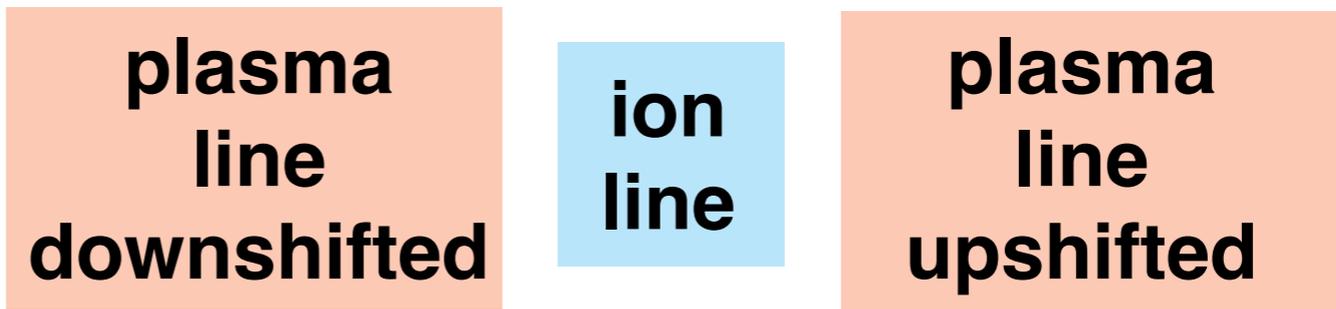
# electron density profile



# Incoherent scatter spectra



spectral amplitude



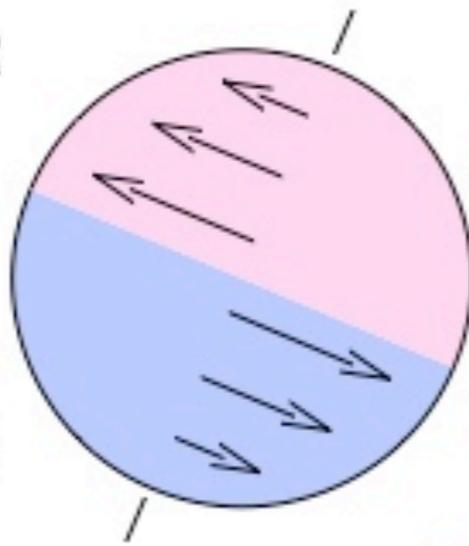
frequency



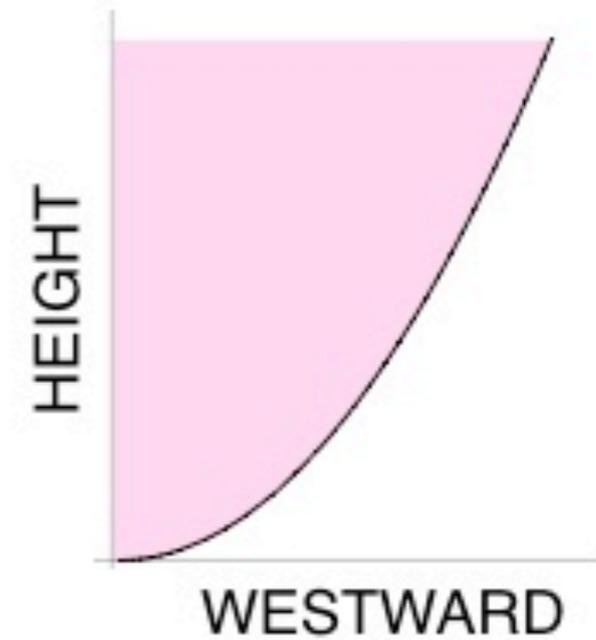
# The Polar Mesosphere is Colder in Summer than in Winter

SUMMER

WINTER



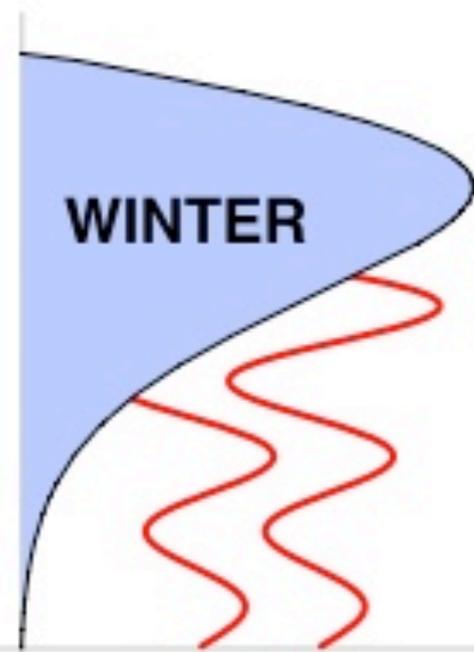
ZONAL WINDS



**Not observed !**

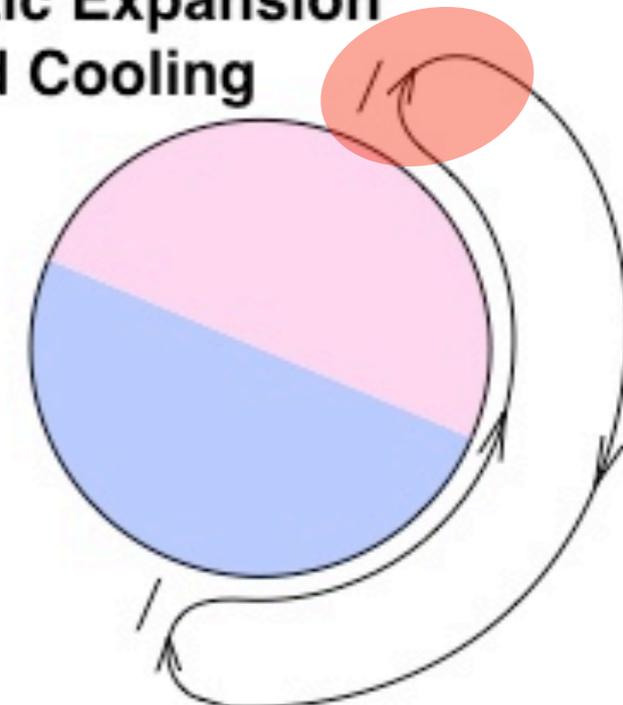
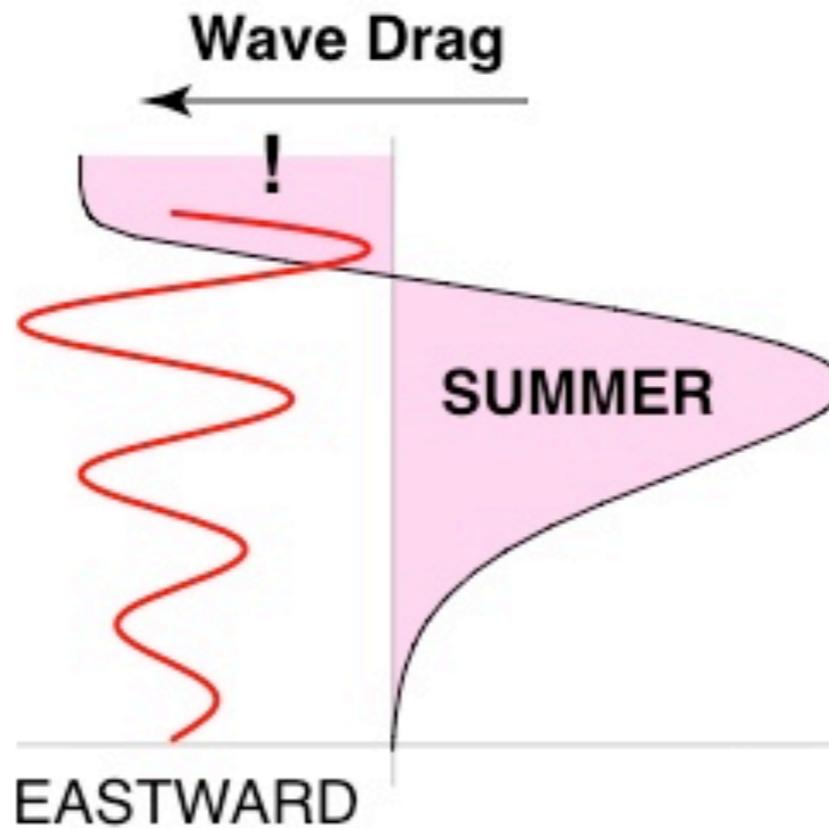
**REFRIGERATOR !**

Adiabatic Expansion and Cooling



ZONAL WINDS

GRAVITY WAVES



MERIDIONAL WINDS

# The Polar Mesosphere is Colder in Summer than in Winter

SUMMER

WINTER

- gravity waves break up in the mesosphere
- reversal of the sun-driven zonal winds
- reversal of pole-to-pole meridional wind
- vertical upwelling in summer pole
- adiabatic expansion in mesosphere
- cooling of the summer mesosphere

GRAVITY WAVES

EASTWARD

SUMMER

MERIDIONAL WINDS

